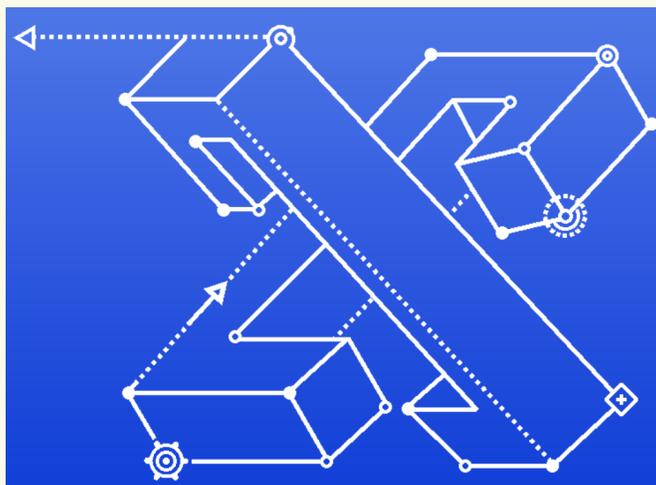


Conflux Protocol Specification

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Abstract

The success of Bitcoin and its follow-ups have demonstrated the value of decentralized consensus system among anonymous participants not trusting each other. On top of the consensus network there can be a public ledger or even a general state transition machine, such that all participants agree on the state of the ledger or the state machine. Conceptually the state machine can be Turing-complete and hence essentially a “world computer” shared by all participants, whose results cannot be tampered by any single person or entity. However, the processing power of the shared state machine is currently bottlenecked on the throughput of underlying consensus system.

Conflux implements a Turing-complete state machine on top of a high-throughput consensus network. To achieve a throughput of thousands of transactions per second, Conflux guarantees consensus on the total order of blocks organized in a Tree-Graph. In this way, all forked blocks contribute to the security and throughput of Conflux as well. In this work we discuss Conflux protocol design and implementation specifications.

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1. Introduction

Since the born of Bitcoin, various blockchain projects have demonstrated extraordinary success with the power of consensus among permissionless and trustless parties. The most successful blockchain project after Bitcoin is widely considered to be Ethereum, which generalizes the blockchain paradigm from a specialized value-transfer system to a more generalized Turing-complete state machine that allows conceptually all kinds of computation. This generalized state machine, known as *Ethereum Virtual Machine* (EVM), makes the Ethereum network essentially a decentralized computing platform where the state advances on input of transactions. Sometimes Ethereum is referred to as the “world computer” that nobody can shut down, except that its processing power is rather poor and severely bounded by the throughput of underlying consensus.

The consensus throughput of Bitcoin is (in expectation) one block per 10 minutes, with block size 1MB (or 2MB with Segregated Witness (segwit)). Bitcoin is set to small block size and low generation rate mainly for security concerns. Intuitively, when there is no adversary, the natural probability of forks is proportional to the ratio of block broadcasting time to block (generation) time, since under the longest chain rule honest mining power may keep working on a fork during the propagation of a newly mined block. Ethereum applies a tailored version of GHOST rule [1] and smaller block size to achieve a much shorter block time, i.e. roughly $< 100\text{KB}$ per 15 seconds. Inclusive Block Chain Protocol [2] is a “block-DAG” proposal which defines a total order of blocks in a directed acyclic graph (DAG) rather than a chain, with the major advantage over GHOST that all forked blocks contribute to the consensus throughput as well. Another line of scaling techniques trades security and decentralization for scalability by using sharding, sidechains, or other second layer extensions. In extreme cases, centralized and somehow permissioned consensus systems are implemented in practice.

Conflux is a project which aims at building a high throughput first layer consensus system without any compromises in security and decentralization; a generalized computation platform that securely processes at least thousands of transactions per second which makes the throughput of consensus is no more a bottleneck. The positioning of Conflux is a strong backbone consensus network on which a numerous number of unprecedented applications and extensions can germinate and thrive. Technically, we follow a similar idea as [2] but organize blocks in a Tree-Graph, which enables a fast implementation of the Conflux protocol.

2. Conventions

Throughout this document, we use the following conventional notations:

- \mathbb{B} denotes the set of bit values, i.e. $\mathbb{B} \equiv \{0, 1\}$. \mathbb{BY} denotes the set of byte values, i.e. $\mathbb{BY} \equiv \{0, \dots, 255\}$.
- \mathbb{N} denotes the set of non-negative integers.
- For every $n \in \mathbb{N}$, we use \mathbb{B}_n to denote a binary string of n bits, and \mathbb{BY}_n for a string of n bytes. In particular, $\mathbb{BY} = \mathbb{B}_8$.
 - Furthermore, we denote by \mathbb{B}^* and \mathbb{BY}^* the set of binary or byte strings of arbitrary length, i.e. $\mathbb{B}^* \equiv \cup_{i \in \mathbb{N}} \mathbb{B}_i$ and $\mathbb{BY}^* \equiv \cup_{i \in \mathbb{N}} \mathbb{BY}_i$.
 - For convenience, we let $\mathbb{N}_n \equiv \{0, 1, \dots, 2^n - 1\}$ be the set of non-negative integers smaller than 2^n .
 - The empty string is denoted by ε , which is distinguished from the empty set denoted by \emptyset .
- Numbers are in decimal base by default. Binary numbers are indicated with square brackets with subscripts, e.g. $[0100]_2$ is the 4-bit binary representation of 4. The subscript ch represents the character representation of bit string, e.g. $[\text{ab}]_{\text{ch}} = [6162]_{16} = [0110000101100010]_2$.
- When interpreting 256-bit binary values from \mathbb{N}_{256} as integers, the representation is big-endian.
- When a 256-bit machine datum in \mathbb{B}_{256} is converted to and from a 160-bit address or hash in \mathbb{B}_{160} , the rightwards (low-order for BE) 160 bits (20 bytes) are used and the leftmost 96 bits (12 bytes) are discarded or filled with zeros, thus the integer values (when the bytes are interpreted as big-endian) are equivalent.
- Tuples are typically denoted with bold upper case letters such as **A**. For frequently used tuples, we denote by **T** for a Conflux transaction, **B** for a Conflux block, and **H** for the header of a block.

- Subscripts can be added to refer to an individual component in the tuple, e.g. T_n denotes the nonce of the transaction T . The type of referred components is the same as the type of subscript, e.g. B_H denotes the header of a block B , where the header itself is another tuple of elements. For succinctness we also write $H(B) \equiv B_H$ and sometimes simply H when there is no ambiguity. Also for succinctness, we sometimes use B and H interchangeably if there is no ambiguity, e.g. B_d stands for the target difficulty of block B , which is formally denoted as $H(B)_d$ or B_{H_d} .
- In case we are considering many transactions or blocks, we add superscripts to refer to a specific one of them, e.g. T^1 denotes the first transaction in a sequence.
- The Tree-Graph structure of blocks is typically denoted by G , which is a graph consisting of blocks represented by vertices and parent/referee relations represented by two kinds of directed edges.
- Scalars and fixed-length sequences of elements (arrays, strings, and vectors) are denoted with normal lower case letters, e.g. n is used to denote a transaction nonce. Those with a special meaning may be denoted with Greek letters.
- Sequences of potentially arbitrary number of elements are typically denoted with bold lower case letters, e.g. \mathbf{o} is used to denote the byte sequence generated as the output data of a message call.
- The highly structured state values are typically denoted with bold lower case Greek letters, e.g. σ (and its variants) is used to denote the world-state, and μ for machine state.
- Square brackets are used to index subsequences of a sequence, with index starting from 0, e.g. $\mu_s[0]$ refers to the first item on the machine’s stack and $\mu_m[0 \dots 31]$ denotes the first 32 items of the machine’s memory.
 - The global state σ is interpreted as a sequence of accounts, where each account is a tuple. Thus the square bracket after σ refers to an individual (or a list of) accounts.
- Functions are typically denoted by upper case letters and subscripts are used for specialized variants, e.g. C is the general cost function and C_{STORE} is the cost function for the STORE operation. Specific functions operating on states are denoted by upper case calligraphic letters, e.g. \mathcal{C} denotes the Conflux global state transition function.
 - For every function F defined on D , we let F^* denote the function on range D^* that element-wise applies F on its input items, i.e. $F^*((x_1, x_2, \dots)) \equiv (F(x_1), F(x_2), \dots)$.
- The superscript of a function with parentheses like $f^{(i)}$ represents call function f for i times recursively. Formally, $f^{(1)}(\cdot) \equiv f(\cdot)$ and $f^{(i)}(\cdot) \equiv f^{(i-1)}(f(\cdot))$ for $i \geq 2$.

Frequently used functions:

- P : the *parent function* takes a block B as input and returns the parent block B' , i.e. B' is referenced in B and designated as the parent of B . Formally, $P(B) \equiv B' : \text{KEC}(\text{RLP}(B')) = H(B)_p$.¹
- CHAIN : the *chain function* takes a block B as input and returns the chain from genesis block to block B following only parent edges. Formally, for genesis block G , $\text{CHAIN}(G) \equiv G$; For other blocks B , $\text{CHAIN}(B) \equiv \text{CHAIN}(P(B)) \circ B$.
- SIBLING : the *sibling function* takes a block B as input and returns the blocks which have the same parent as B . Formally, $\text{SIBLING}(B) \equiv \{B' \mid P(B') = P(B) \wedge B' \neq B\}$.
- PAST : the *past function* takes a block B as input and outputs all blocks in the “past set of B ”, i.e. all blocks that are directly or indirectly referenced by B . The set $\text{PAST}(B)$ does not include B , since B cannot reference itself.
- FUTURE : the *future function* takes a Tree-Graph G and a block $B \in G$ as inputs and outputs all blocks in the “future set of B ”. Formally, $\text{FUTURE}(B; G) \equiv \{B' \in G \mid B \in \text{PAST}(B')\}$.
- EPOCH : the *epoch function* takes a block B as input and returns a sequence of all blocks in the epoch of B , sorted as in the Conflux total order defined in Section 4.2.4.
- BlockNo : the *block number function* takes a Tree-Graph G and a block B as inputs and returns the index of B in the total order of blocks specified by G , where the index starts from 0. In particular, for the genesis block G and for every Tree-Graph G there must be $\text{BlockNo}(G; G) = 0$. Note that $\text{BlockNo}(B; G)$ depends on G and it is different from $\text{PAST}(B)$ which is fully determined by B . For every G and $B \in G$ there must be $\text{BlockNo}(B; G) \geq \text{PAST}(B)$ since all blocks in $\text{PAST}(B)$ precede B in the total order. Furthermore, for $B, B' \in G$ and $B \neq B'$, there must be $\text{BlockNo}(B; G) \neq \text{BlockNo}(B'; G)$ because distinct blocks cannot have identical index in the total order. When the Tree-Graph G is clear from context, we may write $\text{BlockNo}(B)$ for succinctness.
- PIVOT : the *pivot function* takes a block B as input and outputs the pivot block in the epoch of B .
- S : the *sender function* takes a transaction T as input and returns the sender of T , where in particular the sender is represented by its address.
- RLP : this is the serialization function that encodes an input of arbitrary length into a structured binary data, i.e. a byte array explicitly containing information about the length of the input. For more details see Appendix B in [3].
- TRIE : the *trie function* maps an arbitrary-length binary byte array s into a 256-bit commitment that represents the database storing s in a modified Merkle Patricia tree (trie).

¹One may argue whether P is well-defined since KEC has collisions. However, as long as the collision cannot be found in practical situations, the function P only need to look up such a B' from existing blocks and returns \perp if there is none.

- **KEC**: the Keccak 256-bit cryptographic (collision-resistant) hash function that maps an arbitrary-length binary byte array to a random-looking binary string in \mathbb{B}_{256} . Furthermore, we assume KEC implements a *random oracle*, i.e. finding a random collision of KEC requires in expectation roughly 2^{128} attempts and a specific collision requires 2^{256} . Similarly, KEC512 refers to the 512-bit cryptographic hash function Keccak-512.
- **PoW**: this is the proof-of-work function, which takes a block header as input and returns a scalar in \mathbb{B}_{256} .
- **QUALITY**: this is a measurement of the proof-of-work quality of a given block, i.e. how unlikely it is to find such a block. It takes a block or a block header as input and outputs a scalar in \mathbb{N}_{256} . Essentially, a block \mathbf{B} with header $\mathbf{H} = \mathbf{H}(\mathbf{B})$ has quality $\text{QUALITY}(\mathbf{B}) \equiv \text{QUALITY}(\mathbf{H}) \equiv \lfloor 2^{256} / (\text{PoW}(\mathbf{H}) - [\mathbf{H}_n[1 \dots 127]]_2 \times 2^{128} + 1) \rfloor$ except for a few marginal cases. See Section 8.1 for more details.

2.1 Value

To incentivize the maintenance of the Conflux network and charge users for consumption of resources, Conflux has an intrinsic currency called Conflux Coin or simply Conflux, denoted by CFX for short. The smallest subdenomination is denoted by Drip, in which all values processed in Conflux are integers. One Conflux is defined as 10^{18} Drip. Frequently used subdenominations of Conflux are list as follows:

Multiplier (in Drip)	Name
10^0	Drip
10^9	GDrip
10^{18}	Conflux (CFX)

3. Basic Components

In an overview, the Conflux world-state consists of a list of accounts and the associated account states, and the global state is updated via transactions. The Conflux blockchain stores all processed transactions in blocks, together with necessary information in block headers which enables a total ordering of all blocks. In this section we discuss the meaning of accounts, transactions and blocks in more details.

3.1 Accounts

The Conflux global state is described in an account model, with the basic storage component called an *account*. Every actor, which is either a person or an entity that is able to interact with the Conflux world, has its necessary information stored in an account α as a key/value pair $(\alpha_{addr}, \alpha_{state})$ of address and state. The account address α_{addr} is a 160-bit identifier, and the account state α_{state} is a serialized sequence in an RLP structure (c.f. [3]). Furthermore we note that each account α is associated with a pair of public key and private key $(\alpha_{pubkey}, \alpha_{prikey})$. The account address is the concatenation of 4-bit type indicator and a 156-bit digest of the associated public key:

$$\alpha_{addr} \equiv \text{Type}_\alpha \circ \text{KEC}(\alpha_{pubkey}) [100 \dots 255] \tag{1}$$

where $\text{Type}_\alpha \in \mathbb{B}_4$ is the type indicator, which is $\text{Type}_\alpha = [0001]_2$ for *normal accounts* (a.k.a. *non-contract accounts*), $\text{Type}_\alpha = [1000]_2$ for *(Solidity) contracts*, and $\text{Type}_\alpha = [0000]_2$ for *built-in/reserved contracts* (a.k.a. *precompiled contracts*).

For succinctness and convenience, and as long as there is no ambiguity, we will write α without subscript for the state of an account and let $a \equiv \alpha_{addr}$ denote the corresponding address.

An account state $\alpha_{state} \equiv (\alpha_n, \alpha_b, \alpha_c, \alpha_t, \alpha_o, \alpha_r, \alpha_d, \alpha_v, \alpha_a, \alpha_p, \alpha_w, \alpha_s)$ consists of the following fields:

- **nonce**: A scalar counter recording the number of previous activities initiated by this account. Formally denoted by $\alpha_n \in \mathbb{N}_{256}$. For example, the number of transactions sent from α_{addr} , or the number of contract-creations in the case this account is associated with codes.
- **balance**: A scalar value equal to the number of Drip owned by this account. Formally denoted by $\alpha_b \in \mathbb{N}_{256}$.
- **codeHash**: The hash of the EVM code that gets executed when α_{addr} receives a message call. Unlike other fields, it is immutable once established. All such code fragments are stored in a state database for later retrieval. This hash is formally denoted by $\alpha_c \in \mathbb{B}_{256}$, which satisfies $\alpha_c = \text{KEC}(\mathbf{p})$ when the stored code is \mathbf{p} . In particular $\alpha_c = \text{KEC}(\epsilon)$ is the hash of the empty string when α is a normal account.
- **stakingBalance**: A scalar value equal to the number of staked Drip. Formally denoted by $\alpha_t \in \mathbb{N}_{256}$. (See section 7.3 for details)
- **storageCollateral**: A scalar value equal to the number of Drip used as collateral for storage, which will be returned to balance if the corresponding storage is released. Formally denoted by $\alpha_o \in \mathbb{N}_{256}$. (See section 6 for details)

- **accumulatedInterestReturn:** A scalar value equal to the number of Drip in accumulated interest return. Formally denoted by $\alpha_r \in \mathbb{N}_{256}$. (See section 7.3 for details)
- **depositList:** A series of deposit information. Formally denoted by $\alpha_d \in (\mathbb{N}_{256} \times \mathbb{N}_{512} \times \mathbb{N}_{256})^*$. (See section 7.3 for details)
- **stakingVoteList:** A series of vote information. Formally denoted by $\alpha_v \in (\mathbb{N}_{256} \times \mathbb{N}_{512})^*$. (See section 7.3 for details)
- **admin:** The address of the administrator if α is a contract. Formally denoted by $\alpha_a \in \mathbb{B}_{160}$. (See section 7.2 for details)
- **sponsorInfo:** The sponsor information if α is a contract. It contains five components: **sponsor for gas, sponsor for collateral, sponsor balance for gas, sponsor gas limit, sponsor balance for gas and sponsor collateral for gas**. Formally denoted by $\alpha_p \in (\mathbb{B}_{160})^2 \times (\mathbb{N}_{256})^3$. (See section 7.1 for details). We use $\alpha_p[\text{gas}]_a$, $\alpha_p[\text{col}]_a$, $\alpha_p[\text{limit}]_a$, $\alpha_p[\text{gas}]_b$ and $\alpha_p[\text{col}]_b$ to reference these five components.
- **codeOwner:** The address of the payer who provides the collateral for storing the code if α is a contract. Formally denoted by $\alpha_w \in \mathbb{B}_{160}$.
- **storage:** A key/value database representing the account's storage state, if α is a contract account. Every entry is represented as $(k, v, o) \in \mathbb{B}_{256} \times \mathbb{N}_{256} \times \mathbb{B}_{160}$, where k and v denote the key and value of this entry and o denotes the owner who provides storage collateral for this entry. Formally denoted by $\alpha_s \in (\mathbb{B}_{256} \times \mathbb{N}_{256} \times \mathbb{B}_{160})^*$.

Given the Conflux world-state σ and an address $a \in \mathbb{B}_{160}$, we denote by $\sigma[a]$ for the state α_{state} of the account α with address $a = \alpha_{addr}$, i.e. $\sigma[a] \equiv \alpha_{state}$. We denote by $\sigma[a] \equiv \emptyset$ if the account with address a is never initialized. When $\sigma[a] \neq \perp$, we use $\sigma[a]_s[k]_v$ and $\sigma[a]_s[k]_o$ to denote the storage value and storage owner of storage entry with key k in $\sigma[a]_s$. We denote by $\sigma[a]_s[k]_o = \emptyset$ and $\sigma[a]_s[k]_v = \emptyset$ in case key k doesn't exist in $\sigma[a]_s$,

A default account will be initialized as

$$\alpha^0 \equiv (0, 0, 0, 0, 0, 0, \varepsilon, \varepsilon, 0, (0, 0, 0, 0, 0)) \quad (2)$$

3.2 Hash Digest of World-State

3.2.1 State entry

Conflux organizes the account information into a set of key/value pairs with four different types and encodes them in format of $(k, v) \in \mathbb{B}^* \times \mathbb{B}^*$ respectively.

Account entry. The account entry stores all the components $(\alpha_n, \alpha_b, \alpha_c, \alpha_t, \alpha_o, \alpha_r, \alpha_d, \alpha_v, \alpha_a, \alpha_p)$ except **storage** α_s and **codeOwner** α_w in account state α_{state} . In this case, we have

$$k \equiv \alpha_{addr} \quad (3)$$

$$v \equiv \text{RLP}(\alpha_n, \alpha_b, \alpha_c, \alpha_t, \alpha_o, \alpha_r, \alpha_d, \alpha_v, \alpha_a, \alpha_p) \quad (4)$$

Storage entry. The storage entry stores all the storages in α_s . Given account α with address α_{addr} , for each storage key $s \in \mathbb{B}_{256}$ with $\alpha_s[s]_v \neq 0$, we have

$$k \equiv \alpha_{addr} \cdot [\text{data}]_{\text{ch}} \cdot s \quad (5)$$

$$v \equiv \text{RLP}(\alpha_s[s]_v, \alpha_s[s]_o) \quad (6)$$

Storage root entry. The storage root entry stores the storage layout for account α .

$$k \equiv \alpha_{addr} \cdot [\text{data}]_{\text{ch}} \quad (7)$$

$$v \equiv 0 \quad (8)$$

Code entry. The code entry stores the **code p** $\in \mathbb{B}^*$ for account α , with **codeHash** denoted by $\alpha_c = \text{KEC}(\mathbf{p})$.

$$k \equiv \alpha_{addr} \cdot [\text{code}]_{\text{ch}} \cdot \alpha_c \quad (9)$$

$$v \equiv \text{RLP}(\mathbf{p}, \alpha_w) \quad (10)$$

3.2.2 Multi-version Merkle Patricia Trie

Ethereum collects all the key/value pairs into MPT (Merkle Patricia Trie) and updates it during execution of transactions. However, in a high throughput blockchain system, the MPT may be accessed in a high frequency and hence become a bottleneck of performance. Conflux maintains a **read-through write-back** cache and commits cached changes to MPT periodically.

Formally, at any time, Conflux maintains three key/value sets T_0, T_1, T_2 , which are called **snapshot**, **intermediate set** and **delta set** respectively. The later one is the cache of the former one. T_2 is the only one updated during transaction execution. In

order to balance the keys in MPT **delta set** and achieve a high performance, T_2 has a different way in computing keys. Let

$$p \equiv \text{KEC}(\text{TRIE}(T_0), \text{TRIE}(T_1)) \quad (11)$$

$$f_{addr}(\alpha_{addr}, p) \equiv \text{KEC}(p[0..11] \cdot \alpha_{addr})[0..11] \cdot \alpha_{addr} \quad (12)$$

$$f_{store}(s, p) \equiv \text{KEC}(p \cdot s)[4..31] \cdot s \quad (13)$$

(The index here are applied on byte-level.) the key is defined as (the symbols are inherited from the previous section)

- **Account entry.** $k \equiv f_{addr}(\alpha_{addr}, p)$
- **Storage entry.** $k \equiv f_{addr}(\alpha_{addr}, p) \cdot [\text{data}]_{\text{ch}} \cdot f_{store}(s, p)$
- **Storage root entry.** $k \equiv f_{addr}(\alpha_{addr}, p) \cdot [\text{data}]_{\text{ch}}$
- **Code entry.** $k \equiv f_{addr}(\alpha_{addr}, p) \cdot [\text{code}]_{\text{ch}} \cdot \alpha_c$

Delta set. During transaction execution, each time an account or storage entry is added, updated or removed, it will be marked dirty and its newest content will be added to the delta set when the transaction execution succeed. Specially, if the storage entries α_s of an account α are updated, account entry and storage root entry for α will also be marked dirty and added to delta set even if their contents are not changed. The code owner α_w is immutable once contract α has been created. Once an entry is marked dirty, the dirty mark will not be removed unless the execution reverted or failed.

In case of removing account, storage or code from the world-state, an empty account α^0 , empty storage entry $(0, 0)$ or empty code $(\varepsilon, 0)$ for corresponding entry will be added to the delta set representing deletion operation.

At the time ???, Conflux will merge intermediate set T_1 to snapshot T_0 , move delta set to intermediate set and reset delta set as empty.

$$T'_0 \equiv \text{MPTMerge}(T_0, T_1) \quad (14)$$

$$T'_1 \equiv T_2 \quad (15)$$

$$T'_2 \equiv \emptyset \quad (16)$$

where MPTMerge is the function updates the entries in T_0 which have new version in T_1 . Specially, for the entries with empty content (an empty account α^0 , empty storage entry $(0, 0)$ or empty code $(\varepsilon, 0)$), T_0 removes them.

3.2.3 State root

Let $\text{TRIE}(T_0^{(i)})$, $\text{TRIE}(T_1^{(i)})$, $\text{TRIE}(T_2^{(i)})$ be the roots of MPT after execution transaction of epoch i , then the state root of epoch i should be

$$\text{StateRoot}^{(i)} \equiv \text{KEC}(\text{RLP}(\text{TRIE}(T_0^{(i)}), \text{TRIE}(T_1^{(i)}), \text{TRIE}(T_2^{(i)}))).$$

Notice that Conflux doesn't insert $\text{StateRoot}^{(i)}$ to the header of pivot block in epoch i , see the following for details.

3.3 Transactions

A Conflux transaction T is a single instruction composed by an external actor with a Conflux account α , and this instruction is cryptographically signed under the associated private key α_{prikey} of the sending account α . The authentication key, i.e. the sending account's associated public key α_{pubkey} , is also included in the transaction for verification.

There are two types of transactions depending on the "destinations":

1. to an account address: these are normal transactions that may transfer value and/or result in message calls, known as *action transactions*;
2. to "nowhere": these transactions are used to create new contracts, known as *contract creation transactions* or simply *creation transactions*.

Both types of transactions share the following common fields:

- **nonce:** A scalar value equal to the number of previously sent transactions. Formally denoted by $T_n \in \mathbb{N}_{256}$.
- **gasPrice:** A scalar value indicating the number of Drip to be paid per unit of gas that is consumed as a result of the execution of T . Formally denoted by $T_p \in \mathbb{N}_{256}$.
- **gasLimit:** A scalar value indicating the *total* amount of gas paid for the cost of the execution of T . This is paid up-front, before any actual computation is done, and may not be increased or refunded later. Formally denoted by $T_g \in \mathbb{N}_{256}$. It is the transaction sender's responsibility to avoid any extravagance caused by an unnecessarily high **gasLimit**.
- **action:** A variable size field indicating the action of this transaction, formally denoted by T_a . There is a sub-field **create** indicating whether T is a contract creation transaction, which we make it implicit for notation convenience. Thus, for action transactions T_a indicates the 160-bit address of the recipient, which refers to either a normal account or a contract account; otherwise in case of a creation transaction, the recipient is indeed the newly created contract and we interpret T_a as the only element in \mathbb{B}_0 and write $T_a = \emptyset$.

- **value:** A scalar value equal to the amount of Drip that the transactions sender wants to transfer to the recipient, i.e. the account specified in T_a or the newly created contract. Formally denoted by $T_v \in \mathbb{N}_{256}$.
- **storageLimit:** A scalar value indicating the maximum increment of storage used in the execution of T , measured in bytes. Formally denoted by $T_\ell \in \mathbb{N}_{64}$.
- **epochHeight:** A scalar value specifying the range of epochs where T can be executed. Formally denoted by $T_e \in \mathbb{N}_{64}$ such that T can only be executed between the epochs of $[T_e - 100000, T_e + 100000]$.
- **chainID:** A binary chain id indicating where T is intended to be executed. Formally denoted by $T_c \in \mathbb{B}_{64}$ and the chain id of Conflux is a constant $T_c = 503$.
- **v, r, s:** Corresponding fields of the recoverable ECDSA signature of T , formally denoted by T_w, T_r and T_s .

In addition to the shared fields, a transaction may contain either of the following fields of unlimited length byte arrays for contract creation and invocation:

- **init:** A byte array specifying the EVM code for the initialization procedure, formally denoted by $T_i \in \mathbb{B}Y^*$. Note that **init** is executed once and discarded thereafter, and it returns another code fragment **body** as the actual contract code that will be executed each time the contract account receives a message call (either through a transaction or due to the internal execution of code).
- **data:** A byte array specifying the input data of the message call to an existing contract, formally denoted by $T_d \in \mathbb{B}Y^*$.

There is a function $S(\cdot)$ that maps a transaction to its sender using the recoverable ECDSA signature, i.e. $S(T)$ henceforth represents the sender of the transaction T . For convenience, we further introduce the function L_T that parses a transaction T as follows:

$$L_T(T) \equiv \begin{cases} (T_n, T_p, T_g, T_a, T_v, T_\ell, T_e, T_c, T_i, T_w, T_r, T_s) & \text{if } T_a = \emptyset \\ (T_n, T_p, T_g, T_a, T_v, T_\ell, T_e, T_c, T_d, T_w, T_r, T_s) & \text{otherwise} \end{cases} \quad (17)$$

3.4 Blocks

The Conflux blockchain organizes all on-chain information in blocks. Every Conflux block B consists of two parts: a block header H and a list of transactions Ts . The header H contains a list of other unreferenced block headers (a.k.a. *referee* blocks or simply *referees*).

The block header H is a collection of relevant pieces of information:

- **parentHash:** The Keccak 256-bit hash of the parent block's header, formally denoted by $H_p \in \mathbb{B}_{256}$.
- **height:** A scalar value equal to the height of the block, which is also the number of parent references to reach the genesis block. This is formally denoted by $H_h \in \mathbb{N}_{64}$. The genesis block has a height of zero.
- **timestamp:** A scalar value equal to the reasonable output of Unix's `time()` at this block's inception. Formally denoted by $H_s \in \mathbb{N}_{64}$.
- **author:** The 160-bit address of the author of this block, formally denoted by $H_a \in \mathbb{B}_{160}$. This is indeed the beneficiary's address to receive all rewards caused by successfully mining this block.
- **transactionRoot:** The Keccak 256-bit hash of the root node of the trie structure populated with each transaction in the transaction list portion of the block, formally $H_t \in \mathbb{B}_{256}$.
- **deferredStateRoot:** The Keccak 256-bit hash commitment of the state after all "stable transactions" are executed and finalized, formally $H_r \in \mathbb{B}_{256}$. Note that due to *deferred execution* in Conflux, "stable transactions" are those included in the past blocks of the pivot block of 5 epochs ago, i.e. 5 steps along the parent references.
 - If the **blame** field is zero, i.e. $H_m = 0$, then H_r is the root node of the state trie after all "stable transactions" are executed and finalized.
 - Otherwise if $H_m > 0$, then H_r will be the Keccak 256-bit hash of the vector consisting of the state root in the previous case and the corrected state roots of B 's ancestors until (not including) the first ancestor that is not blamed.
- **deferredReceiptsRoot:** The Keccak 256-bit hash commitment of the receipts of each transaction executed when updating the **deferredStateRoot** field of the block, formally $H_e \in \mathbb{B}_{256}$.
 - If the **blame** field is nonzero, i.e. $H_m = 0$, then H_e is the Keccak 256-bit hash of the root node of the trie structure populated with the receipts of transactions in the epoch that is just executed.
 - Otherwise if $H_m > 0$, then H_e will be the Keccak 256-bit hash of the vector consisting of the receipt root in the previous case and the corrected receipt roots of B 's ancestors until (not including) the first ancestor that is not blamed.
- **deferredLogsBloomHash:** The Keccak 256-bit hash commitment of the Bloom filter composed from indexable information (logger address and log topics) contained in each log entry from the receipts of all transactions executed when updating the **deferredStateRoot** field, formally $H_b \in \mathbb{B}_{256}$.

- If the **blame** field is zero, i.e. $H_m = 0$, then H_b is the Keccak 256-bit hash commitment of the Bloom filter composed from receipts of transactions in the epoch that is just executed.
 - Otherwise if $H_m > 0$, then H_b will be the Keccak 256-bit hash of the vector consisting of the Bloom filter commitment in the previous case and the corrected Bloom filter commitments of B 's ancestors until (not including) the first ancestor that is not blamed.
- **blame**: A scalar value $H_m \in \mathbb{N}_{32}$ indicating the number of immediate ancestors whose header is incorrect in the execution state fields: **deferredStateRoot**, **deferredReceiptsRoot**, **deferredLogsBloomHash**, or **blame**. This **blame** field is relevant in reward distribution.
For example, if $P(B)$ is correct on all the four fields then $H_m = 0$; if any of these fields is wrong in $P(B)$, then $H_m \geq 1$.
 - **difficulty**: A scalar value $H_d \in \mathbb{N}_{256}$ specifying the target difficulty level of this block. This is calculated from the previous block's difficulty level and the timestamp.
 - **adaptiveWeight**: The Boolean value $H_w \in \mathbb{B}$ indicating whether adaptive weight is triggered.
 - **gasLimit**: A scalar value $H_\ell \in \mathbb{N}_{256}$ equal to the current limit of gas expenditure per block. Starting from $H_\ell(G) \equiv 3 \times 10^7 = 30000000$.
 - **refereeHash**: The serialized RLP sequence of the referee list consisting of Keccak 256-bit hashes of referee blocks, formally denoted by $H_o \in \mathbb{B}\mathbb{Y}^*$. This list consists of up to 100 hash references of referee blocks. For convenience, we let $U(B)$ denote these referee blocks of a block B .
 - **mixHash**: A 256-bit hash which, combined with the **nonce**, proves that a sufficient amount of computation has been carried out on this block; formally $H_x \in \mathbb{B}_{256}$.
 - **nonce**: A 256-bit value which proves that a sufficient amount of computation has been carried out on this block, formally $H_n \in \mathbb{B}_{256}$.

The other part of B is simply a list of transactions. Therefore the block B can be represented as follows:

$$B \equiv (B_H, B_{Ts}) \quad (18)$$

3.4.1 Transaction Receipt

For convenience and easy verification of the outcome of transaction execution, we introduce *transaction receipt* to record certain information of every executed transaction. When updating the **deferredStateRoot** H_r of a block, we encode a receipt $B_R[i]$ for the i -th executed transaction and store these receipts in an index-keyed trie. This root is recorded in the header as $H_e \in \mathbb{B}_{256}$.

For every executed transaction T , the receipt $R \equiv (R_u, R_b, R_l, R_z, R_o, R_i)$ is a tuple consisting of six fields:

- $R_u \in \mathbb{N}$ is the cumulative gas used *in the epoch where T is executed* as of immediately after T has been processed;
- R_l is the set of logs created in the execution of T ;
- $R_b \in \mathbb{B}_{2048}$ is the Bloom filter composed from logs in R_l ;
- $R_z \in \mathbb{N}$ is the status code of the transaction T .
- R_o is the set of incremental storage (in bytes) for addresses in the execution of T ;
- R_i is the set of decremental storage (in bytes) for addresses in the execution of T ;

The sequence $R_l \equiv (O_0, O_1, \dots) \in (\mathbb{B}_{160} \times (\mathbb{B}_{256})^* \times \mathbb{B}_*)^*$ is a series of log entries, where each log entry O is a tuple of the logger's address $O_a \in \mathbb{B}_{160}$, a possibly empty series of 256-bit log topics $O_t \equiv (O_{t_0}, O_{t_1}, \dots)$, such that $O_{t_i} \in \mathbb{B}_{256}$ for every $i \in \mathbb{N}$, and a sequence of data $O_d \in \mathbb{B}_*$:

$$O \equiv (O_a, O_t, O_d) \quad (19)$$

The Bloom filter function M reduces a log entry into a single 256-byte (2048-bit) hash as follows:

$$M(O) \equiv \bigvee_{x \in \{O_a\} \cup O_t} (M_{3:2048}(x)) \quad (20)$$

where $M_{3:2048}$ is the specialized Bloom filter that sets three out of 2048 bits to 1 on input of an arbitrary byte sequence, as formally defined in [3].

The sequence $R_o \equiv (P_0, P_1, \dots) \in (\mathbb{B}_{160} \times \mathbb{B}_{256})^*$ where each entry P is a tuple of an address and the incremental storage collateral of such address. R_o only collects the addresses with positive incremental storage collateral. It is sorted in ascending order of addresses and each address only appears once. R_i has the same settings as R_o .

3.4.2 Serialization

The function L_B and L_H are the preparation functions for a block and block header respectively (similar as L_T defined in eq. (17)), where we recall that L_T^* and L_H^* refer to element-wise sequence transformations. We assert the types and order of the structure when the RLP transformation is required:

$$L_H(\mathbf{H}) \equiv (\mathbf{H}_p, \mathbf{H}_h, \mathbf{H}_s, \mathbf{H}_a, \mathbf{H}_t, \mathbf{H}_r, \mathbf{H}_e, \mathbf{H}_b, \mathbf{H}_m, \mathbf{H}_d, \mathbf{H}_w, \mathbf{H}_\ell, \mathbf{H}_o, \mathbf{H}_x, \mathbf{H}_n) \quad (21)$$

$$L_B(\mathbf{B}) \equiv (L_H(\mathbf{B}_H), L_T^*(\mathbf{B}_{Ts})) \quad (22)$$

In addition, we let L_O be the preparation function for the referee blocks as follows:

$$L_O(\mathbf{H}) \equiv L_H^*(\mathbf{H}_o)$$

The component types are defined thus:

$$\begin{aligned} & \mathbf{H}_p \in \mathbb{B}_{256} & \wedge & \mathbf{H}_h \in \mathbb{N}_{64} & \wedge & \mathbf{H}_s \in \mathbb{N}_{64} & \wedge & \mathbf{H}_a \in \mathbb{B}_{160} & \wedge & \mathbf{H}_t \in \mathbb{B}_{256} \\ \wedge & \mathbf{H}_r \in \mathbb{B}_{256} & \wedge & \mathbf{H}_e \in \mathbb{B}_{256} & \wedge & \mathbf{H}_b \in \mathbb{B}_{256} & \wedge & \mathbf{H}_m \in \mathbb{N}_{32} & \wedge & \mathbf{H}_d \in \mathbb{N}_{256} \\ \wedge & \mathbf{H}_w \in \mathbb{B} & \wedge & \mathbf{H}_\ell \in \mathbb{N}_{256} & \wedge & \mathbf{H}_o \in (\mathbb{B}_{256})^{\leq 100} & \wedge & \mathbf{H}_x \in \mathbb{B}_{256} & \wedge & \mathbf{H}_n \in \mathbb{B}_{256} \end{aligned} \quad (23)$$

Now we have the specification for the construction of a formal block structure. With the RLP transformation we can further serialize this structure into a sequence of bytes ready for transmission and storage.

3.4.3 Well-formedness

Every Conflux block \mathbf{B} (with header $\mathbf{H} = \mathbf{H}(\mathbf{B})$) is *well-formed* if and only if it is internally consistent and satisfies the following:

$$\mathbf{H}_r = \text{TRIE}(\forall i < \|\mathbf{B}_{Ts}\|, i \in \mathbb{N} : (\text{RLP}(i), \text{RLP}(L_T(\mathbf{B}_{Ts}[i])))) \quad (24)$$

Intuitively, a block \mathbf{B} is well-formed if its header \mathbf{H} is consistent with the contents inside \mathbf{B} . In other words, \mathbf{H} effectively represents the whole block \mathbf{B} .

3.4.4 Block Header Validity

Given a block \mathbf{B} with header $\mathbf{H} = \mathbf{H}(\mathbf{B})$, we decide whether the header \mathbf{H} is valid by checking the following fields of \mathbf{H} and comparing to $\mathbf{H}(\mathbf{P}(\mathbf{B}))$ and $\text{PAST}(\mathbf{B})$ when necessary:

- the height is increased by one;
- the timestamp (in Unix's `time()`) is increased;
- the canonical gas limit does not change too much (i.e. more than $1/1024$) and it remains above 5000;
- the target difficulty is properly set according to Section 8.2;
- the proof-of-work quality exceeds the target difficulty;
- the parent is chosen properly from $\text{PAST}(\mathbf{B})$ (the past view of \mathbf{B}) following the GHASt rule;
- the adaptive weight flag **adaptiveWeight** must set properly according to the GHASt rule with respect to $\text{PAST}(\mathbf{B})$;
- the referee list **refereeHash** properly decomposes to block headers.

Formally, the header \mathbf{H} is valid if and only if:

$$\mathbf{H}_h = \mathbf{H}(\mathbf{P}(\mathbf{B}))_h + 1 \quad (25)$$

$$\wedge \mathbf{H}_s > \mathbf{H}(\mathbf{P}(\mathbf{B}))_s \quad (26)$$

$$\wedge \mathbf{H}_l < \left(1 + \frac{1}{1024}\right) \mathbf{H}(\mathbf{P}(\mathbf{B}))_l \quad \wedge \quad \mathbf{H}_l > \left(1 - \frac{1}{1024}\right) \mathbf{H}(\mathbf{P}(\mathbf{B}))_l \quad \wedge \quad \mathbf{H}_l \geq 5000 \quad (27)$$

$$\wedge \mathbf{H}_d \text{ is legitimate according to the difficulty adjusting function} \quad (28)$$

$$\wedge \mathbf{H}_x \text{ is the correct mix-hash (see (170) in Section 8)} \quad (29)$$

$$\wedge \text{QUALITY}(\mathbf{H}) \geq \mathbf{H}_d \quad (30)$$

$$\wedge \mathbf{P}(\mathbf{B}) \text{ specified by } \mathbf{H}_p \text{ is legitimate according to GHASt rule in } \text{PAST}(\mathbf{B}) \quad (31)$$

$$\wedge \mathbf{H}_w \text{ is legitimate according to the GHASt rule in } \text{PAST}(\mathbf{B}) \quad (32)$$

$$\wedge \mathbf{H}_o \text{ is well-formed and encodes referee block headers} \quad (33)$$

We remark that the validity of H only matters for consensus of total order of blocks, and it *does not* rely on the correctness of the execution related fields **deferredStateRoot**, **deferredReceiptsRoot**, **deferredLogsBloomHash** and **blame** of the header, i.e. H_r, H_e, H_b and H_m of H respectively. However, being incorrect in these fields may indicate that the author of the block fails to maintain the state and execute the transactions properly, in which case we still count the contribution of this block to consensus but the author gets no reward, as discussed in Section 3.4.6 and Section 9.

3.4.5 Partially (In)Valid Blocks

We call a block B *partially valid* if either $P(B)$ is marked as partially valid or its header $H = H(B)$ passes all the assertions as in Section 3.4.4 except for the following:

- the parent reference $P(B)$ specified by $H(B)_p$ is not chosen properly according to the GHAST rule in $PAST(B)$;
- the adaptive weight flag $H(B)_w$ is not set properly according to the GHAST rule in $PAST(B)$;
- the target difficulty $H(B)_d$ satisfies the threshold condition of difficulty adjustment but it is not calculated properly according to the GHAST difficulty adjusting function.

A partially valid block may not be referenced by honest blocks in several hours after it is released. When a block becomes old and loses the ability to influence the pivot chain, we do not care about whether a block is partially valid or not. See Section 4.1 for details. Once a partially valid block is accepted, then it is treated as a fully valid block except for the decision of timer chain (Section 4.2.1).

We note that as long as the target difficulty is legitimate and the proof of work is valid, the partially valid block can still contribute to the throughput. This is because we allow referencing partially valid blocks and the transactions inside will be processed as in any fully valid block. We further remark that since the producer of a partially valid block is entitled to no reward, transaction fees may be burnt in case these transactions are only collected in partially valid blocks.

3.4.6 Blaming Mechanism

The **blame** field is introduced for easy verification of states by light nodes. Intuitively, this field represents the vote to the latest ancestor block which commits to a correct state, i.e. the author of the current block agrees with the committed state (represented in **deferredStateRoot**, **deferredReceiptsRoot**, **deferredLogsBloomHash**, and **blame**) of that block. We emphasize that these fields are *not* checked for validity of a block, however, committing to an incorrect state may lead to loss of block reward.

More specifically, $H(B)_m$ should be set to the minimum non-negative number such that $P^{(H(B)_m+1)}(B)$ is correct on all the four fields of **deferredStateRoot**, **deferredReceiptsRoot**, **deferredLogsBloomHash**, and **blame**. For example, $H(B)_m$ should be 1 if $P(B)$ is incorrect in $H(P(B))_r, H(P(B))_e, H(P(B))_b$ or $H(P(B))_m$ while $P^{(2)}(B)$ is correct in these fields.

Then, in the current block B 's view, all blocks in between of B and $P^{(H(B)_m+1)}(B)$, i.e. $P(B), \dots, P^{(H(B)_m)}(B)$, are committing to incorrect states, for which we say that those blocks are (directly) *blamed* by B . Furthermore, since B agrees with the state committed in $P^{(H(B)_m+1)}(B)$, the blocks blamed by $P^{(H(B)_m+1)}(B)$ is also (indirectly) blamed by B , and recursively we can determine all the blocks on $CHAIN(B)$ that are blamed by the newest block B .

For blocks off $CHAIN(B)$ (which is indeed the pivot chain in $PAST(B)$ as long as B is valid), we do a best effort test to decide whether they are blamed by B . More precisely, every block B' must have determined a set of blocks blamed by B' along $CHAIN(B')$, and B' is blamed by B if they do not agree on exactly the same set of blamed blocks in the intersection $CHAIN(B) \cap CHAIN(B')$. We remark that no further check is applied on the execution related fields B'_r, B'_e, B'_b of B' as long as B' is off the current pivot chain.

Thus we have determined for every block B' whether it is blamed by any other block B . The punishment for blamed blocks (in particular, those blamed by the latest block on the pivot chain) is specified in Section 9.

In addition, the fields of state commitments, i.e. **deferredStateRoot**, **deferredReceiptsRoot**, **deferredLogsBloomHash**, would be handled differently when being blamed, as briefly described at the beginning of Section 3.4. That is, if $H_m > 0$ and the those fields are blamed, then the commitment will be a Keccak hash of the vector consisting of the correct commitments. For example, if a block B has $H(B)_m = 2$ such that $P(B), P^{(2)}(B)$ are blamed but $P^{(3)}(B)$ is not, then the **deferredStateRoot** field $H(B)_r$ of block B would be

$$H(B)_r = \text{KEC} \left(\text{CorrectDeferredStateRoot}(B), \text{CorrectDeferredStateRoot}(P(B)), \text{CorrectDeferredStateRoot}(P^{(2)}(B)) \right) \quad (34)$$

where $\text{CorrectDeferredStateRoot}(\cdot)$ is the function that returns the correct value of the deferred state root, which is a 256-bit Keccak hash, that should be filled in the given block. Note that 1) RLP serialization is not used in the vector since each element has fixed length, and 2) the vector length only depends on the **blame** field, regardless of correctness of individual fields in blamed blocks. Similar rules apply to **deferredReceiptsRoot** and **deferredLogsBloomHash**, i.e. $H(B)_e$ and $H(B)_b$.

4. Consensus

The consensus rules in Conflux are designed to make decision on two questions: the first is that whether a block is valid and should be added to the Conflux blockchain; the other is that in what order those valid blocks should be processed.

In an overview, the Conflux consensus protocol optimistically accepts all formally correct blocks and organizes them as a Tree-Graph (instead of a tree or a chain), and then specifies a total order of blocks in the Tree-Graph following the GHAST rule. This total order will be agreed by all honest participants and it is hard to change (under reasonable assumptions). After fixing such an order, transactions inside blocks are executed accordingly, and invalid transactions, which can be duplicating or conflicting previously processed transactions, are ignored.

4.1 Validation of Blocks

A set of Conflux blocks form a Tree-Graph structure where each vertex in the Tree-Graph represents a Conflux block and each directed edge in the Tree-Graph corresponds to a parent or referee reference. Every full node maintains a Tree-Graph structure of accepted blocks, which are blocks that are valid in the node's local view. Whenever receiving a new block, the full node verifies whether the block is valid before adding it into the Tree-Graph.

The validation of a new block can result in four outcomes:

- **suspending:** the block B is partially valid and $\text{TimerDis}(B; G) < 240$. ($\text{TimerDis}(\cdot)$ is defined later in eq. (36) and G denotes the current Tree-Graph.) The status of block B will be checked again each time a new valid (or partially valid) block appears in the future set of B .
- **accept:** the block is valid (either fully valid or partially valid but not **suspending** anymore) and will be added to the Tree-Graph immediately.
- **reject:** the block is clearly invalid and will be discarded.
- **pending:** the block references some blocks not in the current Tree-Graph. Such blocks will be checked again once all the referenced blocks have been added to the Tree-Graph.

Given a new block B that is no longer **suspending**, the validation of B is done in the following steps:

1. **Header Validation.** This step asserts that B has a valid header (or at least a partially valid one) following Section 3.4.4 and 3.4.5. Note that a **Proof-of-Work Validation** of B is embedded inside the **Header Validation**, where the solution to the PoW puzzle is verified w.r.t. the legitimate target difficulty $H(B)_d$. The canonical gas limit $H(B)_\ell$ is also checked here, i.e. $H(B)_\ell \in (1 \pm \frac{1}{1024}) \times H(P(B))_\ell$ and $H(B)_\ell \geq 5000$ as in (27).

The **Proof-of-Work Validation** is the major mechanism against Sybil attacks and should be performed before invoking more expensive steps of verification and execution. It is interchangeable with other steps of the validation for better efficiency; and it will be performed last and repeatedly when mining a new block.

2. **Referee Validation.** The validation of referee headers asserts that B only references existing valid blocks. In case the new block references the head of an unknown block, it is marked as **pending** until all its referee blocks have been added to the Tree-Graph. The node is suggested (but not forced) to query its neighbors about the referenced unknown block.
3. **Volume Validtion.** The size of block body must not exceed 200 KB. Formally, $\sum_{T \in B_{T_s}} |\text{RLP}(T)| \leq 204800$.
4. **Internal Consistency.** This step asserts that B is self-consistent. More specifically:
 - the block header B_H is formally consistent with content in B_{T_s} , i.e. B_H is well-formed following Section 3.4.3;
 - every transaction $T \in B_{T_s}$ is *locally legitimate*, which is the first test of the intrinsic validity of transactions:
 - (a) T is well-formed RLP with no trailing bytes;
 - (b) T has a valid signature by its sender $S(T)$;
 - (c) T has correct chain id $T_c = 503$;
 - (d) the **gasLimit** T_g is no smaller than the intrinsic gas g_0 , where

$$\begin{aligned}
 g_0 \equiv & \sum_{i \in T_i, T_d} \begin{cases} G_{\text{txdatazero}} & \text{if } i = 0 \\ G_{\text{txdatanonzero}} & \text{otherwise} \end{cases} \\
 & + \begin{cases} G_{\text{txcreate}} & \text{if } T_a = \emptyset \\ 0 & \text{otherwise} \end{cases} \\
 & + G_{\text{transaction}}
 \end{aligned} \tag{35}$$

- the total gas consumption does not exceed the block gas limit, i.e. $\sum_{T \in B_{T_S}} T_g \leq B_{H_t}$.
5. If **B** passes all above steps, then it is marked **accept** and added into the Tree-Graph structure, otherwise it is marked **reject** and discarded.

Note that because a valid block must pass all the above validation steps and there is no jump or loop, all validation steps are interchangeable and parallelizable.

We emphasize an important difference of Conflux from other blockchains in validating blocks: in Conflux we check the validity of each transaction locally, i.e. at this moment we do not care if it is a duplicate of some processed transaction or the sender has insufficient balance. Thus a block **B** being valid **does not** imply that all transactions in B_{T_S} are valid or will be eventually executed. The validation of transactions in B_{T_S} will be deferred to the finalization of **B**.

4.2 Total Order in the Tree-Graph

Every Conflux full node maintains a Tree-Graph structure of accepted blocks, and now we discuss how to decide the total order of all accepted blocks.

Recall that in the Tree-Graph each vertex represents a Conflux block and each directed edge represents the reference of another block. The vertex for the genesis block has no outgoing edges, since the genesis block does not reference any other block. Other than the genesis block, each block has exactly one parent reference and possibly multiple (can be zero) referee references, represented by multiple outgoing edges from the corresponding vertex. This directed graph is acyclic since every directed edge reflects a clear chronological order of blocks, unless the referenced block is generated using a hash collision. Based on this Tree-Graph structure the Conflux consensus will first select a pivot chain that defines order of blocks on the chain, and then extend to the total order of all blocks.

4.2.1 GHAST and Weight Adaption on the Tree-Graph

In Conflux the valid blocks may have heterogeneous weights, even if there is no difficulty adjustment. This feature is introduced to improve the liveness guarantee in case a divergence of computing power (which is also the block generation power) happens, either by chance or caused by an active attack.

At a high level, the GHAST rule defines block weight as follows:

- In the usual case, all valid blocks have homogeneous weight. That is, every block with a proof of work satisfying the target difficulty of the epoch it belongs to would have the same weight, say weight 1.
- When a divergence of block generation power is observed, the distribution of block weights is changed adaptively:
 - A small fraction of blocks are marked as “heavy blocks” and given a greater weight. In particular, if the attached proof of work of a block has difficulty at least **250** times of the epoch’s normal target difficulty, then this block is called a *heavy block* and its weight is also **250** times of a usual block, so as its base award.
 - Other blocks under this circumstance are still valid as long as the attached proof of work satisfies the normal target difficulty. But they have zero weight when making consensus decisions.
 - When the divergence is resolved, the weight distribution resumes to the usual case, where every block with a valid proof of work has the same weight as target difficulty of the epoch.

To be more specific, we remark that the GHAST rule only considers blocks in recent eras, e.g. the choice of parent edge is defined and validated *within* the subtree of the corresponding era genesis. See Section 4.3 for more details about era and checkpoints.

Timer Chain Conflux introduces the notion of timer block and timer chain as a robust estimation of elapsed time. Intuitively the timer chain is the longest chain that would be generated if the block generation were slow, or equivalently only high quality blocks were considered.

Every **fully valid** block **B** with quality $QUALITY(B) \geq 180 \cdot B_d$ is called a *timer block*. The partial order of timer blocks can be deduced from the Tree-Graph of all blocks, which then determines the longest chain of timer blocks, called the *timer chain*. More specifically, the genesis block is also genesis of the timer chain, and the “parent timer block” of every timer block **B** is recursively defined by choosing the tip of timer chain in $PAST(B)$. For convenience, the parent timer block of **B** is denoted by $P_{timer}(B)$.

For convenience the timer chain in Tree-Graph **G** is denoted by $TimerChain(G)$, and the difference of timer blocks in two Tree-Graphs **G** and **G'** is denoted by $TimerDis(G, G')$ as follows

$$TimerDis(G, G') \equiv |TimerChain(G) \setminus G'| \tag{36}$$

The timer block difference $TimerDis(G, G')$ provides an estimate of the time difference between two local views **G** and **G'**.

Triggering Condition of Adaptive Weight Intuitively, a block B should apply the adaptive weight rule if any previous pivot block (on $\text{CHAIN}(B)$) fails to receive support from a clear majority of computing power, i.e. the nemesis pivot block does not accumulate enough weight under its subtree after a sufficiently long time.

Formally, a block B is an *adaptive block*, denoted by $\text{Adaptive}(B) = \text{True}$, if there exists $B' \in \text{CHAIN}(B)$ satisfying both of the following conditions:

1. $\text{TimerDis}(\text{PAST}(B), \text{PAST}(P(B'))) \geq 240$;
2. $\text{SubTW}(B'; \text{PAST}(B)) - (\text{SubTW}(P(B'); \text{PAST}(B)) - \text{SubTW}(B'; \text{PAST}(B)) - \text{Weight}(P(B'))) < 1000 \cdot B_d$,
 where $\text{SubTW}(A; G)$ denotes the total weight of the sub-tree rooted at A in graph G , and $\text{Weight}(\cdot)$ is the adaptive weight function as defined in (37).

Otherwise the block B is a *non-adaptive block* and denoted by $\text{Adaptive}(B) = \text{False}$. The adaptive weight mechanism is only triggered for adaptive blocks.

Adaptive Block Weight Recalling that $\text{PoW}(\cdot)$ denotes the proof-of-work function and B_d denotes the target difficulty of B , the GHASt rule formally defines the weight of a block B as follows:

$$\text{Weight}(B) \equiv \begin{cases} B_d & \text{if } \neg \text{Adaptive}(B) \\ 0 & \text{if } \text{Adaptive}(B) \wedge 250 \cdot \text{PoW}(B_H) \cdot B_d > 2^{256} \text{ (i.e. } \text{QUALITY}(B) < 250 \cdot B_d) \\ 250 \cdot B_d & \text{if } \text{Adaptive}(B) \wedge 250 \cdot \text{PoW}(B_H) \cdot B_d \leq 2^{256} \text{ (i.e. } \text{QUALITY}(B) \geq 250 \cdot B_d) \end{cases} \quad (37)$$

We remark that whether a block B should be adaptive or not is fully determined by $\text{PAST}(B)$, which is indeed specified by B through directly and indirectly referenced blocks. Therefore it is not necessary to put a specific flag in the header of B for this condition, unless for efficiency concerns.

4.2.2 The GHASt Rule for Selecting the Pivot Chain

Since every block (except the genesis block) has exactly one parent, all parent edges in the Tree-Graph together form a *parental tree* with the genesis block being the root. In the parental tree, Conflux applies the GHASt rule to select a chain from the genesis block to one of the leaf blocks as the *pivot chain*, where blocks on the pivot chain are called *pivot blocks* and other blocks called *off-pivot blocks*.

In Conflux the pivot chain is not necessarily the longest chain or the “heaviest” chain. Indeed, the GHASt rule requires that the pivot chain should proceed to the branch whose subtree has greatest total weight (after weight adaption), in case there are multiple child blocks to choose. The Conflux selection algorithm starts from the genesis block. At each step, it computes the accumulated *total weight* of each child subtree in the parental tree and advances to the child block whose subtree has the largest total weight, until it reaches a leaf block in the local Tree-Graph.

The total weight of a subtree rooted at block B is denoted by B_t and defined recursively as:

$$B_t \equiv B_d + \sum_{B': P(B')=B} B'_t \quad (38)$$

where $B_d \equiv H(B)_d$ denotes the target difficulty of B , and $P(B')$ is the parent block of B' (hence the summation is taken over B 's children). Note that B_t is not a part of the block B – indeed it describes a state of B in the local view and may increase as more subsequent blocks are included afterwards.

We further remark that the total weight of every subtree can be computed from all block headers, since a block header contains the block difficulty as well as its parent and referees, which suffices to decide the weight of this block as in Section 4.2.1 and hence the total subtree weight recursively. As a result, the whole pivot chain can be determined by the block headers.

The advantage of the GHASt rule is that it guarantees the irreversibility of the selected pivot chain even if honest nodes fork because of network delays or other reasons. This is because forked blocks also contribute to the safety of the pivot chain (indeed, this property is inherited from GHOST rule, c.f. [1]).

For example, consider the local view as in Figure 1 and for simplicity suppose that all blocks have equal weight. Conflux would select Genesis, A, C, E, and H as pivot blocks. Note that they do not form the longest chain in the parental tree – the longest chain is Genesis, B, F, J, I, and K. Conflux does not select that longest chain because the subtree of A contains more blocks (and hence more total amount of computation) than the subtree of B. Therefore, the chain selection algorithm selects A over B at its first step.

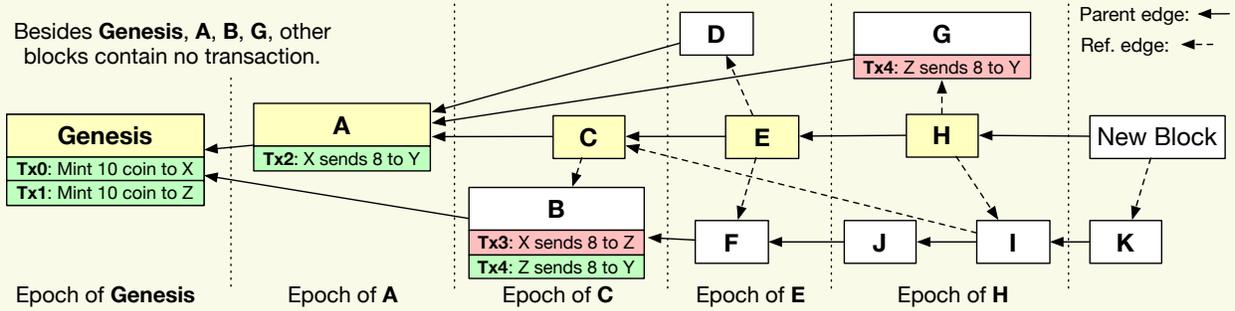


Figure 1. An example local Tree-Graph state to illustrate the consensus algorithm of Conflux. The yellow blocks are on the pivot chain in the Tree-Graph. Each block on the pivot chain forms a new epoch to partition blocks in the Tree-Graph.

4.2.3 Epoch

Given the pivot chain in a Tree-Graph, Conflux splits all blocks into epochs as follows:

- Every pivot block B is at epoch $H(B)_h$, or simply the *epoch of B* , which is denoted by $EPOCH(B)$. In particular the genesis block is at epoch 0.
- Every off-pivot block B' is at the epoch of the first pivot block B that references it, directly or indirectly. That is, every block $B' \in U(B)$ is at the epoch of B ; then every block B'' referenced by B' , i.e. $B'' \in U(B') \cup \{P(B')\}$, if not already included in an earlier epoch, is also at the epoch of B ; and recursively all blocks referenced by B'' and so on.

In other words, the epoch of B consists of all blocks within the local view of B , such that there blocks are potentially produced after $P(B)$ but clearly before B . For example, each of the pivot blocks Genesis, A, C, E, and H corresponds to one individual epoch in Figure 1. The block J belongs to the epoch of H but not the epoch of E, because J is reachable from H but not reachable from the previous pivot block E.

It is clear from the definition that as long as the pivot chain is not reverted, the partition of epochs cannot be changed.

Epoch capacity Each epoch now has a limit of executing 200 blocks. When a single epoch contains more than 200 blocks, Conflux will only execute the last 200 blocks (as specified in Section 4.2.4) in that epoch. This limit is introduced to battle DoS attacks about releasing a lot of blocks suddenly.

4.2.4 Total Order of Blocks

Conflux extends the total order of pivot blocks to all blocks in a Tree-Graph as follows. Conflux first sorts blocks according to their corresponding epochs, so that a block in an earlier epoch always precedes another block in a later epoch; and then Conflux sorts the blocks inside each epoch based on their topological order, i.e. corresponding to the partial order implied by referee references. In case two blocks have no partial order relation, Conflux breaks ties deterministically with the unique ids of these two blocks. More detailed rules are described with codes in Figure 2.

Input : A block B and the local Tree-Graph G (with B in G and G is the genesis block of G)

Output : A list of blocks $L = B_1 \circ B_2 \circ \dots \circ B_n$, where B_1, \dots, B_n are blocks in G , and in particular $B_1 = G$ and $B_n = B$

```

1  $B' \leftarrow P(B)$ 
2 if  $B' = \perp$  then
3   return  $B$ 
4  $L \leftarrow \text{ConfluxOrder}(B'; G)$ 
5  $L' \leftarrow$  An empty list
6  $\Delta \leftarrow \text{PAST}(B) \setminus (\text{PAST}(B') \cup \{B'\})$ 
7 while  $\Delta \neq \emptyset$  do
8    $\Delta' \leftarrow \Delta \setminus (\cup_{A \in \Delta} \text{PAST}(A))$ 
9    $B'' \leftarrow \arg \max_{A \in \Delta'} \{\text{Hash}(A)\}$ 
10   $L' \leftarrow B'' \circ L'$ 
11   $\Delta \leftarrow \Delta \setminus \{B''\}$ 
12  $L \leftarrow L \circ L' \circ B$ 
13 return  $L$ 

```

Figure 2. The Definition of the ConfluxOrder function.

For example, the local Tree-Graph in Figure 1 may give a total order as Genesis, A, B, C, D, F, E, G, J, I, H, and K. The order of D and F may change if the block id of F is smaller than D, and the same holds for G, J, and I.

Here we remark that the weight of blocks is not used when extending the pivot chain to the total order of all blocks. All blocks, even blocks with zero weight after adaption, are treated equally in this procedure.

4.2.5 Total Order of Transactions

Conflux first sorts transactions based on the relative order of their enclosing blocks. In case two transactions belong to the same block, Conflux sorts them based on their appearance order in that block. Conflux checks conflicts of transactions at the same time when deriving the orders. If two transactions are conflicting with each other, e.g. they have exactly the same sender and nonce, then Conflux will attempt to execute the first one and ignore the second one if the first one is executed. If one transaction appears in multiple blocks, Conflux will keep the first valid appearance of this transaction and discard all redundant ones.

For example, the transaction total order in Figure 1 is Tx0, Tx1, Tx2, ~~Tx3~~, Tx4, and ~~Tx4~~, where Conflux discards Tx3 because it conflicts with a previously executed valid transaction Tx2, and discards the second appearance of Tx4 because it is redundant.

4.3 Checkpoint

Conflux implements a checkpoint mechanism to tailor the ever-growing blockchain history data. At a high level, every 50000 epochs form an *era*² and a *checkpoint* is made when the era genesis block becomes stable. Thereafter, full nodes can safely discard the content of old blocks.

4.3.1 Era and Era Genesis

Formally, eras in Conflux are partitioned with respect to the height of pivot blocks. Every 50000 height corresponds to one era, and in particular the pivot block of height $50000 \cdot N$ is called the *era genesis block of Era N*. For example, the genesis block, which is the only block at height 0, is the era genesis block of Era 0 (i.e. the first era); the pivot block at height 50000 is the era genesis block of Era 1 (i.e. the second era). Furthermore, an era genesis will eventually be finalized and become a *stable era genesis*, which is irreversible in any case.

The stable era geneses are recursively defined as below:

1. The genesis block is the first stable era genesis.
2. An era genesis block G becomes a stable era genesis if it satisfies the following:
 - G is in the subtree of the last stable era genesis;
 - the subtree of G contains 240 *consecutive* timer blocks ended by B , i.e. $\exists B$ such that $B, P_{timer}(B), \dots, P_{timer}^{(239)}(B)$ are all in the subtree of G ;
 - there are 240 *consecutive* timer blocks in the future of B (these blocks are not necessarily within the subtree of G).
3. Era genesis blocks preceding a stable era genesis are also stable.

Let the latest stable era genesis block of a Tree-Graph G be denoted by $\text{StableEraGenesis}(G)$. The GHAST rule, including weight adaption and parent selection (as specified in Section 4.2.1 and 4.2.2), are applied within the subtree of $\text{StableEraGenesis}(G)$. The anti-cone penalty, as defined in Section 9.1.1, is also subject to blocks within the subtree of $\text{StableEraGenesis}(G)$, though such restriction makes no essential difference according to current anti-cone parameters.

4.3.2 Truncation of Consensus Tree-Graph

In a Tree-Graph G , the latest stable era genesis $\text{StableEraGenesis}(G)$ is indeed a checkpoint that can be treated as the “new genesis block” thereafter, since the consensus rules only apply to blocks within the subtree of $\text{StableEraGenesis}(G)$. Therefore, the bodies of blocks in PAST($\text{StableEraGenesis}(G)$) are no longer needed for future world-states and can be safely discarded from every full node’s memory. However, the headers of those blocks in PAST($\text{StableEraGenesis}(G)$) are still needed for validation of references from future blocks (blocks outside the future set $\text{FUTURE}(\text{StableEraGenesis}(G); G)$ may reference blocks in PAST($\text{StableEraGenesis}(G)$)).

For convenience we let B' and B'' denote the latest two stable era geneses as follows:

$$B' \equiv \text{StableEraGenesis}(G)$$

$$B'' \equiv \text{StableEraGenesis}(\text{PAST}(B'))$$

Blocks missing one stable era genesis, i.e. the blocks in $\text{FUTURE}(B''; G) \setminus \text{FUTURE}(B'; G)$, can be referenced by a new block in G but will not affect consensus decision. Blocks missing two stable era geneses, i.e. the blocks outside $\text{FUTURE}(B''; G)$, cannot be referenced. More specifically, when adding a new block B into the Tree-Graph G , the validity of B is examined as follows:

²In geologic time scale, *eons* are divided into *eras*, which are in turn divided into *periods*, *epochs* and *ages*.

1. If $B \notin \text{FUTURE}(B''; \mathbf{G})$, then B is discarded.
2. If $B \in \text{FUTURE}(B''; \mathbf{G}) \setminus \text{FUTURE}(B'; \mathbf{G})$, then B is partially valid. That is, the block B has zero weight in consensus decision and should not be referenced, but the transactions in B_{TS} are still valid.
3. If $B \in \text{FUTURE}(B'; \mathbf{G})$ but $P(B) \notin \text{SubTree}(B''; \mathbf{G})$, then B is also partially valid.
4. Otherwise follow the rules in Section 3.4.5.

4.4 Finalization

In this part we discuss when a block or a transaction in Conflux is considered irreversible, or “finalized”. This is crucial for off-chain users to decide when to confirm a transaction or a state.

Like every other PoW consensus system, the risk that an adversary succeeds in reverting the blockchain history decreases over time but never goes to zero. That is, there is always a positive probability, no matter how tiny it is, that an adversary generates a branch with higher accumulated weight than the one generated by honest parties. This is a nature of PoW consensus but not one weakness, because: 1) a sufficiently small probability is usually considered equivalent to zero in practice; 2) that tiny probability can be made even smaller than the probability that an adversary breaks the public-key cryptosystem or finds a collision of the hash reference, and hence not the bottleneck of security. Therefore, in order to decide the concrete finalization rule, a user must specify how much risk he can tolerate as well as his (perhaps subjective) assumption about several system parameters.

In what follows we elaborate the finalization of a block. A transaction T is finalized if the first block B' where T is **executed** becomes finalized. This is a sufficient but sometimes not necessary condition³. Note that “the first block including T becomes finalized” is insufficient, since Conflux allows invalid transactions.

Consider the block B' in a Tree-Graph and suppose that B' belongs to the epoch of a pivot block B . Then the finalization of B' reduces to the finalization of B on the pivot chain. The user can decide whether B is finalized as follows:

1. Estimate or make assumptions about following system parameters:
 - **Block Generation Rate:** Let $q \equiv \lambda_a / \lambda_h$ where λ_h denotes the combined block generation rate of honest nodes and λ_a denotes the block generation rate of attacker. The user needs to make an assumption of the attacker’s power by setting an upper bound for q .
 - **Network Synchronization:** If at time t , an honest node broadcasts a block via the gossip network, then by time $t + d$ all honest nodes receive this block (the nodes not receiving by time $t + d$ will be counted as adversary). According to our experiment in a globally distributed testing environment, we set d equal to 10 seconds.
2. Make sure that all the pivot blocks preceding B have been finalized.
3. Make sure that block B stays on the pivot chain since $2d$ time ago.
4. For $q \leq 0.2$, compute the confirmation risk r_1 according to the **Fast Confirmation Rule**.
 - The fast confirmation rule assumes that the GHASt weight adaption is not triggered under the subtree of $P(B)$ during the generation of 8000 blocks (≈ 1.1 hours) since the creation of $P(B)$.
 - Let r_2 denote the risk that an attacker breaks the above assumption.
5. For $q < 1$, compute the confirmation risk r_3 according to the **Slow Confirmation Rule**.
6. The confirmation risk for B is bounded as $\text{Risk}(B) \leq \min \{r_1 + r_2, r_3\}$.

4.4.1 Fast/Slow Confirmation Rules

Since evaluating $\text{Risk}(B)$ may be costly, we provide the following simple (but not tight) formulas for risk estimation. These estimations are conservative and hence result in a longer confirmation time. Users, especially those who are also developers, are encouraged to make more accurate estimation and design sophisticated strategies to achieve a better balance between confirmation time and security.

For the estimation of confirmation risk, we introduce the following values with respect to the current local Tree-Graph \mathbf{G} and any block $A \in \mathbf{G}$.

- c_0 : the total weight of all blocks locally observable in \mathbf{G} ;
- c_1 : the total weight of received blocks in the past $2d$ time (in local clock);

³The finalization of a transaction may be much faster. For example, a simple transaction T may be safely confirmed before the blocks containing T being finalized, if the execution of T is indifferent of the agreement of pivot chain, i.e. no conflicting or dependent transactions of T included in competing blocks.

- \mathbf{d} : the largest target difficulty in the last one day (in local clock);
- $w_1(\mathbf{A})$: the total weight of blocks under the subtree rooted at \mathbf{A} in \mathbf{G} , i.e. $w_1(\mathbf{A}) \equiv \sum_{\mathbf{A}' \in \mathbf{G}: \mathbf{A} \in \text{CHAIN}(\mathbf{A}')} \text{Weight}(\mathbf{A}')$;
- $w_2(\mathbf{A})$: the maximum weight of subtrees rooted at blocks in $\text{SIBLING}(\mathbf{A})$, i.e. $w_2(\mathbf{A}) \equiv \max_{\mathbf{A}' \in \text{SIBLING}(\mathbf{A})} \{w_1(\mathbf{A}')\}$ (here malicious blocks can be excluded for better performance, while failing to exclude malicious blocks would result in a correct but more conservative (less accurate) estimation for the upper bound of confirmation risk);
- $w_3(\mathbf{A})$: the total weight of all the blocks in $\text{PAST}(\mathbf{A})$, i.e. $w_3(\mathbf{A}) \equiv \sum_{\mathbf{A}' \in \text{PAST}(\mathbf{A})} \text{Weight}(\mathbf{A}')$.

Then we let n be the estimation of \mathbf{B} 's advantage over its siblings, and m denote the total (equivalent) number of blocks competing with \mathbf{B} , where n and m are formally defined as below:

$$n \equiv \lceil (w_1(\mathbf{B}) - w_2(\mathbf{B}) - c_1) / \mathbf{d} \rceil, \quad m \equiv \lfloor (c_0 - w_3(\mathbf{P}(\mathbf{B}))) / \mathbf{d} \rfloor \quad (39)$$

If n approaches m quickly then it must be the case that most of the mining power are concentrating under the subtree of \mathbf{B} , in which case the block \mathbf{B} can be finalized using the Fast Confirmation Rule. However, it is possible that the Fast Confirmation Rule is never satisfied for a predetermined risk tolerance in case the convergence of mining power is not that timely. Then the confirmation of \mathbf{B} has to rely on the Slow Confirmation Rule, which takes time but will eventually come true as long as the majority of mining power is honest.

Table 1. The confirmation risk lookup table for Fast Confirmation Rule.

Risk tolerance \ Adversary power	$q \leq 0.1$ (i.e. 9.1% adversary)	$q \leq 0.2$ (i.e. 16.7% adversary)
Risk(\mathbf{B}) < 10^{-4}	$m - n \leq \min\{0.85m - 12, 4400\}^*$	$m - n \leq \min\{0.75m - 22, 2250\}$
Risk(\mathbf{B}) < 10^{-6}	$m - n \leq \min\{0.80m - 12, 3800\}$	$m - n \leq \min\{0.70m - 22, 1500\}$
Risk(\mathbf{B}) < 10^{-8}	$m - n \leq \min\{0.75m - 12, 3200\}$	$m - n \leq \min\{0.65m - 22, 750\}$

* Slightly better security than confirmation with 6 successive blocks in Bitcoin.

Table 2. The confirmation risk lookup table for Slow Confirmation Rule.

Risk tolerance \ Adversary power	$q \leq 0.25$ (i.e. 20% adversary)	$q \leq 0.5$ (i.e. 33.3% adversary)
Risk(\mathbf{B}) < 10^{-4}	$m - n \leq 0.6m - 5700^\dagger$	$m - n \leq 0.35m - 10900$
Risk(\mathbf{B}) < 10^{-6}	$m - n \leq 0.6m - 7200$	$m - n \leq 0.35m - 13600$
Risk(\mathbf{B}) < 10^{-8}	$m - n \leq 0.6m - 8700$	$m - n \leq 0.35m - 16200$

† Security equivalent to confirmation with 13 ~ 14 successive blocks in Bitcoin.

Safety of Fast Confirmation Rule. Now we upper bound the risk r_2 that the GHASt weight adaption is triggered within 8000 successive blocks since the generation of $\mathbf{P}(\mathbf{B})$.

Let h be the height of the latest stable era genesis block in the current Tree-Graph \mathbf{G} . Let \mathbf{B}_i denote the block at height $h + i$ on $\text{CHAIN}(\mathbf{B})$. Let ψ be an arbitrary positive integer (e.g. $\psi = 50$). For integer $j \in \mathbb{N}$, let m' and m_j, n_j be defined as follows:

$$m' \equiv \lfloor (c_0 - w_3(\mathbf{P}(\mathbf{B}))) / \mathbf{d} \rfloor \quad (40)$$

$$n_j \equiv \lceil (w_1(\mathbf{B}_{(j+1) \cdot \psi}) - \max_{i \in (j \cdot \psi, (j+1) \cdot \psi)} w_2(\mathbf{B}_i) - c_1) / \mathbf{d} \rceil - m' \quad (41)$$

$$m_j \equiv \lfloor (c_0 - w_3(\mathbf{B}_{j \cdot \psi})) / \mathbf{d} \rfloor \quad (42)$$

Let j_{\max} be the largest integer satisfying $\text{TimerDis}(\mathbf{G}, \text{PAST}(\mathbf{B}_{j_{\max} \cdot \psi})) \geq 140$. For $q \leq 0.2$, the risk r_2 is bounded by

$$10^{-7} + \sum_{j=0}^{j_{\max}} 10^{(m_j/3 - n_j)/700 + 5.3} \quad (43)$$

5. Transaction Processing

Conflux implements the same virtual machine as Ethereum [3]. Roughly speaking, after determining the total order of transactions and removing invalid transactions, the remaining valid transactions are executed on the EVM as if they are packed into sequential blocks on an Ethereum-like chain. In what follows we focus on the Conflux specific designs in the execution.

5.1 Gas and Payment

As defined in Section 3.3 every transaction T has two fields of **gasLimit** and **gasPrice** that declare the specific amount of associated gas T_g and the price T_p of per unit gas. When starting the execution of a transaction T , the purchase of gas happens at the price $T_g \times T_p$ and the transaction T is considered invalid if the actor responsible for the cost of gas consumption cannot afford such a purchase. Normally $S(T)$, the sender of T , is responsible for the cost of gas consumption. In case the transaction T is calling a smart contract C with sponsorship for gas consumption and T is qualified for the subsidy as specified in Section 7.1, C is responsible for the purchase of gas if it has sufficient **sponsor balance for gas**, and otherwise the sender $S(T)$ is still responsible for the whole purchase of gas as if there were no sponsor at all. Like in Ethereum, gas does not exist outside the execution of transactions.

The unused gas can be refunded after the transaction T is executed, but no more than a quarter of the total value spent on purchasing. Thus, the *refundable amount of gas* g^\dagger is the minimum of the *legitimately remaining gas* g' and a quarter of the **gasLimit** of T , i.e. $g^\dagger \equiv \min\{g', T_g/4\}$, where in principle no gas is refundable (i.e. $g^\dagger = g' = 0$) if the execution of T fails due to the sender's fault. The *consumed amount of gas*⁴ $\text{Gas}_{\text{used}}(T)$ is defined as

$$\text{Gas}_{\text{used}}(T) \equiv \begin{cases} T_g - g^\dagger & \text{if } T \text{ is executed} \\ 0 & \text{if } T \text{ is not executed (i.e. only when } R_z = 2 \text{ as in Section 5.2)} \end{cases}$$

The actor who initially purchased the gas for T will get the refund of $g^\dagger \times T_p$.

The CFX paid for the consumed gas, which is $\text{Gas}_{\text{used}}(T) \times T_p = (T_g - g^\dagger) \times T_p$, is added to the reward pool for miners. Thus in general a higher gas price on a transaction would cost the sender more but also increase the chance of being processed timely.

5.2 Pre-execution Validation

Before being executed, a transaction T in the processing queue must pass the following secondary test of intrinsic validity.

1. The current epoch is in the range specified by **epochHeight**, i.e. current epoch height is in $[T_e - 100000, T_e + 100000]$.
2. The transaction **nonce** is valid, i.e. $T_n = \sigma[S(T)]_n$ where σ is the current world-state.
3. The recipient address is valid, i.e. the type indicator (first 4-bit) of T_a belongs to $\{[0000]_2, [0001]_2, [1000]_2\}$.

Note that the local legality of the transaction, e.g. the RLP format and the validity of signature, is already verified in the first intrinsic validity test before accepting the corresponding block into the Conflux Tree-Graph, as discussed in Section 4.1, and will not be checked again at this moment.

If T fails at these checks, the transaction will not be executed, the nonce for account will not increase and no transaction fee is charged for such transaction. Let R' be the receipt of last transaction. Then the receipt of current transaction will be as follows:

$$R_u = R'_u \qquad R_1 = \varepsilon \qquad R_z = 2 \qquad R_o = \varepsilon \qquad R_i = \varepsilon \qquad (44)$$

(The bloom filter R_b of $\log R_1$ is computed accordingly.)

If T passes all the above pre-execution checks, the execution of T is as specified in the rest of this section.

5.3 Transaction Execution

The execution of the transaction T transforms the world-state from σ into $\sigma' \equiv Y(\sigma, T)$ following the function Y with the following steps.

5.3.1 Preprocessing

In the preprocessing phase of T , the balance of $S(T)$ (and the sponsor, if applicable) is examined so that the payment for any further operation is assured. The world-state will be transformed from σ into $\sigma^0 \equiv \sigma^{**}$ if T passes the preprocessing, or directly into σ' and the execution is aborted if T fails at any step.

Responsibility for not enough balance. If T is calling a contract C , then Conflux first assumes that C has unlimited **sponsor balance for gas** and **sponsor balance for collateral** and rehearses the preprocessing steps. If the rehearsal succeeds, then the contract C is considered responsible for possible *not enough balance exception*. Otherwise the sender $S(T)$ is responsible for it. If T is calling a non-sponsored account, the sender is always responsible for *not enough balance exception*.

⁴Here for simplicity we write $\text{Gas}_{\text{used}}(\cdot)$ as a function of T . However it is indeed a function defined on both T and the world-state at the beginning of the execution of T . Thus, multiple occurrences of T are considered as distinct inputs for this function and they may incur different amount of consumed gas.

Nonce incremental. The beginning of execution causes an irrevocable changed to the state σ : the nonce of the sender, $S(T)_n$, is incremented by one. We define the state σ^* :

$$\sigma^* \equiv \sigma \quad \text{except:} \quad (45)$$

$$\sigma^*[S(T)]_n \equiv \sigma[S(T)]_n + 1 \quad (46)$$

Up-front payment validation. The up-front payment of a transaction T consists of the gas fee $T_g \times T_p$ and the transferred value T_v , which is validated as follows.

- For value-transferring transaction T where the recipient of T is a normal account, the balance of $S(T)$ should satisfy $\sigma^*[S(T)]_b \geq T_g \times T_p + T_v$ and otherwise a *not enough balance exception* is generated. The world-state after the up-front payment is defined as:

$$\sigma^{**} \equiv \sigma^* \quad \text{except:} \quad (47)$$

$$\sigma^{**}[S(T)]_b \equiv \max \{ \sigma^*[S(T)]_b - T_g \times T_p, 0 \} \quad (48)$$

- For transaction T calling a contract C where $C_p[\text{gas}]_b$ and $C_p[\text{limit}]$ denote the **sponsor limit for gas fee** and **sponsor balance for gas** of C :

- If $S(T)$ is not in the **whitelist** of C or the claimed gas fee exceeds the sponsor limit for gas with $T_p \times T_g > C_p[\text{limit}]$, then T is not eligible for sponsorship on gas consumption. The execution of T fails and generates a *not enough balance exception* if $\sigma^*[S(T)]_b < T_g \times T_p + T_v$. The world-state after the up-front payment is defined as:

$$\sigma^{**} \equiv \sigma^* \quad \text{except:} \quad (49)$$

$$\sigma^{**}[S(T)]_b \equiv \max \{ \sigma^*[S(T)]_b - T_g \times T_p, 0 \} \quad (50)$$

- If $S(T)$ is in the **whitelist** of C and $T_p \times T_g \leq \min \{ C_p[\text{gas}]_b, C_p[\text{limit}] \}$, then the gas consumption of T is sponsored. The execution of T may fail due to *not enough balance exception* if and only if $\sigma^*[S(T)]_b < T_v$. The world-state σ^{**} after charging gas fee is as follows:

$$\sigma^{**} \equiv \sigma^* \quad \text{except:} \quad (51)$$

$$\sigma^{**}[C_{addr}]_p[\text{gas}]_b \equiv \sigma^*[C_{addr}]_p[\text{gas}]_b - T_g \times T_p \quad (52)$$

- Otherwise, when $S(T)$ is in the **whitelist** of C and $C_p[\text{gas}]_b < T_p \times T_g \leq C_p[\text{limit}]$, T is eligible for sponsorship on gas consumption but it is not sponsored because the contract balance is insufficient. In this case, if the sender's balance affords the transferred value but not the whole up-front payment, i.e. $T_v \leq \sigma^*[S(T)]_b < T_g \times T_p + T_v$, then the sender $S(T)$ is considered not responsible for the generated *not enough balance exception* and the world-state is reverted to $\sigma^{**} \equiv \sigma$. Note that in this specific case the sender's nonce $\sigma^{**}[S(T)]_n$ is reverted to $\sigma[S(T)]_n$ so that T is reusable. In other cases when the sender $S(T)$ is responsible for causing the *not enough balance exception*, i.e. the sender's balance is either sufficient for the whole up-front payment or even less than the transferred value, the resultant world-state σ^{**} will be the same as unsponsored case in (49).

Thus, whenever the execution of T fails and generates a *not enough balance exception*, there will be no further execution of T and the resultant world-state would be $\sigma' \equiv \sigma^{**}$. The corresponding receipt is then composed as follows (where R' refers to the receipt of last transaction):

- If sender $S(T)$ is responsible for the exception, i.e. $\sigma^*[S(T)]_b < T_g \times T_p + T_v$ when T is not eligible for sponsorship or $\sigma^*[S(T)]_b < T_v$, then the receipt of this execution will be

$$R_u = R'_u + \max \{ \sigma^*[S(T)]_b - T_g \times T_p, 0 \} \quad R_l = \varepsilon \quad R_z = 1 \quad R_o = \varepsilon \quad R_i = \varepsilon \quad (53)$$

- Otherwise if sender $S(T)$ is not responsible for the exception, i.e. when $S(T)$ is in the **whitelist** of C and $\sigma^*[S(T)]_b \geq T_v$, then the receipt will be

$$R_u = R'_u \quad R_l = \varepsilon \quad R_z = 2 \quad R_o = \varepsilon \quad R_i = \varepsilon \quad (54)$$

Storage limit validation. After the up-front payment validation, Conflux decides who is responsible for storage collateral. The storage limit ℓ is set to $\min \{ T_l, 2^{64} - 1 \}$. If T is calling a sponsored contract C with $\ell \times 10^{18} / 1024 \leq C_p[\text{col}]_b$ (where $C_p[\text{col}]_b$ refers to the **sponsor balance for collateral** of C) and $S(T)$ in the **whitelist** of C , then contract C is responsible for

the storage collateral resulted in the execution of T and will be the owner of modified entries. Otherwise, the sender $S(T)$ is the owner of modified entries and has the obligation to pay corresponding storage collateral.

If $S(T)$ is the storage owner but his balance cannot afford the full collateral as declared in **storageLimit**, i.e. $\sigma^{**}[S(T)]_b < \ell \times 10^{18}/1024$, then the execution of T fails due to *not enough balance exception*. The resultant world-state and receipt are defined as follows:

- If T is not eligible for sponsorship on storage collateral, i.e. $S(T)$ not in the **whitelist** of C , then the resultant world-state is $\sigma' \equiv \sigma^{**}$ and the receipt is as follows (where R' refers to the receipt of last transaction):

$$R_u = R'_u + T_g \times T_p \quad R_l = \varepsilon \quad R_z = 1 \quad R_o = \varepsilon \quad R_i = \varepsilon \quad (55)$$

- Otherwise if T is eligible for sponsorship on storage collateral but neither C nor $S(T)$ affords the cost of collateral as declared in the **storageLimit** T_ℓ , the resultant world-state is reverted to $\sigma' \equiv \sigma$ and the receipt is as below:

$$R_u = R'_u \quad R_l = \varepsilon \quad R_z = 2 \quad R_o = \varepsilon \quad R_i = \varepsilon \quad (56)$$

5.3.2 Execution Substate

The *transaction substate* A is a five tuple which accrues intermediate information during execution.

$$A \equiv (A_s, A_l, A_t, A_o, A_e) \quad (57)$$

The components of A are defined as follows:

- A_s is the self-destruct set of accounts that will be discarded upon the transaction's completion.
- A_l is the log series consisting of indexable “checkpoints” in the VM code execution, allowing light clients to track the execution of a contract.
- A_t is the set of touched accounts, of which the empty ones will be deleted on the transaction's completion.
- A_o is the list of storage collateral occupation.
- A_e is the list of storage collateral release.

The empty substate A^0 , which is also the initial substate, has no self-destructs, no logs, no touched accounts, and zero refund. Formally, A^0 is defined as

$$A^0 \equiv (\emptyset, \varepsilon, \emptyset, \varepsilon, \varepsilon) \quad (58)$$

5.3.3 Type dependent execution

If transaction passes the preprocessing, then Conflux evaluates the *post-execution provisional state* σ^P from *pre-execution provisional state* σ^0 depending on the transaction type as specified in T_a : either contract creation or message call. The gas available for the proceeding computation is $g \equiv T_g - g_0$, where g_0 is the intrinsic cost of T as in (35).

We define the tuple of post-execution provisional state σ^P , remaining gas g' , accrued substate A and status code z :

$$(\sigma^P, g', A, z) \equiv \begin{cases} \Lambda(\sigma^0, \sigma^0, S(T), S(T), i, g, T_p, T_v, T_i, 0, T) & T_t = \emptyset \\ \Theta(\sigma^0, \sigma^0, S(T), S(T), i, T_t, T_t, g, T_p, T_v, T_v, T_d, 0, T) & T_t \neq \emptyset \end{cases} \quad (59)$$

where i is the address paying for storage collateral decided in preprocessing. Notice that we have two more parameters at the second and the fifth positions compared with Ethereum.

The specifications of function Λ and Θ are given in Section 5.4 and Section 5.5 respectively.

5.3.4 Postprocessing

Storage collateral refund and charge. After the message call or contract creation is processed, Conflux checks whether the incremental storage exceeds storage limit specified in T_ℓ and if the storage owner has enough balance for storage collateral. Let v be the available balance to pay for storage collateral, which is defined as

$$v \equiv \begin{cases} \sigma^P[i]_b & \text{if } i = S(T) \\ \sigma^P[T_t]_p[\text{col}]_b & \text{if } i = T_t \end{cases} \quad (60)$$

Let $\sigma^P[i]_o - \sigma^0[i]_o$ be the incremental storage collateral during execution. If $\sigma^P[i]_o - \sigma^0[i]_o > \min\{v, \ell \times 10^{18}/1024\}$, then the execution fails because of exceeding the storage limit, and all the modified state will be reverted to σ^0 , i.e. $\sigma' \equiv \sigma^0$. Let R' denote the receipt of last transaction. Then the receipt of current transaction T will be

$$R_u = R'_u + T_g \times T_p \quad R_l = \varepsilon \quad R_z = 1 \quad R_o = \varepsilon \quad R_i = \varepsilon \quad (61)$$

Otherwise Conflux charges and refunds storage collateral and transforms world-state σ^P into σ^* . We skim the self-destructed contracts here because their storage collateral have been refunded during self-destruction.

$$\sigma^* \equiv \sigma^P \quad \text{except:} \quad (62)$$

$$\forall a \in \mathbb{B}_{160} \text{ with } \sigma^P[a] \neq \emptyset \text{ and } a \notin A_s \quad (63)$$

$$\begin{cases} \sigma^*[a]_p[\text{col}]_b \equiv \sigma^P[a]_p[\text{col}]_b - (\sigma^P[a]_o - \sigma^0[a]_o) & \text{if } a \text{ refers to a contract account, i.e. } \text{Type}_a = [1000]_2 \\ \sigma^*[a]_b \equiv \sigma^P[a]_b - (\sigma^P[a]_o - \sigma^0[a]_o) & \text{if } a \text{ refers to a normal account, i.e. } \text{Type}_a = [0001]_2 \end{cases} \quad (64)$$

Gas fee refund. The *refundable amount of gas* g^\dagger is the minimum of the *legitimately remaining gas* g' (as calculated in (59)) and a quarter of the **gasLimit** of \mathbb{T} , i.e. $g^\dagger \equiv \min\{g', \mathbb{T}_g/4\}$. The refund of gas fee is applied on world-state σ^* and results in $\sigma' \equiv \Upsilon(\sigma, \mathbb{T})$.

$$\sigma' \equiv \sigma^* \quad \text{except:} \quad (65)$$

$$\begin{cases} \sigma'[\mathbf{C}_{addr}]_p[\text{gas}]_b \equiv \sigma^*[\mathbf{C}_{addr}]_p[\text{gas}]_b + g^\dagger \times \mathbb{T}_p & \text{if contract } \mathbf{C} \text{ paid the gas fee} \\ \sigma'[\mathbf{S}(\mathbb{T})]_b \equiv \sigma^*[\mathbf{S}(\mathbb{T})]_b + g^\dagger \times \mathbb{T}_p & \text{if the sender paid the gas fee} \end{cases} \quad (66)$$

Transaction Receipt. Now the transaction execution is accomplished. The returning status code z denotes whether the execution succeeds or not. Supposing that R' is the receipt of last transaction, the receipt of current transaction will be as follows:

$$R_u = R'_u + (\mathbb{T}_g - g^\dagger) \times \mathbb{T}_p \quad R_{\mathbf{1}} = A_{\mathbf{1}} \quad R_z = z \quad R_{\mathbf{0}} = \text{Agg}(A_{\mathbf{0}}) \quad R_{\mathbf{i}} = \text{Agg}(A_{\mathbf{i}}) \quad (67)$$

where $\text{Agg}(\cdot)$ refers to aggregating the list of key/value pairs into groups by keys, taking the summation of values for each group and sort the results in ascending order of keys.

5.4 Contract Creation

A number of intrinsic parameters are used when creating a smart contract account:

- world-state σ ;
- original world-state $\tilde{\sigma}$;
- sender s ;
- original sender o ;
- storage owner i ;
- available gas g ;
- gas price p ;
- endowment v ;
- initialization code \mathbf{i} as an arbitrary length byte array;
- the present depth of message-call/contraction-creation stack e ;
- the salt for new account's address ζ ,
where $\zeta = \emptyset$ if the creation was caused by **CREATE**, and $\zeta \in \mathbb{B}_{256}$ if the creation was caused by **CREATE2**;
- and finally the permission to change the state w .

We define the contract creation function by Λ , which evaluates from the above parameters and modifies the state σ to a new state σ' , together with the leftover gas g' , the accrued substate A , the result of creation, and the output \mathbf{o} .

$$(\sigma', g', A, z, \mathbf{o}) \equiv \Lambda(\sigma, \tilde{\sigma}, s, o, i, g, p, v, \mathbf{i}, e, w) \quad (68)$$

The address a of the account α newly created by **CREATE** is defined as the 4-bit contract type indicator concatenating the rightmost 156 bits (i.e. the 100-th to 255-th bit) of the Keccak hash of a zero byte, the sender address s , the little-endian 32-byte array of its account nonce and the Keccak hash of EVM code. For **CREATE2** the rule is slightly different by substituting account nonce with the salt ζ and changing the leading byte before taking Keccak (following EIP-1014). Combining these two cases, the resultant address for the new contract account α is defined as follows:

$$a = A(s, \sigma[s]_n - 1, \zeta, \mathbf{i}) \equiv \begin{cases} [1000]_2 \circ \text{KEC}([00]_{16} \circ s \circ \text{LE}_{32}(\sigma[s]_n - 1) \circ \text{KEC}(\mathbf{i})) [100 \dots 255] & \text{if } \zeta = \emptyset \\ [1000]_2 \circ \text{KEC}([\text{ff}]_{16} \circ s \circ \zeta \circ \text{KEC}(\mathbf{i})) [100 \dots 255] & \text{otherwise} \end{cases} \quad (69)$$

where $\text{LE}_{32}(\cdot)$ denotes the function that expands an integer value in $[0, 2^{256} - 1]$ to a little-endian 32-byte array. Note that we use $\sigma[s]_n - 1$ since it is indeed the sender's nonce at the generation of the respective transaction or VM operation.

If $\sigma[a] \neq \emptyset$, a *Contract Address Conflict* exception is triggered. Function Λ returns $(\emptyset, g, A^0, 1, \emptyset)$ immediately.

Otherwise, the account's nonce is initialized to one, the balance as the value passed by the contract creation transaction, the storage and code as for the empty string. The sender's balance is reduced by the transferred value (there must be enough balance or the transaction will not be executed). Thus the mutated state becomes σ^* :

$$\sigma^* \equiv \sigma \quad \text{except:} \quad (70)$$

$$\sigma^*[a] \equiv \alpha^0 \quad \text{except: } \sigma^*[a]_n = 1 \wedge \sigma^*[a]_b = v \wedge \sigma^*[a]_a = s \wedge \sigma^*[a]_w = i \quad (71)$$

$$\sigma^*[s] \equiv \begin{cases} \emptyset & \text{if } \sigma[s] = \emptyset \wedge v = 0 \\ \sigma[s] & \text{except: } \sigma^*[s]_b = \sigma[s]_b - v \quad \text{otherwise} \end{cases} \quad (72)$$

where α^0 is the default account specified in eq. (2).

The unmentioned components of an account are initialized by default.

Finally the account α is initialized by EVM code \mathbf{i} according to the execution model. Code execution may effect several events that are not internal to the execution state: the account's storage can be altered, further accounts can be created and further messages calls can be made. As such, the code execution function Ξ evaluates to a tuple of resultant state σ^{**} , available gas remaining g^{**} , the accrued substate A and the body code \mathbf{o} .

$$(\sigma^{**}, g^{**}, A, \mathbf{o}) \equiv \Xi(\sigma^*, g, I) \quad (73)$$

where I consists of the parameters of the execution environment as follows:

$$I_a \equiv a \quad (74)$$

$$I_o \equiv o \quad (75)$$

$$I_i \equiv i \quad (76)$$

$$I_p \equiv p \quad (77)$$

$$I_d \equiv \varepsilon \quad (78)$$

$$I_s \equiv s \quad (79)$$

$$I_v \equiv v \quad (80)$$

$$I_b \equiv \mathbf{i} \quad (81)$$

$$I_H \equiv H \quad (82)$$

$$I_e \equiv e \quad (83)$$

$$I_w \equiv w \quad (84)$$

$$I_\sigma \equiv \tilde{\sigma} \quad (85)$$

I_d evaluates to the empty tuple as there is no input data to this call. I_H is the block header of the present block.

Code execution depletes gas, and gas may not go below zero, thus the actual execution may exit before the code has come to a natural halting state. In this (and several other) exceptional cases we say an out-of-gas (OOG) exception has occurred: the evaluated state is set to the empty set \emptyset , and the entire contract creation should have no effect on the state, effectively leaving it as it was immediately prior to the attempt of the failed creation.

If the initialization code completes successfully, a final storage cost is charged for depositing the code. The storage cost s is proportional to the code size of the created contract and it consists of two parts:

- the code-deposit cost d charged as gas consumption:

$$d \equiv |\mathbf{o}| \times G_{\text{codedeposit}} \quad (86)$$

- the collateral for storage c (measured in Drip) that will be locked during the lifetime of the created contract (Conflux will record the owner of code in world-state and refund the collateral when the contract is destroyed):

$$c \equiv \frac{10^{18}}{1024} \times |\mathbf{o}| \quad (87)$$

If the remaining gas cannot afford the code-deposit cost, i.e. $g^{**} < d$, then we also declare that an out-of-gas exception occurs and handle it as a failed contract creation attempt.

If the contract creation fails for any reason, the value of the transaction is not transferred to the aborted contract, and collateral for storing the code is not locked either. Thus we formally specify the resultant state, gas, storage limit, substate, and status code by (σ', g', A, z) as follows:

$$g' \equiv \begin{cases} 0 & \text{if } F \\ g^{**} - d & \text{otherwise} \end{cases} \quad (88)$$

$$\sigma' \equiv \begin{cases} \sigma & \text{if } F \\ \sigma^{**} \text{ except: } \sigma'[a]_c = \text{KEC}(\mathbf{o}) \wedge \sigma'[i]_o = \sigma^{**}[i]_o + c & \text{otherwise} \end{cases} \quad (89)$$

$$z \equiv \begin{cases} 1 & \text{if } F \\ 0 & \text{otherwise} \end{cases} \quad (90)$$

where $F \equiv ((\sigma^{**} = \emptyset \wedge \mathbf{o} = \emptyset) \vee g^{**} < d \vee |\mathbf{o}| > 24576)$ denotes the event that the contract creation attempt fails.

In the determination of σ' , the final body code for the newly created account is specified by the byte sequence \mathbf{o} derived from the execution of the initialization code \mathbf{i} . The status code z is an indicator of whether the contract creation succeeds.

Therefore the result of contract creation is either a successfully created new contract with its endowment and collateral for storage, or no new contract and no transfer of value or collateral at all.

Subtleties. Note that while the initialization code is executing, the newly created address exists but with no intrinsic body code. Thus any message call received by it during this time causes no code to be executed. If the initialization execution ends with a SELFDESTRUCT instruction, the matter is moot since the account will be deleted before the transaction is completed. For a normal STOP code, or if the code returned is otherwise empty, then the world-state may left with a zombie account. Only the administrator of such contract can destroy it by calling the internal contract described in section 7.2.

5.5 Message Call

The following intrinsic parameters are used when executing a message call:

- world-state σ ;
- original world-state $\tilde{\sigma}$;
- sender s ;
- original sender o ;
- recipient r ;
- storage owner i
- the account c whose code is to be executed, usually the same as recipient;
- available gas g ;
- gas price p ;
- value v ;
- input data \mathbf{d} of the call, as an arbitrary length byte array;
- the present depth of message-call/contraction-creation stack e ;
- and finally the permission to change the state w .

During the execution of message calls, the state and transaction substate may change, and finally an output data array \mathbf{o} will be generated. In case of executing transactions (generated by external controllers) the output data \mathbf{o} is ignored, however message calls (generated by internal execution process) can result further consequences due to the execution of VM-codes, especially when the message call is generated inside the execution of another message call (or transaction).

$$(\sigma', g', A, z, \mathbf{o}) \equiv \Theta(\sigma, \tilde{\sigma}, s, o, r, i, c, g, p, v, \tilde{v}, \mathbf{d}, e, w) \quad (91)$$

Note that we differentiate between the value to be transferred, v , from the value apparent in the execution context, \tilde{v} , for the DELEGATECALL instruction.

We let σ^* denote the first transitional world-state, which is the same as the original state except for the value transferred from sender s to recipient r (if $s \neq r$):

$$\sigma^*[r]_b \equiv \sigma[r]_b + v \quad \wedge \quad \sigma^*[s]_b \equiv \sigma[s]_b - v \quad (92)$$

In particular, if $\sigma[r]$ was undefined in σ , Conflux will treat it as an empty account with address r which has no code or state and zero balance and nonce. If furthermore the transferred value v is positive, the account will be created and stored in $\sigma^*[r]$. Thus the previous equation should be taken to mean:

$$\sigma^* \equiv \sigma \quad \text{except:} \quad (93)$$

$$\sigma^*[s] \equiv \begin{cases} \emptyset & \text{if } \sigma[s] = \emptyset \wedge v = 0 \\ \sigma[s] \quad \text{except: } \sigma^*[s]_b = \sigma[s]_b - v & \text{otherwise} \end{cases} \quad (94)$$

$$\sigma^*[r] \equiv \begin{cases} \alpha^0 \quad \text{except: } \sigma^*[r]_b = v & \text{if } \sigma[r] = \emptyset \wedge v \neq 0 \\ \emptyset & \text{if } \sigma[r] = \emptyset \wedge v = 0 \\ \sigma[r] \quad \text{except: } \sigma^*[r]_b = \sigma[r]_b + v & \text{otherwise} \end{cases} \quad (95)$$

The recipient's associated code \mathbf{b} , whose Keccak hash is $\sigma[r]_c$, is executed according to the execution model if the re-entrance protection is not triggered as in Section 5.5.1. Note that the pair $(\text{KEC}(\mathbf{b}), \mathbf{b})$ must be stored at some previous point, i.e. at the last update of the code hash $\sigma[r]_c$ of the recipient's account. Thus \mathbf{b} can be efficiently determined from $\sigma[r]_c$, and it is unique following the collision resistance of KECCAK.

Similar as with contract creation, if the execution halts due to an exception, then the state is reverted to the point immediately prior to balance transfer (i.e. σ) of the message call but no gas is refunded. The new state σ' after executing this message call is as follows:

$$\sigma' \equiv \begin{cases} \sigma & \text{if } \sigma^{**} = \emptyset \\ \sigma^{**} & \text{otherwise} \end{cases} \quad (96)$$

$$g' \equiv \begin{cases} 0 & \text{if } \sigma^{**} = \emptyset \wedge \mathbf{o} = \emptyset \\ g^{**} & \text{otherwise} \end{cases} \quad (97)$$

$$z \equiv \begin{cases} 1 & \text{if } \sigma^{**} = \emptyset \\ 0 & \text{otherwise} \end{cases} \quad (98)$$

where the resultant state σ^{**} and available gas remaining g^{**} , together with the accrued substate A and the output data \mathbf{o} , are determined by the code execution function Ξ evaluated on state σ^* .

$$(\sigma^{**}, g^{**}, A, \mathbf{o}) \equiv \Xi(\sigma^*, g, I) \quad (99)$$

where I contains the parameters of the execution environment as follows:

$$I_a \equiv r \quad (100)$$

$$I_o \equiv o \quad (101)$$

$$I_i \equiv i \quad (102)$$

$$I_p \equiv p \quad (103)$$

$$I_d \equiv \mathbf{d} \quad (104)$$

$$I_s \equiv s \quad (105)$$

$$I_v \equiv \tilde{v} \quad (106)$$

$$I_b \equiv \mathbf{b} \quad (107)$$

$$I_H \equiv H \quad (108)$$

$$I_e \equiv e \quad (109)$$

$$I_w \equiv w \quad (110)$$

$$I_\sigma \equiv \tilde{\sigma} \quad (111)$$

For the frequently used functionalities such as the elliptic curve public key recovery, the SHA2-256 hash scheme, and so on, we set up eight “precompiled contracts” with reserved recipient's address $r \in \{1, 2, \dots, 8\}$ (with type indicator $[0000]_2$). In the present implementation of Conflux these exceptional contracts are specified as in the latest version of Ethereum [3].

5.5.1 Re-entrance Protection

When calling a contract, Conflux virtual machine makes sure that re-entrance attack is impossible by invalidating codes to be executed in re-entrance calls.

To be specific, the Conflux virtual machine maintains a call stack and invalidates the code execution when the callee is already in the call stack but different from the caller before executing the code invoked by each message call. By requiring that the callee being different from the caller, it is still allowed to call and execute other functions in the caller's contract. Because in such cases the developer should be able to fully anticipate the execution flow and we do not consider it necessary to trigger the re-entrance protection.

If the message call is indeed re-entering some other contract in the call stack, the re-entrance protection is triggered such that the callee's code is invalidated in this message call and a "reentrancy" exception is generated. However, we remark that after returning from the re-entrance call, the changes on consumed gas and transferred value are not reverted, i.e. the state is reverted to the first transitional world-state σ^* as in (92). Here the value transfer is not reverted since it is necessary in some cases, e.g. withdrawing CFX from a contract when the transfer has to happen via a re-entrance call.

5.6 Execution Model

The execution model specifies the system state transition on input of a sequence of bytecode instructions and a small tuple of environmental data. The state transition function is formalized as a virtual state machine, which is Turing-complete except that its running time and storage space is intrinsically bounded by the limited amount of available gas and collateral for storage. For this moment we implement the well-known Ethereum Virtual Machine (EVM), and the execution model follows [3].

5.6.1 Basics

The EVM is a stack-based architecture with 256-bit word size. The stack has a maximum size of 1024 words. The memory model is a simple word-addressed byte array. The machine also has an independent storage model which is a word-addressable word array (rather than byte array for the memory). The memory is volatile and storage is steady and maintained as part of the system state. All locations in both memory and storage are initialized as zero. The program code is stored separately in a virtual ROM that is only interactable via specific instructions.

The execution of the virtual machine may reach exceptions for various reasons, including stack underflows/overflow, invalid instruction, invalid jump destination, out-of-gas and so on. Like the out-of-gas exception, the machine halts immediately and throws an exception to the execution agent, either the transaction processor or recursively the spawning execution environment, which will catch and deal with it separately.

5.6.2 Gas Consumption

The cost of execution, aka. *gas*, is charged under following circumstances:

1. the execution of instructions, where each type of instructions is assigned an intrinsic amount of gas;
2. the generation of subordinate message call or contract creation.

5.6.3 Storage Consumption

Conflux requires a fixed amount of fund, i.e. 1/16 CFX, locked as collateral during the whole lifetime of each 64B storage entry in the world-state. This fund is locked when the entry is created, and is unlocked and returned to the owner when that entry is cleared or overwritten by someone else eventually, as described in Section 6. The interest generated by the collateral is paid to miners as specified in Section 9.2. Thus the cost of storing an entry is proportional to the time length of storage usage.

The owner of the collateral of a storage entry, which is called "the owner of that entry" for simplicity, essentially records who has written the latest content of that entry. Normally the initial owner of an entry should be the sender of the transaction that causes the creation of this entry. However, in case a contract provides the collateral on behalf of the sender, the owner will be that contract instead (see Section 7.1 for details). When a storage entry is modified in the execution of a transaction, the ownership of this entry is changed, and the old owner's collateral for that entry is replaced by the new owner's collateral.

If a storage entry is cleared from the world-state, then the corresponding collateral is unlocked and returned to the owner of that entry. We remark that there is no refund to the actor who causes the clearance, which is distinct from the gas refunding policy in Ethereum [3]. Furthermore, to ensure that unlocked collateral for storage is always returned properly, Conflux does not allow destructing any smart contract with non-zero collateral for storage.

During the execution of a transaction T , the total incremental in storage usage cannot exceed T_ℓ as specified in the `storageLimit` field of T . In case more storage space is required, the execution of T would fail.

More details about collateral for storage is explained in Section 6.

5.6.4 Execution Environment

Besides the global system state σ and the amount of remaining gas g , the execution agent must provide the following important information used in the execution environment, as contained in the tuple I :

- I_a , the address of the account which owns the code that is executing.
- I_o , the address of the original sender who originated this execution.
- I_i , the address of the storage owner.
- I_p , the gas price designated by the transaction that originated this execution.
- I_d , the byte array that is the input data to this execution; in case the execution agent is a transaction T , this would be the transaction data T_d .
- I_s , the address of the account that invoked the code; in case the execution agent is a transaction T , this would be the transaction sender's address $S(T)$.
- I_v , the value, in Drip, passed to the recipient's account; in case the execution agent is a transaction T , this would be the transaction value T_v .
- I_b , the byte array of the machine code to be executed.
- I_H , the block header of the present block.
- I_e , the depth of the current message-call or contract-creation in the stack.
- I_w , the permission to make modifications to the state.
- I_σ , the original world-state right before this execution.

The state transition is defined by the execution function Ξ , which takes as input the current world-state σ , the amount of gas g , and the input I as defined above, and outputs the resultant state σ' , the remaining gas g' , the accrued substate A and the resultant output \mathbf{o} . Formally, we define it as follows:

$$(\sigma', g', A, \mathbf{o}) \equiv \Xi(\sigma, g, I) \quad (112)$$

where we recall that the accrued state A consists of the selfdestructs set A_s , the log series A_l , the touched accounts A_t , a series of addresses recording the owners of storage occupation A_o and a series of addresses recording the owners of storage release A_e (as described in Section 5.3.2):

$$A \equiv (A_s, A_l, A_t, A_o, A_e) \quad (113)$$

5.6.5 Execution Overview

The Ξ function is defined mostly following the Ethereum yellowpaper [3], except for a few instructions. For self-sufficiency we explain the definition of Ξ briefly.

In most practical implementations Ξ will be modeled as an iterative progression of the pair (σ, μ) comprising the world-state and the machine state. Formally, it can be recursively defined with a function X . This uses an iterator function O (which defines the result of a single cycle of the state machine) together with functions Z , which determines if the present state is an **exceptional halting** state of the machine, and H , specifying the output data of the instruction if and only if the present state is a **normal halting** state of the machine.

Recall that the empty sequence, denoted by ε , is not equal to the empty set, denoted by \emptyset ; this is important when interpreting the output of H , which evaluates to \emptyset when execution is to continue but a series (potentially empty) when execution should halt.

$$\Xi(\sigma, g, I) \equiv (\sigma', \mu'_g, A, \mathbf{o}) \quad (114)$$

$$(\sigma', \mu'_g, A, \dots, \mathbf{o}) \equiv X((\sigma, \mu, A^0, I)) \quad (115)$$

$$\mu_g \equiv g \quad (116)$$

$$\mu_{pc} \equiv 0 \quad (117)$$

$$\mu_m \equiv (0, 0, \dots) \quad (118)$$

$$\mu_i \equiv 0 \quad (119)$$

$$\mu_s \equiv \varepsilon \quad (120)$$

$$\mu_o \equiv \varepsilon \quad (121)$$

$$\mu_r \equiv \varepsilon \quad (122)$$

$$X((\sigma, \mu, A, I)) \equiv \begin{cases} (\emptyset, \mu, A^0, I, \emptyset) & \text{if } Z(\sigma, \mu, I) \\ (\emptyset, \mu', A^0, I, \mathbf{o}) & \text{if } w = \text{REVERT} \\ O(\sigma, \mu, A, I) \cdot \mathbf{o} & \text{if } \mathbf{o} \neq \emptyset \\ X(O(\sigma, \mu, A, I)) & \text{otherwise} \end{cases} \quad (123)$$

where

$$\mathbf{o} \equiv H(\mu, I) \quad (124)$$

$$(a, b, c, d) \cdot e \equiv (a, b, c, d, e) \quad (125)$$

$$\mu' \equiv \mu \text{ except:} \quad (126)$$

$$\mu'_g \equiv \mu_g - C(\sigma, \mu, I) \quad (127)$$

Note that, when evaluating Ξ instead of X , the fourth element I' is dropped and the remaining gas μ'_g is extracted from the resultant machine state μ' .

X is thus cycled (recursively here, but implementations are generally expected to use a simple iterative loop) until either Z becomes true indicating that the present state is exceptional and that the machine must be halted and any changes discarded or until H becomes a series (rather than the empty set) indicating that the machine has reached a controlled halt.

Machine State. The machine state μ is defined as the tuple $(g, pc, \mathbf{m}, i, \mathbf{s}, \mathbf{r})$ which are the gas available, the program counter $pc \in \mathbb{N}_{256}$, the memory contents, the active number of words in memory (counting continuously from position 0), the data stack contents and return stack contents. The memory contents $\mu_{\mathbf{m}}$ are a series of zeros of size 2^{256} . The return stack $\mu_{\mathbf{r}}$ is limited to 1023 items.

For the ease of reading, the instruction mnemonics, e.g. ADD, should be interpreted as their numeric eqdefalts; the full table of instructions and their specifics is given in Appendix D.2.

For the purposes of defining Z , H and O , we define w as the current operation to be executed:

$$w \equiv \begin{cases} I_{\mathbf{b}}[\mu_{pc}] & \text{if } \mu_{pc} < \|I_{\mathbf{b}}\| \\ \text{STOP} & \text{otherwise} \end{cases} \quad (128)$$

Furthermore, we let δ and ρ denote the fixed number of stack items removed from and pushed into the data stack $\mu_{\mathbf{s}}$ by executing an instruction. Both δ and ρ are assumed subscriptable on the instruction. Similarly we define δ^* and ρ^* for the return stack $\mu_{\mathbf{r}}$, which is only accessed when entering or returning from subroutines on JUMPSUB and RETURNSUB instructions. An instruction cost function C evaluates to the full cost, in gas, of executing the given instruction.

Exceptional Halting. The exceptional halting function Z is defined as:

$$\begin{aligned} Z(\sigma, \mu, I) \equiv & \mu_g < \mathcal{C}(\sigma, \mu, I) \\ & \vee \delta_w = \emptyset \\ & \vee \|\mu_{\mathbf{s}}\| < \delta_w \\ & \vee (w = \text{JUMP} \wedge \mu_{\mathbf{s}}[0] \notin D(I_{\mathbf{b}})) \\ & \vee (w = \text{JUMPI} \wedge \mu_{\mathbf{s}}[1] \neq 0 \wedge \mu_{\mathbf{s}}[0] \notin D(I_{\mathbf{b}})) \\ & \vee (w = \text{RETURNDATACOPY} \wedge \mu_{\mathbf{s}}[1] + \mu_{\mathbf{s}}[2] > \|\mu_{\mathbf{o}}\|) \\ & \vee \|\mu_{\mathbf{s}}\| - \delta_w + \rho_w > 1024 \\ & \vee (\neg I_w \wedge W(w, \mu)) \end{aligned} \quad (129)$$

where

$$\begin{aligned} W(w, \mu) \equiv & w \in \{\text{CREATE}, \text{CREATE2}, \text{SSTORE}, \text{SELFDESTRUCT}\} \\ & \vee (\text{LOG0} \leq w \wedge w \leq \text{LOG4}) \\ & \vee (w \in \{\text{CALL}, \text{CALLCODE}\} \wedge \mu_{\mathbf{s}}[2] \neq 0) \end{aligned} \quad (130)$$

This states that the execution is in an exceptional halting state if there is insufficient gas, if the instruction is invalid (and therefore its δ subscript is undefined), if there are insufficient stack items, if a JUMP/JUMPI destination is invalid, if the output data size $\|\mu_{\mathbf{o}}\|$ is insufficient for the copy-output-data operation specified in a RETURNDATACOPY instruction, or if the new stack size would be larger than 1024 or state modification is attempted during a static call. The astute reader will realize that this implies that no instruction can, through its execution, cause an exceptional halt.

Jump Destination Validity. We previously used D as the function to determine the set of valid jump destinations given the code that is being run. We define this as any position in the code occupied by a JUMPDEST instruction.

All such positions must be on valid instruction boundaries, rather than sitting in the data portion of PUSH* operations and must appear within the explicitly defined portion of the code (rather than in the implicitly defined STOP operations that trail it).

Formally:

$$D(\mathbf{c}) \equiv D_J(\mathbf{c}, 0) \quad (131)$$

where:

$$D_J(\mathbf{c}, i) \equiv \begin{cases} \{\} & \text{if } i \geq \|\mathbf{c}\| \\ \{i\} \cup D_J(\mathbf{c}, N(i, \mathbf{c}[i])) & \text{if } \mathbf{c}[i] = \text{JUMPDEST} \\ D_J(\mathbf{c}, N(i, \mathbf{c}[i])) & \text{otherwise} \end{cases} \quad (132)$$

where N is the next valid instruction position in the code, skipping the data of a PUSH* instruction, if any:

$$N(i, w) \equiv \begin{cases} i + w - \text{PUSH1} + 2 & \text{if } w \in [\text{PUSH1}, \text{PUSH32}] \\ i + 1 & \text{otherwise} \end{cases} \quad (133)$$

Normal Halting. The normal halting function H is defined:

$$H(\mu, I) \equiv \begin{cases} H_{\text{RETURN}}(\mu) & \text{if } w \in \{\text{RETURN}, \text{REVERT}\} \\ \varepsilon & \text{if } w \in \{\text{STOP}, \text{SELFDESTRUCT}\} \\ \emptyset & \text{otherwise} \end{cases} \quad (134)$$

The data-returning halt operations, RETURN and REVERT, have a special function H_{RETURN} . Note also the difference between the empty sequence and the empty set as discussed [here](#).

5.6.6 The Execution Cycle

Stack items are added or removed from the left-most, lower-indexed portion of the series; all other items remain unchanged:

$$O((\sigma, \mu, A, I)) \equiv (\sigma', \mu', A', I) \quad (135)$$

$$\Delta \equiv \rho_w - \delta_w \quad (136)$$

$$\|\mu'_s\| \equiv \|\mu_s\| + \Delta \quad (137)$$

$$\forall x \in [\rho_w, \|\mu'_s\| - 1] : \mu'_s[x] \equiv \mu_s[x - \Delta] \quad (138)$$

The gas is reduced by the instruction's gas cost.

$$\mu'_g \equiv \mu_g - C(\sigma, \mu, I) \quad (139)$$

For most instructions, the program counter pc increases by 1 on each cycle, except for following instructions: PUSH*, JUMP, JUMPI, JUMPSUB, RETURN SUB. The next valid instruction position for PUSH* instructions is already specified in N as in eq. (133). We assume a function J , subscripted by one instruction from $\{\text{JUMP}, \text{JUMPI}, \text{JUMPSUB}, \text{RETURN SUB}\}$, which evaluates to the according value:

$$\mu'_{\text{pc}} \equiv \begin{cases} J_{\text{JUMP}}(\mu) & \text{if } w = \text{JUMP} \\ J_{\text{JUMPI}}(\mu) & \text{if } w = \text{JUMPI} \\ J_{\text{JUMPSUB}}(\mu) & \text{if } w = \text{JUMPSUB} \\ J_{\text{RETURN SUB}}(\mu) & \text{if } w = \text{RETURN SUB} \\ N(\mu_{\text{pc}}, w) & \text{otherwise} \end{cases} \quad (140)$$

In general, we assume the memory, self-destruct set and system state do not change:

$$\mu'_m \equiv \mu_m \quad (141)$$

$$\mu'_i \equiv \mu_i \quad (142)$$

$$A' \equiv A \quad (143)$$

$$\sigma' \equiv \sigma \quad (144)$$

However, instructions do typically alter one or several components of these values. Altered components listed by instruction are noted in Appendix D, alongside values for ρ , δ , ρ^* , δ^* and a formal description of the gas requirements.

5.6.7 Difference from Ethereum

The execution function Ξ follows nearly the same definition as in Ethereum yellowpaper [3] except for a few instructions. When executing $O(\sigma, \mu, A, I) \equiv (\sigma', \mu', A, I')$ for the iterator function O which defines the result of a single cycle of the state machine, Conflux differs from Ethereum on following instructions.

Sub-call operations. Conflux has two additional parameters comparing with Ethereum: the original world-state $\tilde{\sigma}$ and the storage owner i . In sub-call operations such as CREATE, CALL, CALLCODE, DELEGATECALL, and STATICCALL, the original world-state I_σ and storage owner I_i are also passed to Λ and Θ as part of the execution environment I .

SSTORE operation. The SSTORE operation transforms (σ, A) into (σ', A') via intermediate states (σ^*, A^*) and (σ^{**}, A^{**}) as follows:

$$\sigma^* \equiv \sigma \quad \text{except:} \quad (145)$$

$$\sigma^*[I_a]_s[\mu_s[0]] \equiv \begin{cases} (\mu_s[1], I_i) & \mu_s[1] \neq 0 \\ \emptyset & \mu_s[1] = 0 \end{cases} \quad (146)$$

$$C_{\text{SSTORE}}(\sigma, \mu) \equiv G_{\text{sreset}} \quad (147)$$

$$(\sigma^{**}, A^{**}) \equiv \begin{cases} \Phi(\sigma^*, A, s_o, -64) & s_o \neq \emptyset \wedge s_o \neq s_o^* \\ (\sigma^*, A) & \text{otherwise} \end{cases} \quad (148)$$

$$(\sigma', A') \equiv \begin{cases} \Phi(\sigma^{**}, A^{**}, I, 64) & s_o^* \neq \emptyset \wedge s_o \neq s_o^* \\ (\sigma^{**}, A^{**}) & \text{otherwise} \end{cases} \quad (149)$$

where $s \equiv \sigma[I_a]_s[\mu_s[0]]$, $s^* \equiv \sigma^*[I_a]_s[\mu_s[0]]$, and Φ denotes the function such that $\Phi(\sigma, A, \alpha, n)$ updates the world-state and substate when the account α occupies n bytes ($n \in \mathbb{Z}$ can be both positive and negative). The output of $(\sigma^2, A^2) \equiv \Phi(\sigma^1, A^1, \alpha, n)$ is defined as follows:

$$\sigma^2 \equiv \sigma^1 \quad \text{except:} \quad (150)$$

$$\sigma^2[\alpha]_o \equiv \sigma^1[\alpha]_o + n \times 10^{18}/1024 \quad (151)$$

and

$$A^2 \equiv A^1 \quad \text{except:} \quad (152)$$

$$A^2_o \equiv \begin{cases} A^1_o \cdot (a, n) & n > 0 \\ A^1_o & \text{otherwise} \end{cases} \quad (153)$$

$$A^2_i \equiv \begin{cases} A^1_i \cdot (a, -n) & n < 0 \\ A^1_i & \text{otherwise} \end{cases} \quad (154)$$

In Ethereum, the cost of operation SSTORE is $G_{\text{sset}} = 20000$ gas when the storage value is set to non-zero from zero, and $G_{\text{sreset}} = 5000$ gas when the storage value is set to zero. Ethereum will also refund $R_{\text{sclear}} = 15000$ gas when the storage value is set to zero from non-zero.

In Conflux, since cost of using storage is reflected by collateral for storage, there is no need to charge space consumption in gas. Thus Conflux charged $G_{\text{sreset}} = 5000$ gas for all the SSTORE operation, regardless of the storage value, and there is no gas refund either. Furthermore, the Conflux ledger σ tracks the owner of every storage entry with non-zero value. The execution substate A records all changes on ownership of storage entries.

SELFDESTRUCT operation. When executing the SELFDESTRUCT operation on (σ, μ, A, I) , Conflux follows the steps as below:

- Apply buffered changes on the sponsor balance for storage collateral. (Recall that I_σ is part of I and it denotes the original world-state right before the execution of this transaction.)

$$\sigma^1 \equiv \sigma \quad \text{except:} \quad (155)$$

$$\sigma^1[I_a]_p[\text{col}]_b \equiv \sigma[I_a]_p[\text{col}]_b - (\sigma[I_a]_o - I_\sigma[I_a]_o) \quad (156)$$

$$A^1 \equiv A \quad (157)$$

- If the contract has non-zero collateral for storage, i.e. $\sigma[I_a]_o > 0$, the destruction process is interrupted and an *Internal Contract* exception will be generated.
- Refund the balance for code collateral to code owner. Supposing that \mathbf{p} is code for I_a ,

$$(\sigma^2, A^2) = \Phi(\sigma^1, A^1, \sigma^1[I_a]_w, -|\mathbf{p}|) \quad (158)$$

- Refund sponsor balance for gas to sponsor for gas.

$$\sigma^3 \equiv \sigma^2 \quad \text{except:} \quad (159)$$

$$\sigma^3[a]_b \equiv \sigma^2[a]_b + \sigma^2[I_a]_p[\text{gas}]_b \quad \text{where } a \equiv \sigma^2[I_a]_p[\text{gas}]_a \quad (160)$$

$$A^3 \equiv A^2 \quad (161)$$

- Refund sponsor balance for collateral to sponsor for collateral.

$$\sigma^4 \equiv \sigma^3 \quad \text{except:} \quad (162)$$

$$\sigma^4[a]_b \equiv \sigma^3[a]_b + \sigma^3[I_a]_p[\text{col}]_b \quad \text{where } a \equiv \sigma^3[I_a]_p[\text{col}]_a \quad (163)$$

$$A^4 \equiv A^3 \quad (164)$$

- The rest follows the Ethereum's destruction operation on state (σ^4, A^4) .

Subroutine operation. Ethereum introduces BEGINSUB, JUMPSUB, RETURN SUB instructions in EIP-2315, which is not listed in its yellowpaper. Conflux implements this instruction with identical behavior as Ethereum.

Substate Combination. Each time a sub-call/creation returns successfully, Ethereum accrues the substate A^+ returned from callee process to the substate A of caller process, which is denoted by $A' \equiv A \uplus A^+$.

In Conflux, $A' \equiv A \uplus A^+$ refers to $A'_s = A_s \cup A_s^+$, $A'_1 = A_1 \circ A_1^+$, $A'_t = A_t \circ A_t^+$, $A'_o = A_o \circ A_o^+$ and $A'_i = A_i \circ A_i^+$.

6. Collateral for Storage

Collateral for storage (CFS for short) mechanism is introduced in Conflux as a pricing method for the usage of storage, which is more fair and reasonable than the one-off storage fee in Ethereum. In principle, this mechanism requires a fund being locked as collateral for any occupation of storage space. The collateral is locked until the corresponding storage is freed or overwritten by someone else, and the corresponding interest generated by the locked collateral is assigned directly to miners for the maintenance of storage. Thus, the cost of storage in Conflux also depends on the duration of space occupation.

In Conflux, every entry of storage is 64B, which is exactly the size of a single key/value pair in the world-state. The required collateral for storage is proportional to the smallest multiple of 64B that are capable to cover all stored items. For every storage entry, the account that last writes to the entry is called *the owner of that storage entry*. If a storage entry is written in the execution of a contract C with sponsorship for collateral, then C is regarded as the account writing to that entry and hence becomes the owner accordingly (see Section 7.1 for more details). In the whole lifetime of a storage entry in the world-state, the owner of that entry must lock a fixed amount of CFX as collateral for the occupation of storage space. In particular, for each storage entry of size 64B the owner should lock 1/16 CFX. This price is essentially 1 CFX for 1KB space, i.e. every byte of storage requires $10^{18}/1024$ Drip.

At the time that an account α becomes the owner of a storage entry (at either creation or modification), α should lock 1/16 CFX for that entry immediately. If α has enough balance then the required collateral is locked automatically, otherwise if α does not have enough balance, the operation will fail and α cannot create or change that entry.

When a storage entry is deleted from the world-state, the corresponding 1/16 CFX collateral is unlocked and returned to the balance of that entry's owner. In case the ownership of a storage entry is changed, the old owner's 1/16 CFX collateral is unlocked, while the new owner must lock 1/16 CFX as collateral at the same time.

For convenience, we introduce the function CFS which takes an account address a and a world-state σ as input and returns the total amount of Drip's of locked collateral for storage of account a in world-state σ . In case the world-state σ is clear from context, we write $CFS(a)$ instead of $CFS(a; \sigma)$ for succinctness.

$$CFS(a) \equiv CFS(a; \sigma) \equiv \text{total number of storage bytes owned by account } a \text{ in world-state } \sigma \times \frac{10^{18}}{1024} \quad (165)$$

In particular, for a transaction T sent by $\alpha = S(T)$ (or $\alpha = T_a$ if T is calling a sponsored contract at address T_a), let σ be the world-states just before and after the execution of T , and σ' be world-state at the end of transaction execution, the **storageLimit** field T_ℓ asserts that $CFS(\alpha; \sigma') \leq CFS(\alpha; \sigma) + (10^{18}/1024) \cdot T_\ell$.

7. Internal Contracts

Conflux introduces several built-in internal contracts for better system maintenance and on-chain governance.

7.1 Sponsorship for Usage of Contracts

Conflux implements a sponsorship mechanism to subsidize the usage of smart contracts. Thus, a new account with zero balance is able to call smart contracts as long as the execution is sponsored (usually by the operator of Dapps). The built-in *SponsorControl Contract* is introduced to record the sponsorship information of smart contracts.

The SponsorControl contract keeps the following information for each user-established contract **C**:

- **sponsor for gas**: this is the account that provides the subsidy for gas consumption;
- **sponsor for collateral**: this is the account that provides the subsidy for collateral for storage;
- **sponsor balance for gas**: this is the balance of subsidy available for gas consumption;
- **sponsor balance for collateral**: this is the balance of subsidy available for collateral for storage;
- **sponsor limit for gas fee**: this is the upper bound for the gas fee subsidy paid for every sponsored transaction;
- **whitelist**: this is the list of normal accounts that are eligible for the subsidy, where a special all-zero address refers to all normal accounts. Only the contract itself has the authority to change this list.

Sponsor for gas consumption. For a contract **C** with non-empty **sponsor for gas** and a transaction **T** calling **C**, **T** is eligible for the subsidy for gas consumption if **S(T)** is in the **whitelist** of **C** and the gas fee specified by **T** is within the limit, i.e. $T_p \times T_g \leq \text{sponsor limit for gas fee}$ of **C**. The gas consumption of **T** is paid from the **sponsor balance for gas** of **C** (if it is sufficient) rather than from the sender's balance, and the execution of **T** would fail if the **sponsor balance for gas fee** cannot afford the gas consumption. In case the transaction specifies a gas fee (i.e. $T_p \times T_g$) greater than $\min\{\text{sponsor limit for gas fee}, \text{sponsor balance for gas}\}$, there is no subsidy and the sender **S(T)** should pay for the gas consumption as usual.

Sponsor for storage collateral. For a contract **C** with non-empty **sponsor for collateral** and a transaction **T** calling **C**, **T** is eligible for the subsidy for storage usage if: a) its **sender S(T)** is in the **whitelist** of **C**, and b) its **storageLimit** T_ℓ costs no more than **sponsor balance for collateral** of **C**. If **T** is eligible, then the collateral for storage incurred in the execution of **T** is deducted from **sponsor balance for collateral** of **C**, and the owner of those modified storage entries is set to **C** accordingly. In case **S(T)** is not in the **whitelist** or the **sponsor balance for collateral** cannot cover the **storageLimit**, the sender **S(T)** has to pay for storage usage from its own balance as usual.

Components. The first five items **sponsor for gas**, **sponsor for collateral**, **sponsor balance for gas**, **sponsor balance for collateral**, **sponsor limit for gas fee** are stored in account component C_p . The **whitelist** is stored in storage of the sponsor whitelist control smart contract, which has a hard-code address C_{sw} specified in section 10. If $\sigma[C_{sw}]_\alpha[\text{KEC}(\text{RLP}(\mathbf{C}, \alpha))]_v$ is non-zero, address α is in the whitelist of contract **C**. In particular, we let $\alpha_0 = 0$ be a zero address and $\sigma[C_{sw}]_s[\text{KEC}(\text{RLP}(\mathbf{C}, \alpha_0))]_v \neq 0$ denote that all valid addresses are in the whitelist of contract **C**.

7.1.1 Sponsorship Update

Both sponsorship for gas and for collateral can be updated by calling the SponsorControl contract. The current sponsors can call this contract to transfer funds to increase the sponsor balances directly, and the current sponsor for gas is also allowed to increase the **sponsor limit for gas** without transferring new funds. Other normal accounts can replace the current sponsors by calling this contract and providing more funds for sponsorship.

To replace the **sponsor for gas** of a contract **C**, the new sponsor should transfer to **C** a fund more than the current **sponsor balance for gas** of **C** and set a new value for **sponsor limit for gas fee**. The new value of **sponsor limit for gas fee** should be no less than the old sponsor's limit unless the old **sponsor balance for gas** cannot afford the old limit. Moreover, the transferred fund should be ≥ 1000 times of the new limit, so that it is sufficient to subsidize at least 1000 transactions calling **C**. If the above conditions are satisfied, the remaining **sponsor balance for gas** will be refunded to the old **sponsor for gas**, and then **sponsor balance for gas**, **sponsor for gas** and **sponsor limit for gas fee** will be updated according to the new sponsor's specification.

The replacement of **sponsor for collateral** is similar except that there is no analog of the limit for gas fee. The new sponsor should transfer to **C** a fund more than the fund provided by the current **sponsor for collateral** of **C**. Then the current **sponsor for collateral** will be fully refunded, i.e. the sum of **sponsor balance for collateral** and $\text{CFS}(\mathbf{C})$, and both collateral sponsorship fields are changed as the new sponsor's request accordingly. Note that the contract **C** is the owner of subsidized storage entries, so that the replacement of sponsorship for collateral will not affect ownership of existing storage entries.

Note: A contract account is also allowed to be a sponsor. Therefore it is possible that the sponsoring contract may be destructed before its sponsorship is replaced, in which case the receiver of sponsorship refund will be an already-destructed contract. Since the balance of such a contract is not operable (unless there is collision of KEC), it is meaningless to record that number in state and hence the refund will be burnt immediately.

7.1.2 Interfaces and exceptions

This contract provides the following four solidity interfaces:

- `set_sponsor_for_gas(address contract_addr, uint upper_bound)`
- `set_sponsor_for_collateral(address contract_addr)`
- `add_privilege(address[] mem)`
- `remove_privilege(address[] mem)`

The transferred value when calling function `set_sponsor_for_gas` and `set_sponsor_for_collateral` represents the amount of tokens that the sender (new sponsor) is willing to pay. Every contract maintains its **whitelist** by calling `add_privilege` and `remove_privilege`.

During execution of this SponsorControl contract, *Internal Contract Exception* will be triggered in the following cases:

- Invalid input format, including calling unsupported functions.
- Called from a system operation (e.g. CALLCODE, DELEGATECALL) in EVM.
- Trying to set sponsorship for an inexistent or non-contract address.
- When setting sponsor for gas or collateral, the sender is distinct from the current **sponsor** and the transferred balance does not exceed the current **sponsor balance for gas/collateral**.
- When setting sponsor for gas, the transferred balance is less than 1000 times of the new **sponsor limit for gas fee**.
- When setting sponsor for gas, the caller attempts to decrease **sponsor limit for gas fee** while the current **sponsor balance for gas** is no less than current **sponsor limit for gas fee**.

7.1.3 Gas consumption

The `set_sponsor_for_gas()` and `set_sponsor_for_collateral()` functions of the SponsorControl contract cost 10000 gas to update the sponsor information of a contract. The `add_privilege()` and `remove_privilege()` functions cost 5000 gas for each entry of membership update in the input data. Calling inexistent functions of SponsorControl contract costs 5000 gas by default. And the whole **gasLimit** is consumed in case of any exceptions such as illegal input data or wrong authentication.

7.2 Admin Management

The *AdminControl Contract* is introduced for better maintenance of other smart contracts, especially which are generated tentatively without a proper destruction routine: it records the administrator of every user-established smart contract and handles the destruction on request of corresponding administrators.

The default administrator of a smart contract **C** is the creator of **C**, i.e. the sender α of the transaction that causes the creation of **C**. The current administrator of a smart contract can transfer its authority to another *normal account* by sending a request to the AdminControl contract. Contract accounts are not allowed to be the administrator of other contracts, since this mechanism is mainly for tentative maintenance. Any long term administration with customized authorization rules should be implemented inside the contract, i.e. as a specific function that handles destruction requests.

At any time, the administrator α of an existing contract **C** has the right to request destruction of **C** by calling AdminControl. However, the request would be rejected if the collateral for storage of contract **C** is not zero, i.e. $CFS(C) > 0$, or α is not the current administrator of **C**. If α is the current administrator of **C** and $CFS(C) = 0$, then the destruction request is accepted and processed as follows:

1. the balance of **C** will be refunded to α ;
2. the **sponsor balance for gas** of **C** will be refunded to **sponsor for gas**;
3. the **sponsor balance for collateral** of **C** will be refunded to **sponsor for collateral**;
4. the internal state in **C** will be released and the corresponding collateral for storage refunded to owners;
5. the contract **C** is deleted from world-state.

The administrator of contract a is stored in account component a_a .

7.2.1 Interfaces and exceptions

This contract provides the following two solidity interfaces:

- `set_admin(address contract_addr, address admin)`
- `destroy(address contract_addr)`

This contract will trigger *Internal Contract Exception* in the following cases:

- Invalid input format, including calling unsupported functions.
- Called from a system operation (e.g. CALLCODE, DELEGATECALL) in EVM.
- Try to destroy a contract with non-zero storage collateral (the corresponding storage must be released first).

7.2.2 Gas consumption

Each function of the AdminControl contract costs 5000 gas, including inexistent functions. And the whole **gasLimit** is consumed in case of exceptions such as illegal input data or wrong authentication.

7.3 Staking Mechanism

Conflux introduces the staking mechanism for two reasons: first, staking mechanism provides a better way to charge the occupation of storage space (comparing to “pay once, occupy forever”); and second, this mechanism also helps in defining the voting power in decentralized governance.

At a high level, Conflux implements a built-in *Staking Contract* to record the staking information of all accounts. By sending a transaction to this contract, users (both external users and smart contracts) can deposit/withdraw funds, which is also called *stakes* in the contract. The interest of staked funds is issued at withdrawal, and depends on both the amount and staking period of the fund being withdrawn.

In Conflux, the staking contract keeps track of staked funds and freezing rules. For every account α the staking contract records the following:

- **staking funds:** each staking fund entry consists of the balance $v \in \mathbb{N}_{256}$ and creation time $t \in \mathbb{N}_{64}$ of a staked fund from the sender α , and the entry is cleared when the fund is completely withdrawn;
- **freezing rules:** each freezing rule entry is a combination of $(v, t) \in \mathbb{N}_{256} \times \mathbb{N}_{64}$ which promises that the total stake balance of account α must be at least v (measured in Drip) as long as the block number (as defined in **BlockNo**) does not exceed t . Expired freezing rule entries are cleared at the next update of freezing rules of the same account α .

Both kinds of entries in the staking contract requires collateral for storage, and the collateral is returned at the clearance of corresponding entries.

7.3.1 Interest Rate

The staking interest rate is currently set to 4% per year. Compound interest is implemented in the granularity of blocks.

When executing a transaction sent by account α at block **B** to withdraw a fund of value v deposited at block **B'**, the interest is calculated as follows:

$$\text{Interest issued to } \alpha = v \times \left(\frac{4\%}{63072000} \right)^T \quad (166)$$

where $T \equiv \text{BlockNo}(\mathbf{B}) - \text{BlockNo}(\mathbf{B}')$ is the staking period measured by number of blocks, and 63072000 is the expected number of blocks generated in 365 days with the target block time 0.5 seconds. Therefore after the withdrawal α 's total amount of staking funds is decreased by v , and its balance is increased by:

$$\Delta(\alpha_b) \equiv \left(1 + \left(\frac{4\%}{63072000} \right)^T \right) \cdot v \quad (167)$$

The account α only specifies the value v in its withdrawal request. The withdrawal always starts from the earliest staked fund and recursively continues to the next one until the accumulative amount is sufficient.

The same interest rate applies to collateral for storage as well, but the CFS interest is issued directly to the miners as the payment for storage usage at the generation of every new block. More details about CFS interest issuance are specified in Section 9.2.

7.3.2 Staking for Voting Power

For decentralized governance, the staking mechanism provides a way to measure the involvement and devotion of users with the new dimension of staking age.

When deciding voting power, it is fair and reasonable to take the staking time into consideration, rather than merely the amount of tokens. By relating voting power to committed staking period, the risk of being attacked is also mitigated, since the attacker must hold the tokens for a sufficiently long period to obtain enough voting power, which increases the cost of launching an attack.

For every account α , its committed staking time is recorded in the build-in staking contract in the form of **freezing rules**, where each entry $(v, t) \in \mathbb{N}_{256} \times \mathbb{N}_{64}$ is a promise that the staking balance of α must be at least v Drip until the index of block in total order (e.g. **BlockNo**) reaches t . A withdrawal request from α is invalid if any freezing rule is violated after fulfilling that request. The list of freezing rules for every account is append-only so that committed staking period cannot be canceled or shorten. However every single rule will eventually expire as the block number grows, e.g. the rule (v, t) expires at block **B** with

$\text{BlockNo}(\mathbf{B}) \geq t$. Expired freezing rule entries are cleared from state storage of the built-in staking contract at the next update of freezing rules of the same account.

Note that freezing rules are decoupled from specific staking funds, i.e. old funds can be withdrawn as long as the remaining staking balance is sufficient. Therefore, the staking contract is allowed to maintain staked funds in a first-in-first-out manner (i.e. the earliest staked fund is also first withdrawn).

The voting power of each staked token is defined in the following table:

Remaining Committed Staking Time	Voting Power
One year or more (i.e. ≥ 63072000 blocks)	1
Six months to one year (≥ 31536000 but < 63072000 blocks)	0.5
Three to six months (≥ 15768000 but < 31536000 blocks)	0.25
Less than three month (i.e. < 15768000 blocks)	0

Therefore the total voting power of each account can be easily calculated from its freezing rules as recorded in the staking contract.

7.3.3 Interfaces and exceptions

This contract provides the following three solidity interfaces:

- `deposit(uint amount)`
- `withdraw(uint amount)`
- `lock(uint amount, uint unlock_block_number)`

No value should be transferred to the Staking Contract, even when calling `deposit` or `lock` function. The Staking Contract merely moves tokens from the balance of an account to its staking list.

The execution of Staking Contract will trigger *Internal Contract Exception* in the following cases:

- Invalid input format, including calling unsupported functions.
- Called from a system operation, e.g. via `CALLCODE` or `DELEGATECALL`.
- Not enough balance for the requested operation.

7.3.4 Gas consumption

The `deposit` function of the Staking Contract costs 10000 gas plus additional 10000 gas for each entry in the current staking list, i.e. the total amount of consumed gas by the `deposit` function is $10000(\ell + 1)$ gas, where ℓ denotes the length of staking list. The `withdraw` and `lock` functions cost 10000ℓ gas each. Calling inexistent functions of the Staking Contract costs 10000 gas by default. The whole **gasLimit** is consumed in case of exceptions such as illegal input data or insufficient balance.

8. Proof of Work

Conflux applies the *Multi-point Ethash* function `MpEthash` as the Proof-of-Work function PoW. `MpEthash` is a twisted version of `Ethash` function with additional evaluation of a polynomial on multiple points. The detailed specification of this function is in Appendix E.

The `MpEthash` function is defined as:

$$\text{MpEthash}(\mathbf{H}) \equiv \text{MpEthash}(\text{KEC}(\text{RLP}(\mathbf{H}_{-n})), \mathbf{H}_n, \mathbf{d}) \equiv \{\mathbf{m}_c, \text{KEC}(\mathbf{s}_h \circ \mathbf{m}_c \circ m_p)\} \quad (168)$$

where \mathbf{d} denotes the dataset derived from \mathbf{H} as in Appendix E.3.3 and \mathbf{H}_{-n} denotes the header excluding the **mixHash** and **nonce** fields, i.e. $\mathbf{H} \equiv \mathbf{H}_{-n} \circ \mathbf{H}_x \circ \mathbf{H}_n$ since **mixHash** and **nonce** are indeed the last two fields in the structure of block header, and the fields of \mathbf{H}_{-n} are RLP-serialized according to their order in Section 3.4.

The output of `MpEthash` consists of an array with the compressed mix \mathbf{m}_c as its first item, and the Keccak-256 hash of the concatenation of the seed hash $\mathbf{s}_h \in \mathbb{B}_{512}$, the compressed mix $\mathbf{m}_c \in \mathbb{B}_{256}$, and the compressed multi-point mix $m_p \in \mathbb{B}_{32}$ as the second item. See Appendix E.4 for more details.

The first output item of `MpEthash` is used as the Proof-of-Work function PoW, and the second output item is realized as the mix-hash \mathbf{H}_x :

$$\text{PoW}(\mathbf{H}) \equiv \text{MpEthash}(\text{KEC}(\text{RLP}(\mathbf{H}_{-n})), \mathbf{H}_n, \mathbf{d})[1] = \text{KEC}(\mathbf{s}_h \circ \mathbf{m}_c \circ m_p) \quad (169)$$

$$\mathbf{H}_x \equiv \text{MpEthash}(\text{KEC}(\text{RLP}(\mathbf{H}_{-n})), \mathbf{H}_n, \mathbf{d})[0] = \mathbf{m}_c \quad (170)$$

8.1 Proof-of-Work Quality

The *proof-of-work quality* (a.k.a. *PoW quality* or simply *quality*) of a block refers to the expected amount of work spent in finding such a block. Given a block \mathbf{B} with header $\mathbf{H}(\mathbf{B})$ and the 256-bit scalar $\text{OFFSET}(\mathbf{H}) \equiv [\mathbf{H}_n(\mathbf{B})[1 \dots 127]]_2 \times 2^{128} \in \mathbb{N}_{256}$ which denotes the offset of proof-of-work validation, the quality of \mathbf{B} essentially represents the expected number of random trials to find a block \mathbf{B}' with header \mathbf{H}' satisfying that $\text{PoW}(\mathbf{H}')$ is in between of $\text{OFFSET}(\mathbf{H})$ and $\text{PoW}(\mathbf{H})$.

More specifically, the block \mathbf{B} with header $\mathbf{H}(\mathbf{B})$ has quality

$$\text{QUALITY}(\mathbf{B}) \equiv \text{QUALITY}(\mathbf{H}) \equiv \begin{cases} \lfloor 2^{256} / (\text{PoW}(\mathbf{H}) - \text{OFFSET}(\mathbf{H}) + 1) \rfloor & \text{if } \text{PoW}(\mathbf{H}) > \text{OFFSET}(\mathbf{H}) \\ \lfloor 2^{256} / (2^{256} + \text{PoW}(\mathbf{H}) - \text{OFFSET}(\mathbf{H}) + 1) \rfloor & \text{if } \text{PoW}(\mathbf{H}) < \text{OFFSET}(\mathbf{H}) \\ 2^{256} - 1 & \text{if } \text{PoW}(\mathbf{H}) = \text{OFFSET}(\mathbf{H}) \end{cases} \quad (171)$$

8.2 Difficulty Adjustment

The difficulty is adjusted according to the block generation rate in the past. More specifically, we estimate the current computing power of all miners from the number of blocks in the last 5000 epochs and the average timestamps of blocks in the beginning and ending epochs, and then set the target difficulty for the next 5000 epochs such that the expected block generation rate should be roughly one block per 0.5 seconds.

Formally, for $0 \leq j \leq 5000$, the target difficulty of a block at height j is set to $\mathbf{d}_0 \equiv 5 \times 10^6 = 5000000$; for any positive integer $i \geq 1$, the target difficulty of blocks at height $j \in [5000i + 1, 5000i + 5000]$ is set to $\mathbf{d}_i \in \mathbb{N}_{256}$ such that

$$\mathbf{d}_i \equiv \begin{cases} \lfloor \mathbf{d}_{i-1} \times 1.5 \rfloor & \text{if } \mathbf{d}'_i > \mathbf{d}_{i-1} \times 1.5 \\ \lceil \mathbf{d}_{i-1} \times 0.5 \rceil & \text{if } 5000000 \leq \mathbf{d}'_i < \mathbf{d}_{i-1} \times 0.5 \\ 5000000 & \text{if } \mathbf{d}'_i < 5000000 \\ \mathbf{d}'_i & \text{otherwise } (\mathbf{d}_{i-1} \times 0.5 \leq \mathbf{d}'_i \leq \mathbf{d}_{i-1} \times 1.5) \end{cases} \quad (172)$$

where $\mathbf{d}'_i \in \mathbb{N}_{256}$ is the estimation of ideal target difficulty defined as follows

$$\mathbf{d}'_i \equiv \mathbf{d}_{i-1} \times 5000000 \times \left(\sum_{j=5000(i-1)+1}^{5000i} |\text{EPOCH}_j| - 1 \right) / \left(\mathbf{H}(\mathbf{B}^{(5000i)})_s - \min_{5000(i-1) \leq j < 5000i \wedge \mathbf{H}(\mathbf{B}^{(j)})_s \neq 0} \{ \mathbf{H}(\mathbf{B}^{(j)})_s \} \right) \quad (173)$$

where for every $k \in \mathbb{N}$, EPOCH_k denotes the set of *fully valid* blocks in the k -th epoch and $\mathbf{B}^{(k)}$ denotes the pivot block in EPOCH_k . In the above formula the total number of blocks in last 5000 epochs is decreased by 1, which leads to an unbiased estimation of block generation rate.

Note that a single block \mathbf{B} may not have a global view. Indeed, the best it could do is to compute the target difficulty \mathbf{d}_i from its local view of blocks in $\text{PAST}(\mathbf{B})$. In particular, a block \mathbf{B} at height $h \equiv \mathbf{H}(\mathbf{B})_h$ should have target difficulty

$$\mathbf{H}(\mathbf{B})_d \equiv \begin{cases} \mathbf{d}_0 & h = 0 \\ \mathbf{d}_{\lfloor \frac{h-1}{5000} \rfloor} & h > 0, \mathbf{d}_{\lfloor \frac{h-1}{5000} \rfloor} \text{ is calculated with respect to } \text{PAST}(\mathbf{B}) \end{cases} \quad (174)$$

Epoch difficulty. As soon as all nodes agree on the pivot block $\mathbf{B}^{(k)}$ at the k -th epoch EPOCH_k , we can uniquely define the target difficulty of EPOCH_k as the target difficulty of $\mathbf{B}^{(k)}$. Formally,

$$\mathbf{d}_{\text{EPOCH}_k} \equiv \mathbf{H}(\mathbf{B}^{(k)})_d \quad (175)$$

where $\mathbf{H}(\mathbf{B}^{(k)})_d$ is the **difficulty** field in $\mathbf{B}^{(k)}$'s header and it equals to $\mathbf{d}_{\lfloor \frac{k-1}{5000} \rfloor}$ derived from the past view of $\mathbf{B}^{(k)}$.

9. Incentive Mechanism

Conflux miners get paid by Conflux coins from two sources: the newly minted Conflux coins as block award, and the fees paid by transaction senders. In this section we specify the mechanism design for incentivizing Conflux miners. The adaptive weight introduced by the GHASt rule only affects the distribution of the first part of block award.

9.1 Base Block Award

The amount of coins issued to miners in every block is set in accordance to a global parameter which follows the mining schedule. We refer to the global parameter as the *base block award* or simply *base award*, and denote it by R_{base} .

The base block award starts at $R_{base}(\mathbf{G}) = 11.3$ CFX per block and it decreases by 4.2% every 15768000 blocks (i.e. 91.25 days in expectation) for 630720000 blocks (i.e. roughly 10 years). Eventually the annual inflation rate of mining issuance is below 2 percent.

For every pivot block \mathbf{B} , the base award is defined as follows:

$$R_{base}(\mathbf{B}) \equiv \begin{cases} 11.3 \times 0.958^{\lfloor |\text{PAST}(\mathbf{B})| / 15768000 \rfloor} & \text{if } |\text{PAST}(\mathbf{B})| < 630720000 \\ 2.03 & \text{if } |\text{PAST}(\mathbf{B})| \geq 630720000 \end{cases} \quad (176)$$

For every non-pivot block \mathbf{B} , the base award $R_{base}(\mathbf{B})$ of \mathbf{B} equals to the base award of the pivot block of the epoch that \mathbf{B} belongs to, i.e.

$$R_{base}(\mathbf{B}) \equiv R_{base}(\text{PIVOT}(\mathbf{B}))$$

Based on $R_{base}(\mathbf{B})$, Conflux defines the the actual block award issued to the author of block \mathbf{B} with adjustments as described in the rest of Section 9.1.

9.1.1 Anti-cone Penalty

For every block \mathbf{B} , we recall that a block \mathbf{B}' is in the anti-cone of \mathbf{B} if there is no directed path between \mathbf{B}' and \mathbf{B} , which means the chronological order of these two blocks is not reflected by the underlying Tree-Graph. For every given Tree-Graph \mathbf{G} , let $\mathcal{A}(\mathbf{B}; \mathbf{G})$ denote the set of all anti-cone blocks of $\mathbf{B} \in \mathbf{G}$ that appear no later than 10 epochs after⁵ the epoch where \mathbf{B} resides in. When the Tree-Graph \mathbf{G} is clear from context, we write $\mathcal{A}(\mathbf{B})$ instead of $\mathcal{A}(\mathbf{B}; \mathbf{G})$ for short. Formally,

$$\mathcal{A}(\mathbf{B}) \equiv \mathcal{A}(\mathbf{B}; \mathbf{G}) \equiv \{ \mathbf{B}' \in \mathbf{G} \mid \mathbf{B} \notin \text{PAST}(\mathbf{B}') \wedge \mathbf{B}' \notin \text{PAST}(\mathbf{B}) \wedge H(\text{PIVOT}(\mathbf{B}'))_h \leq H(\text{PIVOT}(\mathbf{B}))_h + 10 \} \quad (177)$$

In other words, let \mathbf{B}^{10} be the pivot block at height $H(\mathbf{B}^{10})_h = H(\text{PIVOT}(\mathbf{B}))_h + 10$, then

$$\mathcal{A}(\mathbf{B}) \equiv \mathcal{A}(\mathbf{B}; \mathbf{G}) \equiv \text{PAST}(\mathbf{B}^{10}) \setminus (\text{PAST}(\mathbf{B}) \cup \text{FUTURE}(\mathbf{B}; \mathbf{G}) \cup \{ \mathbf{B} \}) \quad (178)$$

The *anti-cone penalty factor* of \mathbf{B} is defined as

$$\text{AF}(\mathbf{B}) \equiv \max \left\{ 0, 1 - \left(\frac{\text{Weight}(\mathcal{A}(\mathbf{B})) / \mathbf{d}_{\text{EPOCH}(\mathbf{B})}}{\gamma} \right)^2 \right\} \quad (179)$$

where $\gamma \equiv 100$ is a fixed constant and $\text{Weight}(\mathcal{A}(\mathbf{B})) \equiv \sum_{\mathbf{B}' \in \mathcal{A}(\mathbf{B})} \text{Weight}(\mathbf{B}')$ refers to the total adapted weight of blocks in the anti-cone set $\mathcal{A}(\mathbf{B})$. We remark that $\text{Weight}(\mathcal{A}(\mathbf{B})) / \mathbf{d}_{\text{EPOCH}(\mathbf{B})}$ is the equivalent number of blocks in the anti-cone of \mathbf{B} , which corresponds to the portion of computing power in \mathbf{B} 's anti-cone.

This anti-cone penalty factor is introduced to incentivize inclusion of referee blocks as well as fast propagation. It also punishes withholding attacks when the blocks are not broadcast immediately. There is no additional award for referencing referee blocks, nor discount in block award for non-pivot blocks.

9.1.2 Base Factor

For convenience, we introduce the *base factor* $\text{BF}(\mathbf{B})$ to indicate whether the author of \mathbf{B} is eligible to receive any award.

If a block \mathbf{B} in EPOCH_k has a lower target difficulty, i.e. $\mathbf{B}_d < \mathbf{d}_{\text{EPOCH}_k}$, then we decide the base award of \mathbf{B} by its block quality $\text{QUALITY}(\mathbf{B})$: it gets normal base award if the block quality $\text{QUALITY}(\mathbf{B})$ reaches the epoch's target difficulty $\mathbf{d}_{\text{EPOCH}_k}$, and zero base award $R_{base}(\mathbf{B}) \equiv 0$ in case the quality $\text{QUALITY}(\mathbf{B})$ does not meet $\mathbf{d}_{\text{EPOCH}_k}$. Note that the expected base award is effectively the same as setting $R_{base}(\mathbf{B}) \equiv \frac{\mathbf{B}_d}{\mathbf{d}_{\text{EPOCH}_k}} \cdot R_{base}(\text{EPOCH}_k)$.

If a block \mathbf{B} is partially valid, blamed, or has a large anti-cone, then the author of \mathbf{B} must have made some mistake and hence he is not eligible for any award.

Thus, the base factor $\text{BF}(\mathbf{B})$ of block \mathbf{B} is defined as

$$\text{BF}(\mathbf{B}) \equiv \begin{cases} 1 & \mathbf{B} \text{ is valid and } \text{AF}(\mathbf{B}) > 0, \text{ not blamed, and satisfies the target difficulty of } \text{EPOCH}_k \text{ (which requires} \\ & \text{QUALITY}(\mathbf{B}) \geq 250 \cdot \mathbf{d}_{\text{EPOCH}_k} \text{ if } \text{Adaptive}(\mathbf{B}) = \text{True or } \text{QUALITY}(\mathbf{B}) \geq \mathbf{d}_{\text{EPOCH}_k} \text{ if } \text{Adaptive}(\mathbf{B}) = \text{False)} \\ 0 & \text{otherwise (} \mathbf{B} \text{ is partially valid, } \text{AF}(\mathbf{B}) = 0, \text{ blamed, or } \text{QUALITY}(\mathbf{B}) \text{ does not satisfy the requirement)} \end{cases} \quad (180)$$

⁵If \mathbf{B} is not on the pivot chain in \mathbf{G} , then $\mathcal{A}(\mathbf{B}; \mathbf{G})$ also contains blocks appearing in earlier epochs but not referenced by \mathbf{B} .

9.1.3 Actual Block Award to Miners

Taking all the discounts and adjustments into account, the block award assigned to the author of B is defined as follows:

$$R_{block}(B) \equiv AF(B) \cdot BF(B) \cdot R_{base}(B) \quad (181)$$

Remark: A non-pivot block B_1 may receive a higher block award than the pivot block B_2 in the same epoch, in case $Weight(\mathcal{A}(B_1)) < Weight(\mathcal{A}(B_2))$ and hence $AF(B_1) > AF(B_2)$.

9.2 Storage Maintenance Reward

Miners receive interest generated by collateral for storage, as payment to the cost of occupying storage space in the world-state. More specifically, the CFS interest generated by all blocks in each epoch is redistributed to authors of blocks in the epoch with respect to their actual mining block award. In particular, the CFS interest assigned to the author of block B is calculated as follows:

$$R_{storage}(B) \equiv \sum_{B' \in EPOCH(B)} \left(\sum_{a \in \mathbb{B}_{160}} CFS(a; \sigma(B')) \times \frac{4\%}{63072000} \right) \times \frac{R_{block}(B)}{\sum_{B' \in EPOCH(B)} R_{block}(B')}$$

where $\sigma(B')$ denotes the world-state at the beginning of the execution of transactions in block B' , $\sum_{a \in \mathbb{B}_{160}} CFS(a; \sigma(B'))$ is the total CFS in B' , 4% is the annual interest rate and 63072000 is the (expected) number of blocks in one year, and hence the value in parenthesis is the CFS interest generated by B' ; and the distribution of CFS interest in $EPOCH(B)$ is proportional to actual block awards $R_{block}(B)$ as defined in Section 9.1.3.

9.3 Transaction Fee Reward

If a transaction T is first executed in the i -th epoch $EPOCH_i$, then the transaction fee (for purchasing the consumed gas) of T is divided between all blocks that *properly include* T . Here “a block B properly includes a transaction T ” means that: $T \in B$ and B belongs to $EPOCH_i$ (the epoch that T is executed for the first time).

The transaction fee is distributed proportionally to the binary base factors of blocks as defined in (180). In particular, if the transaction T is exclusively packed in blocks with zero base factor, the transaction fee is burnt although the transaction will still be processed.

For every transaction $T \in \mathcal{B}_{TS}$, the actually charged transaction fee is $Gas_{used}(T) \times T_p$, where T_p is the gas price specified in T and $Gas_{used}(T)$ denotes the consumed gas as in Section 5.1. Recalling that $BF(B)$ is a binary function respecting to the validity of B , the transaction fee assigned to B is defined as follows:

$$R_{fee}(B) \equiv \sum_{T: B \text{ properly includes } T} T_p \cdot Gas_{used}(T) \cdot \frac{BF(B)}{\sum_{B': B' \text{ properly includes } T} BF(B')} \quad (182)$$

9.3.1 Why not distributing transaction fees among all blocks in that epoch?

One may suggest that the transaction fee of T should be shared by all valid blocks in that epoch, rather than among blocks that properly include T as described in (182). In what follows we show that our current implementation has several advantages:

- **For security and incentive compatibility:** the first priority of the incentive mechanism design is to guarantee that every rational participant will behave honestly, i.e. they should respect the consensus protocol and reference all the blocks they have observed. However, the mechanism of sharing transaction fee may bring incentives that prevent the author of a block referencing other blocks.

For example, if there is a transaction T with a considerable fee, miners may be willing to monopolize that fee even if suffering some punishment caused by a larger anti-cone. In particular, the author who packs T into a new block B would prefer not to share the transaction fee of T with others, especially when this fee is much higher than the anti-cone punishment caused by ignoring other blocks that are eligible to share the fee of T .

If the fee of T is to be shared with all other blocks in the same epoch, the author of B would *be hostile to all other unreferenced blocks*, and hence they get incentives to ignore those blocks by shirking all responsibility to network latency. Therefore, by manipulating transaction fees and causing such intentional ignorance, an attacker is able to effectively launch a partition attack.

If the fee of T is to be shared only among blocks including T , the author of B may still want to ignore other blocks with T . However, the difference is that the author of B would not be hostile to blocks without T , since he does not have to

share the transaction fee of T with them. As a result, the author of B will be open to reference other observed blocks without T in B . Furthermore, referencing blocks with T in any later epoch is also safe, even if there are new transactions (other than T) with significant fees. Thus by manipulating transaction fees the attacker could merely cause a slightly longer latency instead of a significant partition.

In conclusion, sharing transaction fee of T only among blocks including T provides a stronger incentive of referencing other blocks honestly.

- **For efficiency:** the current design better discourages “free riders” who only mines on empty blocks and hence saves the effort of maintaining storage states and executing transactions. Since by producing empty blocks, those miners would lose the transaction fees completely, rather than receiving an average revenue of total fees in that epoch.
- **For fairness:** the current design indeed implements a tailored version of Shapley value, which is a fair distribution of total gains well-known in cooperative game theory.

9.4 Final Reward to Miners

The final mining reward of a block B will be added to the block author’s account as specified in the **author** field $H(B)_a$. Since the anti-cone of B may contain blocks up to 10 epochs after the EPOCH of B , the reward assigned to B effects at the end of 12 epochs after the EPOCH of B , where the balance of B_a is updated. For example, if B appears in $EPOCH_i$, then the account B_a receives the mining reward at the end of $EPOCH_{i+12}$. The total mining reward of B is calculated as follows:

$$R(B) \equiv R_{block}(B) + R_{storage}(B) + R_{fee}(B) \tag{183}$$

In particular, note that $AF(B) = 0$ implies $BF(B) = 0$ and $R_{block}(B) = R_{storage}(B) = R_{fee}(B) = 0$. Thus $R(B) = 0$ as long as B has a large anti-cone such that $AF(B) = 0$.

10. Concrete Protocol Implementation

Concretely, we set the following parameters for Conflux.

Note that the numbers here are only for the most recent testnet and may change in the future.

Parameter	Value
Block time	0.5 s
Maximum block size bound	200 KB
Starting coinbase award	11.3 CFX
Starting difficulty (d_0)	$5 \times 10^6 = 5000000$
Starting block gas limit	$3 \times 10^7 = 30000000$
Anti-cone penalty factor (γ)	100
Deferred execution	5 epochs
Mining reward freezing time	12 epochs
AdminControl Contract Address	0x088800
SponsorControl Contract Address	0x08880001
Staking Contract Address	0x08880002

In Conflux we use KEC as the collision-resistant hash function unless otherwise explicitly specified.

For authentication in the current version of Conflux, we use the same recoverable ECDSA signature scheme as in Ethereum [3]. This method utilizes the SECP-256k1 curve.

References

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Appendix A. Checklist for porting EVM contract to Conflux

The Ethereum contract is also a valid Conflux contract. So Ethereum contracts can be ported to Conflux easily and have almost same execution results. But notice that Conflux may have different behavior in the following points:

- **Gas used and refund:** Conflux requires less gas in SSTORE operation but no longer refunds resetting storage and contract destruction.
- **Gas fee refund:** Conflux will refund at most 1/4 of gas limit. So try to provide an accurate estimation for gas limit before signing transactions.
- **Contract address:** Conflux uses a different way to compute address for normal account from public key and compute contract address in contract creation. (See equation (1) and (69) for details.) The contract developers usually don't need to handle this difference.
- **Contract address conflict:** If the contract address has existed before contract creation, Conflux will abort the contract creation. This is different with the behavior in Ethereum.
- **Collateral for storage:** Conflux requires collateral for storage. Please make sure there is enough balance for storage collateral.

Appendix B. Difference between Ethereum and Conflux

	Ethereum	Conflux	
(Virtual Machine and transaction execution)			
Address type	indistinguishable for all accounts	distinct prefixes for normal (non-contract) account, <i>Solidity</i> contracts, and reserved contracts (a.k.a. “precompiled contracts”)	section 3.1
Transaction field	–	added chainID , storageLimit and epochHeight	section 3.3
Gas consumption and refunding	all unused gas is refundable	at most a quarter of gasLimit	section 5.1
	full gas fee charged if execution fails on any exception	no gas fee when exception is not caused by the sender	section 5.3.1
Cost of storage	one-off gas fee	gas fee + collateral	section 5.6.3
	SSTORE costs 5000 or 20000 gas depending on the effect of executing this instruction, may cause a refund of 15000 gas for clearing a storage value	SSTORE costs $G_{sset} = 5000$ gas and every 64B storage costs 1/16 CFX for collateral (locked until the storage is overwritten or released)	section 6
Transaction validation	any invalid transaction leads to the whole block being invalid	invalid transactions are skipped, while other transactions in the same block can still be valid	section 4.2.5
	a transaction is invalid if sender’s balance cannot afford the up-front payment for transferred value and gas fee (indeed the whole block will be invalid)	the transaction is valid if it satisfies all other assertions, but the execution fails immediately because of insufficient balance for the up-front payment (sender’s nonce is increased and gas fee is charged)	section 5.2
	sender must pay transaction fee from his own balance (sender’s balance cannot be zero)	a sponsor may pay for the cost of calling a smart contract (sender’s balance can be zero)	section 7.1
	validity of a transaction cannot depend on current time or height	a transaction is only valid in a specified window of epochs	section 3.3
	no check on recipient’s address	recipient address must have a valid type (i.e. normal account, <i>Solidity</i> contract, or reserved contract)	section 3.1
	Contract creation	the address of contract created by CREATE does not depend on the initialization code CREATE costs $G_{create} = 32000$, regardless initialization code length on address conflict, reset contract but inherit the balance	the address of contract created by both CREATE and CREATE2 depends on the initialization code CREATE costs the same as CREATE2 on address conflict, abort the contract creation
Contract destruction	only by SELFDESTRUCT	destruction may effect on request of the contract’s administrator (via the AdminControl contract)	section 7.2
Internal Contract	–	cannot be invoked by system operation, i.e. via CALLCODE or DELEGATECALL	section 7
BLOCKHASH	get the hash of one of the 256 most recent complete blocks	get the hash of the last block, return zero if querying other blocks	appendix D.2
CHAINID	EIP-1344	get the Conflux chain ID (503)	appendix D.2

Appendix C. Fee Schedule

The fee schedule G is a tuple of 35 scalar values corresponding to the relative costs, in gas, of a number of abstract operations that a transaction may effect.

Name	Value	Description*
G_{zero}	0	Nothing paid for operations of the set W_{zero} .
G_{base}	2	Amount of gas to pay for operations of the set W_{base} .
$G_{verylow}$	3	Amount of gas to pay for operations of the set $W_{verylow}$.
G_{low}	5	Amount of gas to pay for operations of the set W_{low} .
G_{mid}	8	Amount of gas to pay for operations of the set W_{mid} .
G_{high}	10	Amount of gas to pay for operations of the set W_{high} .
$G_{extcode}$	700	Amount of gas to pay for an EXTCODESIZE operation.
$G_{extcodehash}$	400	Amount of gas to pay for an EXTCODEHASH operation.
$G_{balance}$	400	Amount of gas to pay for a BALANCE operation.
G_{sload}	200	Paid for a SLOAD operation.
$G_{jumpdest}$	1	Paid for a JUMPDEST operation.
G_{sset}	5000	Paid for an SSTORE operation.
$R_{selfdestruct}$	24000	Refund given (added into refund counter) for self-destructing an account.
$G_{selfdestruct}$	5000	Amount of gas to pay for a SELFDESTRUCT operation.
G_{create}	32000	Paid for a CREATE operation.
$G_{codedeposit}$	200	Paid per byte for a CREATE operation to succeed in placing code into state.
G_{call}	700	Paid for a CALL operation.
$G_{callvalue}$	9000	Paid for a non-zero value transfer as part of the CALL operation.
$G_{callstipend}$	2300	A stipend for the called contract subtracted from $G_{callvalue}$ for a non-zero value transfer.
$G_{newaccount}$	25000	Paid for a CALL or SELFDESTRUCT operation which creates an account.
G_{exp}	10	Partial payment for an EXP operation.
$G_{expbyte}$	50	Partial payment when multiplied by $\lceil \log_{256}(exponent) \rceil$ for the EXP operation.
G_{memory}	3	Paid for every additional word when expanding memory.
$G_{txcreate}$	32000	Paid by all contract-creating transactions after the <i>Homestead</i> transition.
$G_{txdatazero}$	4	Paid for every zero byte of data or code for a transaction.
$G_{txdatanonzero}$	68	Paid for every non-zero byte of data or code for a transaction.
$G_{transaction}$	21000	Paid for every transaction.
G_{log}	375	Partial payment for a LOG operation.
$G_{logdata}$	8	Paid for each byte in a LOG operation's data.
$G_{logtopic}$	375	Paid for each topic of a LOG operation.
G_{sha3}	30	Paid for each SHA3 operation.
$G_{sha3word}$	6	Paid for each word (rounded up) for input data to a SHA3 operation.
G_{copy}	3	Partial payment for *COPY operations, multiplied by words copied, rounded up.
$G_{blockhash}$	20	Payment for BLOCKHASH operation.
$G_{quaddivisor}$	20	The quadratic coefficient of the input sizes of the exponentiation-over-modulo precompiled contract.

Appendix D. Virtual Machine Specification

D.1 Gas Cost

Recalling that w denotes the current operation to be executed as in (128):

$$w \equiv \begin{cases} I_b[\mu_{pc}] & \text{if } \mu_{pc} < \|I_b\| \\ \text{STOP} & \text{otherwise} \end{cases}$$

The general gas cost function, C , is defined as:

$$C(\sigma, \mu, I) \equiv C_{mem}(\mu'_i) - C_{mem}(\mu_i) + \begin{cases} G_{sset} & \text{if } w = \text{SSTORE} \\ G_{exp} & \text{if } w = \text{EXP} \wedge \mu_s[1] = 0 \\ G_{exp} + G_{expbyte} \times (1 + \lfloor \log_{256}(\mu_s[1]) \rfloor) & \text{if } w = \text{EXP} \wedge \mu_s[1] > 0 \\ G_{verylow} + G_{copy} \times \lceil \mu_s[2] \div 32 \rceil & \text{if } w = \text{CALLDATACOPY} \vee \\ & \text{CODECOPY} \vee \text{RETURNDATACOPY} \\ G_{extcode} + G_{copy} \times \lceil \mu_s[3] \div 32 \rceil & \text{if } w = \text{EXTCODECOPY} \\ G_{log} + G_{logdata} \times \mu_s[1] & \text{if } w = \text{LOG0} \\ G_{log} + G_{logdata} \times \mu_s[1] + G_{logtopic} & \text{if } w = \text{LOG1} \\ G_{log} + G_{logdata} \times \mu_s[1] + 2G_{logtopic} & \text{if } w = \text{LOG2} \\ G_{log} + G_{logdata} \times \mu_s[1] + 3G_{logtopic} & \text{if } w = \text{LOG3} \\ G_{log} + G_{logdata} \times \mu_s[1] + 4G_{logtopic} & \text{if } w = \text{LOG4} \\ C_{CALL}(\sigma, \mu) & \text{if } w = \text{CALL} \vee \text{CALLCODE} \vee \\ & \text{DELEGATECALL} \\ C_{SELFDSTRUCT}(\sigma, \mu) & \text{if } w = \text{SELFDSTRUCT} \\ G_{create} + G_{sha3word} \times \lceil \mu_s[2] \div 32 \rceil & \text{if } w = \text{CREATE} \\ G_{create} + G_{sha3word} \times \lceil \mu_s[2] \div 32 \rceil & \text{if } w = \text{CREATE2} \\ G_{sha3} + G_{sha3word} \times \lceil \mu_s[1] \div 32 \rceil & \text{if } w = \text{SHA3} \\ G_{jumpdest} & \text{if } w = \text{JUMPDEST} \\ G_{sload} & \text{if } w = \text{SLOAD} \\ G_{zero} & \text{if } w \in W_{zero} \\ G_{base} & \text{if } w \in W_{base} \\ G_{verylow} & \text{if } w \in W_{verylow} \\ G_{low} & \text{if } w \in W_{low} \\ G_{mid} & \text{if } w \in W_{mid} \\ G_{high} & \text{if } w \in W_{high} \\ G_{extcode} & \text{if } w = \text{EXTCODESIZE} \\ G_{extcodehash} & \text{if } w = \text{EXTCODEHASH} \\ G_{balance} & \text{if } w = \text{BALANCE} \\ G_{blockhash} & \text{if } w = \text{BLOCKHASH} \end{cases} \quad (184)$$

where:

$$C_{mem}(a) \equiv G_{memory} \cdot a + \left\lfloor \frac{a^2}{512} \right\rfloor \quad (185)$$

with C_{CALL} , $C_{SELFDSTRUCT}$ and C_{SSTORE} as specified in the appropriate section below. We define the following subsets of instructions:

$$W_{zero} = \{\text{STOP, RETURN, REVERT}\}$$

$$W_{base} = \{\text{ADDRESS, ORIGIN, CALLER, CALLVALUE, CALLDATASIZE, CODESIZE, GASPRICE, COINBASE, TIMESTAMP, NUMBER, DIFFICULTY, GASLIMIT, RETURNDATASIZE, POP, PC, MSIZE, GAS, CHAINID, BEGINSUB}\}$$

$$W_{verylow} = \{\text{ADD, SUB, NOT, LT, GT, SLT, SGT, EQ, ISZERO, AND, OR, XOR, BYTE, SHL, SHR, SAR, CALLDATALOAD, MLOAD, MSTORE, MSTORE8, PUSH*, DUP*, SWAP*}\}$$

$$W_{low} = \{\text{MUL, DIV, SDIV, MOD, SMOD, SIGNEXTEND, SELFBALANCE, RETURNSUB}\}$$

$$W_{mid} = \{\text{ADDMOD, MULMOD, JUMP}\}$$

$$W_{high} = \{\text{JUMPI, JUMPSUB}\}$$

Note the memory cost component, given as the product of G_{memory} and the maximum of 0 & the ceiling of the number of words in size that the memory must be over the current number of words, μ_i in order that all accesses reference valid memory whether for read or write. Such accesses must be for non-zero number of bytes.

Referencing a zero length range (e.g. by attempting to pass it as the input range to a CALL) does not require memory to be extended to the beginning of the range. μ'_i is defined as this new maximum number of words of active memory; special-cases are given where these two are not equal.

Note also that C_{mem} is the memory cost function (the expansion function being the difference between the cost before and after). It is a polynomial, with the higher-order coefficient divided and floored, and thus linear up to 724B of memory used, after which it costs substantially more.

While defining the instruction set, we defined the memory-expansion for range function, M , thus:

$$M(s, f, l) \equiv \begin{cases} s & \text{if } l = 0 \\ \max(s, \lceil (f+l) \div 32 \rceil) & \text{otherwise} \end{cases} \quad (186)$$

Another useful function is “all but one 64th” function L defined as:

$$L(n) \equiv n - \lfloor n/64 \rfloor \quad (187)$$

D.2 Instruction Set

As previously specified in Section 5.6, these definitions take place in the final context there. In particular we assume O is the EVM state-progression function and define the terms pertaining to the next cycle’s state (σ', μ') such that:

$$O(\sigma, \mu, A, I) \equiv (\sigma', \mu', A', I) \quad \text{with exceptions, as noted} \quad (188)$$

Here given are the various exceptions to the state transition rules given in Section 5.6 specified for each instruction, together with the additional instruction-specific definitions of J and C . For each instruction, also specified is ρ , the additional items placed on the data stack, and δ , the items removed from data stack, as defined in Section 5.6. For subroutine instructions, further specified is ρ^* , the additional items pushed into the return stack, and δ^* , the items removed from return stack, as defined in Section 5.6.

0s: Stop and Arithmetic Operations

All arithmetic is modulo 2^{256} unless otherwise noted. The zero-th power of zero 0^0 is defined to be one.

Value	Mnemonic	δ	ρ	Description
0x00	STOP	0	0	Halts execution.
0x01	ADD	2	1	Addition operation. $\mu'_s[0] \equiv \mu_s[0] + \mu_s[1]$
0x02	MUL	2	1	Multiplication operation. $\mu'_s[0] \equiv \mu_s[0] \times \mu_s[1]$
0x03	SUB	2	1	Subtraction operation. $\mu'_s[0] \equiv \mu_s[0] - \mu_s[1]$
0x04	DIV	2	1	Integer division operation. $\mu'_s[0] \equiv \begin{cases} 0 & \text{if } \mu_s[1] = 0 \\ \lfloor \mu_s[0] \div \mu_s[1] \rfloor & \text{otherwise} \end{cases}$
0x05	SDIV	2	1	Signed integer division operation (truncated). $\mu'_s[0] \equiv \begin{cases} 0 & \text{if } \mu_s[1] = 0 \\ -2^{255} & \text{if } \mu_s[0] = -2^{255} \wedge \mu_s[1] = -1 \\ \text{sgn}(\mu_s[0] \div \mu_s[1]) \lfloor \mu_s[0] \div \mu_s[1] \rfloor & \text{otherwise} \end{cases}$ Where all values are treated as two's complement signed 256-bit integers. Note the overflow semantic when -2^{255} is negated.
0x06	MOD	2	1	Modulo remainder operation. $\mu'_s[0] \equiv \begin{cases} 0 & \text{if } \mu_s[1] = 0 \\ \mu_s[0] \bmod \mu_s[1] & \text{otherwise} \end{cases}$
0x07	SMOD	2	1	Signed modulo remainder operation. $\mu'_s[0] \equiv \begin{cases} 0 & \text{if } \mu_s[1] = 0 \\ \text{sgn}(\mu_s[0]) (\mu_s[0] \bmod \mu_s[1]) & \text{otherwise} \end{cases}$ Where all values are treated as two's complement signed 256-bit integers.
0x08	ADDMOD	3	1	Modulo addition operation. $\mu'_s[0] \equiv \begin{cases} 0 & \text{if } \mu_s[2] = 0 \\ (\mu_s[0] + \mu_s[1]) \bmod \mu_s[2] & \text{otherwise} \end{cases}$ All intermediate calculations of this operation are not subject to the 2^{256} modulo.
0x09	MULMOD	3	1	Modulo multiplication operation. $\mu'_s[0] \equiv \begin{cases} 0 & \text{if } \mu_s[2] = 0 \\ (\mu_s[0] \times \mu_s[1]) \bmod \mu_s[2] & \text{otherwise} \end{cases}$ All intermediate calculations of this operation are not subject to the 2^{256} modulo.
0x0a	EXP	2	1	Exponential operation. $\mu'_s[0] \equiv \mu_s[0]^{\mu_s[1]}$
0x0b	SIGNEXTEND	2	1	Extend length of two's complement signed integer. $\forall i \in [0..255] : \mu'_s[0]_i \equiv \begin{cases} \mu_s[1]_t & \text{if } i \leq t \text{ where } t = 256 - 8(\mu_s[0] + 1) \\ \mu_s[1]_i & \text{otherwise} \end{cases}$

$\mu_s[x]_i$ gives the i th bit (counting from zero) of $\mu_s[x]$

10s: Comparison & Bitwise Logic Operations				
Value	Mnemonic	δ	ρ	Description
0x10	LT	2	1	Less-than comparison. $\mu'_s[0] \equiv \begin{cases} 1 & \text{if } \mu_s[0] < \mu_s[1] \\ 0 & \text{otherwise} \end{cases}$
0x11	GT	2	1	Greater-than comparison. $\mu'_s[0] \equiv \begin{cases} 1 & \text{if } \mu_s[0] > \mu_s[1] \\ 0 & \text{otherwise} \end{cases}$
0x12	SLT	2	1	Signed less-than comparison. $\mu'_s[0] \equiv \begin{cases} 1 & \text{if } \mu_s[0] < \mu_s[1] \\ 0 & \text{otherwise} \end{cases}$ <p>Where all values are treated as two's complement signed 256-bit integers.</p>
0x13	SGT	2	1	Signed greater-than comparison. $\mu'_s[0] \equiv \begin{cases} 1 & \text{if } \mu_s[0] > \mu_s[1] \\ 0 & \text{otherwise} \end{cases}$ <p>Where all values are treated as two's complement signed 256-bit integers.</p>
0x14	EQ	2	1	Equality comparison. $\mu'_s[0] \equiv \begin{cases} 1 & \text{if } \mu_s[0] = \mu_s[1] \\ 0 & \text{otherwise} \end{cases}$
0x15	ISZERO	1	1	Simple not operator. $\mu'_s[0] \equiv \begin{cases} 1 & \text{if } \mu_s[0] = 0 \\ 0 & \text{otherwise} \end{cases}$
0x16	AND	2	1	Bitwise AND operation. $\forall i \in [0..255] : \mu'_s[0]_i \equiv \mu_s[0]_i \wedge \mu_s[1]_i$
0x17	OR	2	1	Bitwise OR operation. $\forall i \in [0..255] : \mu'_s[0]_i \equiv \mu_s[0]_i \vee \mu_s[1]_i$
0x18	XOR	2	1	Bitwise XOR operation. $\forall i \in [0..255] : \mu'_s[0]_i \equiv \mu_s[0]_i \oplus \mu_s[1]_i$
0x19	NOT	1	1	Bitwise NOT operation. $\forall i \in [0..255] : \mu'_s[0]_i \equiv \begin{cases} 1 & \text{if } \mu_s[0]_i = 0 \\ 0 & \text{otherwise} \end{cases}$
0x1a	BYTE	2	1	Retrieve single byte from word. $\forall i \in [0..255] : \mu'_s[0]_i \equiv \begin{cases} \mu_s[1]_{(i+8\mu_s[0])} & \text{if } i < 8 \wedge \mu_s[0] < 32 \\ 0 & \text{otherwise} \end{cases}$ <p>For the Nth byte, we count from the left (i.e. N=0 would be the most significant in big endian).</p>
0x1b	SHL	2	1	Left shift operation. $\mu'_s[0] \equiv (\mu_s[1] \times 2^{\mu_s[0]}) \bmod 2^{256}$
0x1c	SHR	2	1	Logical right shift operation. $\mu'_s[0] \equiv \lfloor \mu_s[1] \div 2^{\mu_s[0]} \rfloor$
0x1d	SAR	2	1	Arithmetic (signed) right shift operation. $\mu'_s[0] \equiv \lfloor \mu_s[1] \div 2^{\mu_s[0]} \rfloor$ <p>Where $\mu'_s[0]$ and $\mu_s[1]$ are treated as two's complement signed 256-bit integers, while $\mu_s[0]$ is treated as unsigned.</p>

20s: SHA3				
Value	Mnemonic	δ	ρ	Description
0x20	SHA3	2	1	Compute Keccak-256 hash. $\mu'_s[0] \equiv \text{KEC}(\mu_m[\mu_s[0] \dots (\mu_s[0] + \mu_s[1] - 1)])$ $\mu'_i \equiv M(\mu_i, \mu_s[0], \mu_s[1])$

30s: Environmental Information				
Value	Mnemonic	δ	ρ	Description
0x30	ADDRESS	0	1	Get address of currently executing account. $\mu'_s[0] \equiv I_a$
0x31	BALANCE	1	1	Get balance of the given account. $\mu'_s[0] \equiv \begin{cases} \sigma[\mu_s[0]]_b & \text{if } \sigma[\mu_s[0] \bmod 2^{160}] \neq \emptyset \\ 0 & \text{otherwise} \end{cases}$
0x32	ORIGIN	0	1	Get execution origination address. $\mu'_s[0] \equiv I_o$ This is the sender of original transaction; it is never an account with non-empty associated code.
0x33	CALLER	0	1	Get caller address. $\mu'_s[0] \equiv I_s$ This is the address of the account that is directly responsible for this execution.
0x34	CALLVALUE	0	1	Get deposited value by the instruction/transaction responsible for this execution. $\mu'_s[0] \equiv I_v$
0x35	CALLDATALOAD	1	1	Get input data of current environment. $\mu'_s[0] \equiv I_d[\mu_s[0] \dots (\mu_s[0] + 31)]$ with $I_d[x] = 0$ if $x \geq \ I_d\ $ This pertains to the input data passed with the message call instruction or transaction.
0x36	CALLDATASIZE	0	1	Get size of input data in current environment. $\mu'_s[0] \equiv \ I_d\ $ This pertains to the input data passed with the message call instruction or transaction.
0x37	CALLDATACOPY	3	0	Copy input data in current environment to memory. $\forall i \in \{0 \dots \mu_s[2] - 1\} : \mu'_m[\mu_s[0] + i] \equiv \begin{cases} I_d[\mu_s[1] + i] & \text{if } \mu_s[1] + i < \ I_d\ \\ 0 & \text{otherwise} \end{cases}$ The additions in $\mu_s[1] + i$ are not subject to the 2^{256} modulo. $\mu'_i \equiv M(\mu_i, \mu_s[0], \mu_s[2])$ This pertains to the input data passed with the message call instruction or transaction.
0x38	CODESIZE	0	1	Get size of code running in current environment. $\mu'_s[0] \equiv \ I_b\ $
0x39	CODECOPY	3	0	Copy code running in current environment to memory. $\forall i \in \{0 \dots \mu_s[2] - 1\} : \mu'_m[\mu_s[0] + i] \equiv \begin{cases} I_b[\mu_s[1] + i] & \text{if } \mu_s[1] + i < \ I_b\ \\ \text{STOP} & \text{otherwise} \end{cases}$ $\mu'_i \equiv M(\mu_i, \mu_s[0], \mu_s[2])$ The additions in $\mu_s[1] + i$ are not subject to the 2^{256} modulo.
0x3a	GASPRICE	0	1	Get price of gas in current environment. $\mu'_s[0] \equiv I_p$ This is gas price specified by the originating transaction.
0x3b	EXTCODESIZE	1	1	Get size of an account's code. $\mu'_s[0] \equiv \ b\ $ where $\text{KEC}(b) \equiv \sigma[\mu_s[0] \bmod 2^{160}]_c$

0x3c	EXTCODECOPY	4	0	<p>Copy an account's code to memory.</p> $\forall i \in \{0 \dots \mu_s[3] - 1\} : \mu'_m[\mu_s[1] + i] \equiv \begin{cases} \mathbf{b}[\mu_s[2] + i] & \text{if } \mu_s[2] + i < \ \mathbf{b}\ \\ \text{STOP} & \text{otherwise} \end{cases}$ <p>where $\text{KEC}(\mathbf{b}) \equiv \sigma[\mu_s[0] \bmod 2^{160}]_c$ $\mu'_i \equiv M(\mu_i, \mu_s[1], \mu_s[3])$ The additions in $\mu_s[2] + i$ are not subject to the 2^{256} modulo.</p>
0x3d	RETURNDATASIZE	0	1	<p>Get size of output data from the previous call from the current environment.</p> $\mu'_s[0] \equiv \ \mu_o\ $
0x3e	RETURNDATACOPY	3	0	<p>Copy output data from the previous call to memory.</p> $\forall i \in \{0 \dots \mu_s[2] - 1\} : \mu'_m[\mu_s[0] + i] \equiv \begin{cases} \mu_o[\mu_s[1] + i] & \text{if } \mu_s[1] + i < \ \mu_o\ \\ 0 & \text{otherwise} \end{cases}$ <p>The additions in $\mu_s[1] + i$ are not subject to the 2^{256} modulo. $\mu'_i \equiv M(\mu_i, \mu_s[0], \mu_s[2])$</p>
0x3f	EXTCODEHASH	1	1	<p>Get hash of an account's code.</p> $\mu'_s[0] \equiv \begin{cases} 0 & \text{if } \text{DEAD}(\sigma, \mu_s[0] \bmod 2^{160}) \\ \sigma[\mu_s[0] \bmod 2^{160}]_c & \text{otherwise} \end{cases}$

40s: Block Information

Value	Mnemonic	δ	ρ	Description
0x40	BLOCKHASH	1	1	<p>Get the hash of the last block.</p> <p>In Conflux, we only maintain the block hash of the previous block. When querying other block numbers, the returned result is always 0.</p> $\mu'_s[0] \equiv \begin{cases} I_{H_p} & \text{if } \mu_s[0] = H_i \\ 0 & \text{otherwise} \end{cases}$
0x41	COINBASE	0	1	<p>Get the block's beneficiary address.</p> $\mu'_s[0] \equiv I_{H_c}$
0x42	TIMESTAMP	0	1	<p>Get the block's timestamp.</p> $\mu'_s[0] \equiv I_{H_s}$
0x43	NUMBER	0	1	<p>Get the block's number.</p> $\mu'_s[0] \equiv I_{H_i}$
0x44	DIFFICULTY	0	1	<p>Get the block's difficulty.</p> $\mu'_s[0] \equiv I_{H_d}$
0x45	GASLIMIT	0	1	<p>Get the block's gas limit.</p> $\mu'_s[0] \equiv I_{H_l}$
0x46	CHAINID	0	1	<p>Get the chain ID.</p> $\mu'_s[0] \equiv 503$
0x47	SELFBALANCE	0	1	<p>Get balance of the currently executing account.</p> $\mu'_s[0] \equiv \begin{cases} \sigma[I_a]_b & \text{if } \sigma[I_a \bmod 2^{160}] \neq \emptyset \\ 0 & \text{otherwise} \end{cases}$

50s: Stack, Memory, Storage and Flow Operations				
Value	Mnemonic	δ	ρ	Description
0x50	POP	1	0	Remove item from stack.
0x51	MLOAD	1	1	Load word from memory. $\mu'_s[0] \equiv \mu_m[\mu_s[0] \dots (\mu_s[0] + 31)]$ $\mu'_i \equiv \max(\mu_i, \lceil (\mu_s[0] + 32) \div 32 \rceil)$ The addition in the calculation of μ'_i is not subject to the 2^{256} modulo.
0x52	MSTORE	2	0	Save word to memory. $\mu'_m[\mu_s[0] \dots (\mu_s[0] + 31)] \equiv \mu_s[1]$ $\mu'_i \equiv \max(\mu_i, \lceil (\mu_s[0] + 32) \div 32 \rceil)$ The addition in the calculation of μ'_i is not subject to the 2^{256} modulo.
0x53	MSTORE8	2	0	Save byte to memory. $\mu'_m[\mu_s[0]] \equiv (\mu_s[1] \bmod 256)$ $\mu'_i \equiv \max(\mu_i, \lceil (\mu_s[0] + 1) \div 32 \rceil)$ The addition in the calculation of μ'_i is not subject to the 2^{256} modulo.
0x54	SLOAD	1	1	Load word from storage. $\mu'_s[0] \equiv \sigma[l_a]_s[\mu_s[0]]$
0x55	SSTORE	2	0	Save word to storage. $\sigma'[l_a]_s[\mu_s[0]] \equiv \mu_s[1]$
0x56	JUMP	1	0	Alter the program counter. $J_{\text{JUMP}}(\mu) \equiv \mu_s[0]$ This has the effect of writing said value to μ_{pc} . See (139) in Section 5.6.
0x57	JUMPI	2	0	Conditionally alter the program counter. $J_{\text{JUMPI}}(\mu) \equiv \begin{cases} \mu_s[0] & \text{if } \mu_s[1] \neq 0 \\ \mu_{\text{pc}} + 1 & \text{otherwise} \end{cases}$ This has the effect of writing said value to μ_{pc} . See (139) in Section 5.6.
0x58	PC	0	1	Get the value of the program counter <i>prior</i> to the increment corresponding to this instruction. $\mu'_s[0] \equiv \mu_{\text{pc}}$
0x59	MSIZE	0	1	Get the size of active memory in bytes. $\mu'_s[0] \equiv 32\mu_i$
0x5a	GAS	0	1	Get the amount of available gas, including the corresponding reduction for the cost of this instruction. $\mu'_s[0] \equiv \mu_g$
0x5b	JUMPDEST	0	0	Mark a valid destination for jumps. This operation has no effect on machine state during execution.

50s: Stack, Memory, Storage and Flow Operations – Subroutine Operations

- Note 1:** Here we list columns of δ^* and ρ^* because JUMPSUB and RETURNSUB may change the return stack μ_r . However, μ_r is only alterable by these two instructions, and hence there is no need to validate popped values.
- Note 2:** The actual state of the return stack is neither observable by EVM code nor consensus-critical to the protocol. Thus, a node implementor may code JUMPSUB to unobservably push pc on the return stack rather than pc + 1, which is allowed so long as the next RETURNSUB would observably return control to the pc + 1 location.

Value	Mnemonic	δ	ρ	δ^*	ρ^*	Description
0x5c	BEGINSUB	0	0	0	0	Marks the entry point to a subroutine. Attempted execution of a BEGINSUB causes an abort: terminate execution with an OOG (<i>Out Of Gas</i>) exception.
0x5d	RETURNSUB	0	0	1	0	Returns from a subroutine. If $\ \mu_r\ = 0$, then abort: terminate execution with a <i>Return Stack Underflow</i> exception. Otherwise $J_{\text{RETURNSUB}}(\mu) \equiv \mu_r[0]$ This has the effect of writing said value to μ_{pc} . See (139) in Section 5.6.
0x5e	JUMPSUB	1	0	0	1	Jumps to a defined BEGINSUB subroutine and transfers control to it. If $\ \mu_r\ = 1023$, then abort: terminate execution with an <i>Out Of Return Stack</i> exception. Else if $I_b[\mu_s[0]] \neq \text{BEGINSUB}$ then abort: terminate execution with a <i>Bad Jump Destination</i> exception. Otherwise: $\mu'_r[0] \equiv \mu_{pc} + 1$ $J_{\text{JUMPSUB}}(\mu) \equiv \mu_s[0] + 1$ This has the effect of writing said value to μ_{pc} . See (139) in Section 5.6. In case $\mu_s[0] + 1 \geq \ I_b\ $, i.e. the resulting pc is beyond the last instruction, then the opcode is implicitly a STOP, which is not an error.

60s & 70s: Push Operations

Value	Mnemonic	δ	ρ	Description
0x60	PUSH1	0	1	Place 1 byte item on stack. $\mu'_s[0] \equiv c(\mu_{pc} + 1)$ where $c(x) \equiv \begin{cases} I_b[x] & \text{if } x < \ I_b\ \\ 0 & \text{otherwise} \end{cases}$ The bytes are read in line from the program code's bytes array. The function c ensures the bytes default to zero if they extend past the limits. The byte is right-aligned (takes the lowest significant place in big endian).
0x61	PUSH2	0	1	Place 2-byte item on stack. $\mu'_s[0] \equiv c((\mu_{pc} + 1) \dots (\mu_{pc} + 2))$ with $c(x) \equiv (c(x_0), \dots, c(x_{ x -1}))$ with c as defined as above. The bytes are right-aligned (takes the lowest significant place in big endian).
⋮	⋮	⋮	⋮	⋮
0x7f	PUSH32	0	1	Place 32-byte (full word) item on stack. $\mu'_s[0] \equiv c((\mu_{pc} + 1) \dots (\mu_{pc} + 32))$ where c is defined as above. The bytes are right-aligned (takes the lowest significant place in big endian).

80s: Duplication Operations

Value	Mnemonic	δ	ρ	Description
0x80	DUP1	1	2	Duplicate 1st stack item. $\mu'_s[0] \equiv \mu_s[0]$
0x81	DUP2	2	3	Duplicate 2nd stack item. $\mu'_s[0] \equiv \mu_s[1]$
⋮	⋮	⋮	⋮	⋮
0x8f	DUP16	16	17	Duplicate 16th stack item. $\mu'_s[0] \equiv \mu_s[15]$

90s: Exchange Operations

Value	Mnemonic	δ	ρ	Description
0x90	SWAP1	2	2	Exchange 1st and 2nd stack items. $\mu'_s[0] \equiv \mu_s[1]$ $\mu'_s[1] \equiv \mu_s[0]$
0x91	SWAP2	3	3	Exchange 1st and 3rd stack items. $\mu'_s[0] \equiv \mu_s[2]$ $\mu'_s[2] \equiv \mu_s[0]$
⋮	⋮	⋮	⋮	⋮
0x9f	SWAP16	17	17	Exchange 1st and 17th stack items. $\mu'_s[0] \equiv \mu_s[16]$ $\mu'_s[16] \equiv \mu_s[0]$

a0s: Logging Operations

For all logging operations, the state change is to append an additional log entry on to the substate's log series:

$$A'_1 \equiv A_1 \cdot (I_a, \mathbf{t}, \mu_m[\mu_s[0] \dots (\mu_s[0] + \mu_s[1] - 1)])$$

and to update the memory consumption counter:

$$\mu'_i \equiv M(\mu_i, \mu_s[0], \mu_s[1])$$

The entry's topic series, \mathbf{t} , differs accordingly:

Value	Mnemonic	δ	ρ	Description
0xa0	LOG0	2	0	Append log record with no topics. $\mathbf{t} \equiv \varepsilon$
0xa1	LOG1	3	0	Append log record with one topic. $\mathbf{t} \equiv (\mu_s[2])$
⋮	⋮	⋮	⋮	⋮
0xa4	LOG4	6	0	Append log record with four topics. $\mathbf{t} \equiv (\mu_s[2], \mu_s[3], \mu_s[4], \mu_s[5])$

f0s: System operations

Value	Mnemonic	δ	ρ	Description
0xf0	CREATE	3	1	<p>Create a new account with associated code.</p> <p>$\mathbf{i} \equiv \mu_{\mathbf{m}}[\mu_{\mathbf{s}}[1] \dots (\mu_{\mathbf{s}}[1] + \mu_{\mathbf{s}}[2] - 1)]$ $\zeta \equiv \emptyset$</p> $(\sigma', \mu'_g, A^+, \mathbf{o}) \equiv \begin{cases} \Lambda(\sigma^*, I_a, I_o, L(\mu_g), I_p, \mu_{\mathbf{s}}[0], \mathbf{i}, I_e + 1, \zeta, I_w) & \text{if } \mu_{\mathbf{s}}[0] \leq \sigma[I_a]_b \\ & \wedge I_e < 1024 \\ (\sigma, \mu_g, \emptyset) & \text{otherwise} \end{cases}$ <p>$\sigma^* \equiv \sigma$ except $\sigma^*[I_a]_n = \sigma[I_a]_n + 1$ $A' \equiv A \uplus A^+$ which abbreviates: $A'_s \equiv A_s \cup A_s^+ \quad \wedge \quad A'_t \equiv A_t \cdot A_t^+ \quad \wedge$ $A'_r \equiv A_r \cup A_r^+ \quad \wedge \quad A'_r \equiv A_r + A_r^+$ $\mu'_s[0] \equiv x$ where $x = 0$ if the code execution for this operation failed due to an exceptional halting (or for a REVERT) $\sigma' = \emptyset$, or $I_e = 1024$ (the maximum call depth limit is reached) or $\mu_{\mathbf{s}}[0] > \sigma[I_a]_b$ (balance of the caller is too low to fulfil the value transfer); and otherwise $x = A(I_a, \sigma[I_a]_n, \zeta, \mathbf{i})$, the address of the newly created account (69). $\mu'_i \equiv M(\mu_i, \mu_{\mathbf{s}}[1], \mu_{\mathbf{s}}[2])$ $\mu'_o \equiv \varepsilon$ Thus the operand order is: value, input offset, input size.</p>
0xf1	CALL	7	1	<p>Message-call into an account.</p> <p>$\mathbf{i} \equiv \mu_{\mathbf{m}}[\mu_{\mathbf{s}}[3] \dots (\mu_{\mathbf{s}}[3] + \mu_{\mathbf{s}}[4] - 1)]$</p> $(\sigma', g', A^+, \mathbf{o}) \equiv \begin{cases} \Theta(\sigma, I_a, I_o, t, t, C_{\text{CALLGAS}}(\mu), & \text{if } \mu_{\mathbf{s}}[2] \leq \sigma[I_a]_b \wedge \\ I_p, \mu_{\mathbf{s}}[2], \mu_{\mathbf{s}}[2], \mathbf{i}, I_e + 1, I_w) & I_e < 1024 \\ (\sigma, g, \emptyset, \varepsilon) & \text{otherwise} \end{cases}$ <p>$n \equiv \min(\{\mu_{\mathbf{s}}[6], \ \mathbf{o}\ \})$ $\mu'_{\mathbf{m}}[\mu_{\mathbf{s}}[5] \dots (\mu_{\mathbf{s}}[5] + n - 1)] = \mathbf{o}[0 \dots (n - 1)]$ $\mu'_o = \mathbf{o}$ $\mu'_g \equiv \mu_g + g'$ $\mu'_s[0] \equiv x$ $A' \equiv A \uplus A^+$ $t \equiv \mu_{\mathbf{s}}[1] \pmod{2^{160}}$ where $x = 0$ if the code execution for this operation failed due to an exceptional halting (or for a REVERT) $\sigma' = \emptyset$ or if $\mu_{\mathbf{s}}[2] > \sigma[I_a]_b$ (not enough funds) or $I_e = 1024$ (call depth limit reached); $x = 1$ otherwise. $\mu'_i \equiv M(M(\mu_i, \mu_{\mathbf{s}}[3], \mu_{\mathbf{s}}[4]), \mu_{\mathbf{s}}[5], \mu_{\mathbf{s}}[6])$ Thus the operand order is: gas, to, value, in offset, in size, out offset, out size. $C_{\text{CALL}}(\sigma, \mu) \equiv C_{\text{GASCAP}}(\sigma, \mu) + C_{\text{EXTRA}}(\sigma, \mu)$ $C_{\text{CALLGAS}}(\sigma, \mu) \equiv \begin{cases} C_{\text{GASCAP}}(\sigma, \mu) + G_{\text{callstipend}} & \text{if } \mu_{\mathbf{s}}[2] \neq 0 \\ C_{\text{GASCAP}}(\sigma, \mu) & \text{otherwise} \end{cases}$ $C_{\text{GASCAP}}(\sigma, \mu) \equiv \begin{cases} \min\{L(\mu_g - C_{\text{EXTRA}}(\sigma, \mu)), \mu_{\mathbf{s}}[0]\} & \text{if } \mu_g \geq C_{\text{EXTRA}}(\sigma, \mu) \\ \mu_{\mathbf{s}}[0] & \text{otherwise} \end{cases}$ $C_{\text{EXTRA}}(\sigma, \mu) \equiv G_{\text{call}} + C_{\text{XFER}}(\mu) + C_{\text{NEW}}(\sigma, \mu)$ $C_{\text{XFER}}(\mu) \equiv \begin{cases} G_{\text{callvalue}} & \text{if } \mu_{\mathbf{s}}[2] \neq 0 \\ 0 & \text{otherwise} \end{cases}$ $C_{\text{NEW}}(\sigma, \mu) \equiv \begin{cases} G_{\text{newaccount}} & \text{if } \text{DEAD}(\sigma, \mu_{\mathbf{s}}[1] \pmod{2^{160}}) \wedge \mu_{\mathbf{s}}[2] \neq 0 \\ 0 & \text{otherwise} \end{cases}$ </p>

0xf2	CALLCODE	7	1	<p>Message-call into this account with an alternative account's code. Exactly equivalent to CALL except:</p> $(\sigma', g', A^+, \mathbf{o}) \equiv \begin{cases} \Theta(\sigma^*, I_a, I_o, I_a, t, C_{\text{CALLGAS}}(\mu), & \text{if } \mu_s[2] \leq \sigma[I_a]_b \wedge \\ I_p, \mu_s[2], \mu_s[2], \mathbf{i}, I_e + 1, I_w) & I_e < 1024 \\ (\sigma, g, \emptyset, \varepsilon) & \text{otherwise} \end{cases}$ <p>Note the change in the fourth parameter to the call Θ from the 2nd stack value $\mu_s[1]$ (as in CALL) to the present address I_a. This means that the recipient is in fact the same account as at present, simply that the code is overwritten.</p>
0xf3	RETURN	2	0	<p>Halt execution returning output data. $H_{\text{RETURN}}(\mu) \equiv \mu_m[\mu_s[0] \dots (\mu_s[0] + \mu_s[1] - 1)]$ This has the effect of halting the execution at this point with output defined. See section 5.6. $\mu'_i \equiv M(\mu_i, \mu_s[0], \mu_s[1])$</p>
0xf4	DELEGATECALL	6	1	<p>Message-call into this account with an alternative account's code, but persisting the current values for <i>sender</i> and <i>value</i>. Compared with CALL, DELEGATECALL takes one fewer arguments. The omitted argument is $\mu_s[2]$. As a result, $\mu_s[3]$, $\mu_s[4]$, $\mu_s[5]$ and $\mu_s[6]$ in the definition of CALL should respectively be replaced with $\mu_s[2]$, $\mu_s[3]$, $\mu_s[4]$ and $\mu_s[5]$. Otherwise it is equivalent to CALL except:</p> $(\sigma', g', A^+, \mathbf{o}) \equiv \begin{cases} \Theta(\sigma^*, I_s, I_o, I_a, t, C_{\text{CALLGAS}}(\mu), & \text{if } I_v \leq \sigma[I_a]_b \wedge \\ I_p, 0, I_v, \mathbf{i}, I_e + 1, I_w) & I_e < 1024 \\ (\sigma, g, \emptyset, \varepsilon) & \text{otherwise} \end{cases}$ <p>Note the changes (in addition to that of the fourth parameter) to the second and ninth parameters to the call Θ. This means that the recipient is in fact the same account as at present, simply that the code is overwritten <i>and</i> the context is almost entirely identical.</p>
0xf5	CREATE2	4	1	<p>Create a new account with associated code. Exactly equivalent to CREATE except: The salt $\zeta \equiv \mu_s[3]$.</p>
0xfa	STATICCALL	6	1	<p>Static message-call into an account. Exactly equivalent to CALL except: The argument $\mu_s[2]$ is replaced with 0. The deeper argument $\mu_s[3]$, $\mu_s[4]$, $\mu_s[5]$ and $\mu_s[6]$ are respectively replaced with $\mu_s[2]$, $\mu_s[3]$, $\mu_s[4]$ and $\mu_s[5]$. The last argument of Θ is \perp.</p>
0xfd	REVERT	2	0	<p>Halt execution reverting state changes but returning data and remaining gas. The effect of this operation is described in (123). For the gas calculation, we use the memory expansion function, $\mu'_i \equiv M(\mu_i, \mu_s[0], \mu_s[1])$</p>
0xfe	INVALID	\emptyset	\emptyset	Designated invalid instruction.
0xff	SELFDESTRUCT	1	0	<p>Halt execution and register account for later deletion. $A'_s \equiv A_s \cup \{I_a\}$</p> $\sigma'[r] \equiv \begin{cases} \emptyset & \text{if } \sigma[r] = \emptyset \wedge \sigma[I_a]_b = 0 \\ (\sigma[r]_n, \sigma[r]_b + \sigma[I_a]_b, \sigma[r]_s, \sigma[r]_c) & \text{if } r \neq I_a \\ (\sigma[r]_n, 0, \sigma[r]_s, \sigma[r]_c) & \text{otherwise} \end{cases}$ <p>where $r = \mu_s[0] \bmod 2^{160}$</p> $\sigma'[I_a]_b = 0$ $C_{\text{SELFDESTRUCT}}(\sigma, \mu) \equiv G_{\text{selfdestruct}} + \begin{cases} G_{\text{newaccount}} & \text{if } n \\ 0 & \text{otherwise} \end{cases}$ $n \equiv \text{DEAD}(\sigma, \mu_s[0] \bmod 2^{160}) \wedge \sigma[I_a]_b \neq 0$

Appendix E. Multi-point Evaluation Hashing

E.1 Definitions

We employ the following definitions:

Name	Value	Description
$J_{wordbytes}$	4	Bytes in word.
$J_{datasetinit}$	3×2^{31}	Bytes in dataset at genesis.
$J_{datasetgrowth}$	2^{24}	Dataset growth per stage.
$J_{cacheinit}$	3×2^{23}	Bytes in cache at genesis.
$J_{cachegrowth}$	2^{16}	Cache growth per stage.
J_{stage}	2^{19}	Epoches per stage.
$J_{mixbytes}$	128	mix length in bytes.
$J_{hashbytes}$	64	Hash length in bytes.
$J_{parents}$	256	Number of parents of each dataset element.
$J_{cacherrounds}$	3	Number of rounds in cache production.
$J_{accesses}$	64	Number of accesses in hashimoto loop.

E.2 Size of dataset and cache

The size for the hash function's cache $\mathbf{c} \in \mathbb{B}^*$ and dataset $\mathbf{d} \in \mathbb{B}^*$ depend on the stage, which in turn depends on the block height H_h .

$$E_{stage}(H_h) \equiv \left\lfloor \frac{H_h}{J_{stage}} \right\rfloor \quad (189)$$

The size of the dataset growth by $J_{datasetgrowth}$ bytes, and the size of the cache by $J_{cachegrowth}$ bytes, every stage. In order to avoid regularity leading to cyclic behavior, the size must be a prime number. Therefore the size is reduced by a multiple of $J_{mixbytes}$, for the dataset, and $J_{hashbytes}$ for the cache. Let $d_{size} = \|\mathbf{d}\|$ be the size of the dataset, which is calculated using

$$d_{size} \equiv E_{prime}(J_{datasetinit} + J_{datasetgrowth} \cdot E_{stage} - J_{mixbytes}, J_{mixbytes}) \quad (190)$$

The size of the cache, c_{size} , is calculated using

$$c_{size} \equiv E_{prime}(J_{cacheinit} + J_{cachegrowth} \cdot E_{stage} - J_{hashbytes}, J_{hashbytes}) \quad (191)$$

where $E_{prime}(x, y)$ computes the greatest integer x' below x such that x'/y is a prime (given that $x \gg y$).

$$E_{prime}(x, y) \equiv \begin{cases} x & \text{if } x/y \text{ is prime} \\ E_{prime}(x - 2 \cdot y, y) & \text{if } x/y \text{ is not prime but } x/y \in \mathbb{N} \\ E_{prime}(\lfloor x/y \rfloor \cdot y, y) & \text{otherwise (} x \text{ is rounded to a multiple of } y) \end{cases} \quad (192)$$

E.3 Dataset generation

In order to generate the dataset we need the cache \mathbf{c} , which is an array of bytes. It depends on the cache size c_{size} and the seed hash $\mathbf{s} \in \mathbb{B}_{256}$.

E.3.1 Seed hash

The seed hash is different for every stage. For the first stage it is the Keccak-256 hash of a series of 256 bits (32 bytes) of zeros. For every other stage it is always the Keccak-256 hash of the previous seed hash:

$$\mathbf{s} \equiv C_{seedhash}(H_h) \quad (193)$$

$$C_{seedhash}(H_h) \equiv \begin{cases} \mathbf{0}_{256} & \text{if } E_{stage}(H_h) = 0 \\ \text{KEC}(C_{seedhash}(H_h - J_{stage})) & \text{otherwise} \end{cases} \quad (194)$$

where $\mathbf{0}_{256}$ denotes 256 bits of zeros.

E.3.2 Cache

The cache production process involves using the seed hash to first sequentially filling up c_{size} bytes of memory, then performing $J_{cacherounds}$ passes of the RandMemoHash algorithm created by [4]. The initial cache \mathbf{c}' will be constructed as follows.

Recalling that KECS12 denotes the Keccak-512 hash function whose output length is 512 bits (64 single bytes), we define the array \mathbf{c}_i as the i -th element of the initial cache:

$$\mathbf{c}_i \equiv \begin{cases} \text{KECS12}(\mathbf{s}) & \text{if } i = 0 \\ \text{KECS12}(\mathbf{c}_{i-1}) & \text{otherwise} \end{cases} \quad (195)$$

Let n denote the number of elements in cache:

$$n \equiv \lfloor c_{size} / J_{hashbytes} \rfloor \quad (196)$$

The initial cache \mathbf{c}' can be defined as:

$$\mathbf{c}'[i] \equiv \mathbf{c}_i, \quad \forall i \in \{0, 1, 2, \dots, n-1\} \quad (197)$$

The cache \mathbf{c} , consisting of n items of KECS12 hash values, is calculated by performing $J_{cacherounds}$ rounds of the RandMemoHash algorithm to the initial cache \mathbf{c}' :

$$\mathbf{c} \equiv E_{cacherounds}(\mathbf{c}', J_{cacherounds}) \quad (198)$$

$$E_{cacherounds}(\mathbf{x}, y) \equiv \begin{cases} \mathbf{x} & \text{if } y = 0 \\ E_{\text{RMH}}(\mathbf{x}) & \text{if } y = 1 \\ E_{cacherounds}(E_{\text{RMH}}(\mathbf{x}), y-1) & \text{otherwise} \end{cases} \quad (199)$$

Every single round of the RandMemoHash algorithm modifies each subset of the cache as follows:

$$E_{\text{RMH}}(\mathbf{x}) \equiv (E_{\text{rmh}}(\mathbf{x}, 0), E_{\text{rmh}}(\mathbf{x}, 1), \dots, E_{\text{rmh}}(\mathbf{x}, n-1)) \quad (200)$$

$$E_{\text{rmh}}(\mathbf{x}, i) \equiv \text{KECS12}(\mathbf{x}'[(i-1+n) \bmod n] \oplus \mathbf{x}'[\mathbf{x}'[i][0] \bmod n]) \\ \text{with } \mathbf{x}' = \mathbf{x} \text{ except } \mathbf{x}'[j] = E_{\text{rmh}}(\mathbf{x}, j), \quad \forall j < i \quad (201)$$

E.3.3 Full dataset calculation

Essentially, we combine data from $J_{parents}$ pseudorandomly selected cache nodes, and hash that to compute the dataset. The entire dataset is then generated by a number of items, each of $J_{hashbytes}$ bytes in size:

$$\mathbf{d}[i] \equiv E_{datasetitem}(\mathbf{c}, i), \quad \forall i < \left\lfloor \frac{d_{size}}{J_{hashbytes}} \right\rfloor \quad (202)$$

In order to calculate the single item we use an algorithm $E_{\text{FNV}} : \mathbb{B}_{32} \times \mathbb{B}_{32} \rightarrow \mathbb{B}_{32}$ inspired by the FNV hash [5] in some cases as a non-associative substitute for XOR.

$$E_{\text{FNV}}(\mathbf{x}, \mathbf{y}) \equiv ((\mathbf{x} \times 0x01000193) \oplus \mathbf{y}) \bmod 2^{32} \quad (203)$$

The single item of the dataset can now be calculated by iteratively mixing items from the cache \mathbf{c} as follows:

$$E_{datasetitem}(\mathbf{c}, i) \equiv \text{KECS12}\left(E_{parents}(\mathbf{c}, i, 0, \text{KECS12}(\mathbf{c}[i \bmod n] \oplus i))\right) \quad (204)$$

$$E_{parents}(\mathbf{c}, i, p, \mathbf{m}) \equiv \begin{cases} E_{parents}(\mathbf{c}, i, p+1, E_{mix}(\mathbf{m}, \mathbf{c}, i, p)) & \text{if } p < J_{parents} - 1 \\ E_{mix}(\mathbf{m}, \mathbf{c}, i, p) & \text{otherwise} \end{cases} \quad (205)$$

$$E_{mix}(\mathbf{m}, \mathbf{c}, i, p) \equiv E_{\text{FNV}}^*\left(\mathbf{m}, \mathbf{c}[E_{\text{FNV}}(i \oplus p, \mathbf{m}[p \bmod \lfloor J_{hashbytes} / J_{wordbytes} \rfloor]) \bmod n]\right) \quad (206)$$

where $\mathbf{m} \in \mathbb{B}_{512}$ should be interpreted as an array of $\lfloor J_{hashbytes} / J_{wordbytes} \rfloor$ words (each of $J_{wordbytes}$ bytes, i.e. 32 bits), and E_{FNV}^* denotes the element-wise invocation of E_{FNV} .

E.4 Proof-of-work function

Essentially, we maintain a “mix” of $J_{mixbytes}$ bytes wide, and repeatedly sequentially fetch $J_{mixbytes}$ bytes from the full dataset and use the E_{FNV} function to combine it with the mix. $J_{mixbytes}$ bytes of sequential access are used so that each round of the algorithm always fetches a full page from RAM, minimizing translation lookaside buffer misses which ASICs would theoretically be able to avoid.

If the output of this algorithm is below the desired target, then the nonce is valid. Note that the extra application of KEC at the end ensures that there exists an intermediate nonce which can be provided to prove that at least a small amount of work was done; this quick outer PoW verification can be used for anti-DDoS purposes. It also serves to provide statistical assurance that the result is an unbiased, 256 bit number.

The MpEhash function takes $H_{\mathcal{H}}$, which is the hash of the header excluding the **mixHash** and **nonce** fields, i.e. $H_{\mathcal{H}} \equiv \text{KEC}(\text{RLP}(H_{-n}))$, together with the nonce H_n and the dataset \mathbf{d} from appendix E.3.3 as input. The output of MpEhash consists of an array with the compressed mix \mathbf{m}_c as its first item and the Keccak-256 hash of the concatenation of the seed hash $\mathbf{s}_h \in \mathbb{B}_{512}$, the compressed mix $\mathbf{m}_c \in \mathbb{B}_{256}$, and the compressed multi-point mix $m_p \in \mathbb{B}_{32}$ as the second item:

$$\text{MpEhash}(H_{\mathcal{H}}, H_n, \mathbf{d}) \equiv \{\mathbf{m}_c, \text{KEC}(\mathbf{s}_h \circ \mathbf{m}_c \circ m_p)\} \quad (207)$$

E.4.1 Seed hash

The seed hash $\mathbf{s}_h \in \mathbb{B}_{512} = \mathbb{B}\mathbb{Y}_{J_{hashbytes}}$ is defined on $H_{\mathcal{H}}$ and H_n as follows:

$$\mathbf{s}_h \equiv \mathbf{s}_h(H_{\mathcal{H}}, H_n) \equiv \text{KEC512}(H_{\mathcal{H}} \circ E_{revert}(H_n)) \quad (208)$$

where $E_{revert}(H_n)$ returns the reverted bytes sequence of the nonce H_n as $E_{revert}(H_n)[i] \equiv H_n[\|H_n\| - i]$, so that the 64-bit nonce in big-endian order is changed to little-endian representation.

E.4.2 Compressed mix

The compressed mix $\mathbf{m}_c \in \mathbb{B}_{256}$ is obtained from the seed hash \mathbf{s}_h and the dataset \mathbf{d} :

$$\mathbf{m}_c \equiv \mathbf{m}_c(\mathbf{s}_h, \mathbf{d}) \equiv E_{compress}(E_{accesses}(\mathbf{d}, \mathbf{m}_0, \mathbf{s}_h, 0), 0) \quad (209)$$

where \mathbf{m}_0 and $E_{accesses}$, $E_{compress}$ are defined as follows.

The initial mix \mathbf{m}_0 is an array of $\lfloor J_{mixbytes}/J_{wordbytes} \rfloor$ many 32-bit (i.e. 4-byte) words obtained by replicating the seed hash \mathbf{s}_h for n_{mix} times, with n_{mix} defined as:

$$n_{mix} \equiv \left\lfloor \frac{J_{mixbytes}}{J_{hashbytes}} \right\rfloor \quad (210)$$

Formally, the initial mix $\mathbf{m}_0 \in \mathbb{B}_{512 \cdot n_{mix}} = (\mathbb{B}\mathbb{Y}_{J_{hashbytes}})^{n_{mix}}$ is defined as:

$$\mathbf{m}_0 \equiv \underbrace{\mathbf{s}_h \circ \dots \circ \mathbf{s}_h}_{n_{mix} \text{ many copies of } \mathbf{s}_h} \quad (211)$$

In order to add random dataset nodes to the mix, the $E_{accesses}$ function is used:

$$E_{accesses}(\mathbf{d}, \mathbf{m}, \mathbf{s}, i) \equiv \begin{cases} E_{mixdataset}(\mathbf{d}, \mathbf{m}, \mathbf{s}, i) & \text{if } i = J_{accesses} - 1 \\ E_{accesses}(\mathbf{d}, E_{mixdataset}(\mathbf{d}, \mathbf{m}, \mathbf{s}, i), \mathbf{s}, i + 1) & \text{otherwise} \end{cases} \quad (212)$$

$$E_{mixdataset}(\mathbf{d}, \mathbf{m}, \mathbf{s}, i) \equiv E_{FNV}^*(\mathbf{m}, E_{newdata}(\mathbf{d}, \mathbf{m}, \mathbf{s}, i)) \quad (213)$$

where E_{FNV}^* denotes the element-wise invocation of E_{FNV} on 32-bit elements, and $E_{newdata}$ returns an array consisting of n_{mix} elements from the dataset \mathbf{d} (so that the array is of same length as the intermediate mix \mathbf{m} , i.e. each of $J_{mixbytes} = n_{mix} \cdot J_{hashbytes}$ bytes):

$$E_{newdata}(\mathbf{d}, \mathbf{m}, \mathbf{s}, i)[j] \equiv \mathbf{d}[p \cdot n_{mix} + j], \quad \forall \quad 0 \leq j \leq n_{mix} - 1 \quad (214)$$

with the mixing index p obtained as follows:

$$p \equiv E_{FNV} \left(i \oplus \mathbf{s}[0], \mathbf{m} \left[i \bmod \left\lfloor \frac{J_{mixbytes}}{J_{wordbytes}} \right\rfloor \right] \right) \bmod \left\lfloor \frac{d_{size}/J_{hashbytes}}{n_{mix}} \right\rfloor \quad (215)$$

The $E_{compress}$ function converts $J_{mixbytes}$ -byte mix eventually returned by $E_{accesses}$, which is an array of $\lfloor J_{mixbytes}/J_{wordbytes} \rfloor$ words, into the compressed mix $\mathbf{m}_c \in \mathbb{B}\mathbb{Y}_{32} = \mathbb{B}\mathbb{Y}_{\lfloor J_{mixbytes}/4 \rfloor}$ as follows:

$$E_{compress}(\mathbf{m}, i) \equiv \begin{cases} \varepsilon & \text{if } i \geq \|\mathbf{m}\| - 4 \\ E_{FNV}(E_{FNV}(E_{FNV}(\mathbf{m}[i], \mathbf{m}[i+1]), \mathbf{m}[i+2]), \mathbf{m}[i+3]) \circ E_{compress}(\mathbf{m}, i+4) & \text{otherwise} \end{cases} \quad (216)$$

E.4.3 Multi-point mix

The multi-point mix $m_p \in \mathbb{B}_{32}$ is calculated from the header $H_{\mathcal{H}}$ and \mathbf{s}_h, \mathbf{d} as follows:

$$m_p \equiv m_p(H_{\mathcal{H}}, \mathbf{s}_h, \mathbf{d}) \equiv E_{\text{FNV-compress}}(E_{\text{mp-eval}}(a, b, c, w, \mathbf{z}), J_{\text{accesses}}) \quad (217)$$

with arguments and functions described in the rest of this section.

Interpreting $H_{\mathcal{H}}$ as a byte array, input arguments $a, b, c, w \in \mathbb{B}_{32}$ are defined as follows:

$$a \equiv H_{\mathcal{H}}[0] \quad (218)$$

$$b \equiv H_{\mathcal{H}}[1] \quad (219)$$

$$c \equiv H_{\mathcal{H}}[2] \quad (220)$$

$$w \equiv H_{\mathcal{H}}[3] \quad (221)$$

whereas the last argument \mathbf{z} is an array of J_{accesses} items drawn from \mathbb{B}_{32} . More specifically, $\mathbf{z}[i]$ is defined as:

$$\mathbf{z}[i] \equiv E_{\text{parity}}(E_{\text{mp-accesses}}(\mathbf{d}, \mathbf{m}_0, \mathbf{s}_h, i, 0)), \quad \forall \quad 0 \leq i \leq J_{\text{accesses}} - 1 \quad (222)$$

where the $E_{\text{mp-accesses}}$ function is defined as:

$$E_{\text{mp-accesses}}(\mathbf{d}, \mathbf{m}, \mathbf{s}, i, j) \equiv \begin{cases} E_{\text{mixdataset}}(\mathbf{d}, \mathbf{m}, \mathbf{s}, i) & \text{if } j \geq i \\ E_{\text{mp-accesses}}(\mathbf{d}, E_{\text{mixdataset}}(\mathbf{d}, \mathbf{m}, \mathbf{s}, j), \mathbf{s}, i, j+1) & \text{otherwise} \end{cases} \quad (223)$$

and the E_{parity} function is defined over $\mathbb{B}\mathbb{Y}_{J_{\text{mixbytes}}} \rightarrow \mathbb{B}_{32}$ and it simply returns the parity of all items in the input array at word level (i.e. realizing $\mathbb{B}\mathbb{Y}_{J_{\text{mixbytes}}}$ as $\lfloor J_{\text{mixbytes}}/J_{\text{wordbytes}} \rfloor$ elements each of $J_{\text{wordbytes}}$ bytes), formally defined as:

$$E_{\text{parity}}(\mathbf{m}) \equiv \bigoplus_{i=0}^{\lfloor J_{\text{mixbytes}}/J_{\text{wordbytes}} \rfloor - 1} \mathbf{m}[i] \quad (224)$$

The $E_{\text{mp-eval}}$ function evaluates the polynomial $E_{\text{polynomial}}$ on multiple points $\mathbf{x}[i]$ for $i \in \{0, 1, \dots, J_{\text{accesses}} - 1\}$ and returns the concatenation of J_{accesses} elements drawn from \mathbb{B}_{32} as follows:

$$E_{\text{mp-eval}}(a, b, c, w, \mathbf{z}) \equiv E_{\text{polynomial}}(\mathbf{x}[0]) \circ E_{\text{polynomial}}(\mathbf{x}[1]) \circ \dots \circ E_{\text{polynomial}}(\mathbf{x}[J_{\text{accesses}}-1]) \quad (225)$$

where \mathbf{x} is an array of 32-bit integers defined as:

$$\mathbf{x}[i] \equiv a + b \cdot w^i + c \cdot w^{2i}, \quad \forall \quad 0 \leq i \leq J_{\text{accesses}} - 1 \quad (226)$$

and the $E_{\text{polynomial}}$ function is a polynomial with coefficients specified by \mathbf{z} :

$$E_{\text{polynomial}}(x) \equiv \left(\sum_{j=0}^{J_{\text{accesses}}-1} \mathbf{z}[j] \cdot x^j \right) \pmod{(10^9 + 7)} \quad (227)$$

The FNV-compress function $E_{\text{FNV-compress}}$ is defined over $(\mathbb{B}_{32})^* \times \mathbb{N} \rightarrow \mathbb{B}_{32}$ and used to compress an array of \mathbb{B}_{32} elements into a single \mathbb{B}_{32} element:

$$E_{\text{FNV-compress}}(\mathbf{m}, i) \equiv \begin{cases} \mathbf{0}_{32} & \text{if } i < 1 \\ E_{\text{FNV}}(E_{\text{FNV-compress}}(\mathbf{m}, i-1), \mathbf{m}[i-1]) & \text{otherwise} \end{cases} \quad (228)$$